



# Typing for a Minimal Aspect Language

Peter Hui, James Riely

DePaul CTI

{phui,jriely}@cs.depaul.edu

# $\mu$ ABC

## Minimal Aspect Calculus

- First presented: Bruns, Jagadeesan, et. al (CONCUR'04)
  - First version of  $\mu$ ABC
  - source/target/message model
  - No types
  - Sketches of encodings into  $\mu$ ABC
    - untyped  $\lambda$ -calculus w/aspects (subset of minAML (Walker, Zdancewic, Ligatti))
    - object language

# $\mu$ ABC

- FOAL '06: Temporal variant
- This paper:
  - Nontemporal, polyadic version
    - Provide types for  $\mu$ ABC
    - Provide full translations into  $\mu$ ABC
      - typed, advised  $\lambda$ -Calculus
      - typed, advised object language
  - Translations type-preserving. i.e.:
    - well-typed  $\lambda$ -Calc term  $\Rightarrow$  well-typed  $\mu$ -term
    - well-typed object term  $\Rightarrow$  well-typed  $\mu$ -term

$\mu$ ABC

Example term:

role  
declarations

{  
new a;  
new b;  
new c;

adv(b -> call<c>)  
adv(a -> call<b>)

}  
advice  
declarations

call<a>;

current  
event



# μABC

declarations  
remain  
constant

```
new a;  
new b;  
new c;  
adv(b -> call<c>)  
adv(a -> call<b>)  
call<a>;
```



```
new a;  
new b;  
new c;  
adv(b -> call<c>)  
adv(a -> call<b>)  
[adv(a -> call<b>)]<a>;
```

'call' triggers  
advice lookup

matching advice  
(LIFO)

current event



# $\mu$ ABC

declarations  
remain  
constant

new a;  
new b;  
new c;

adv(b ->call<c>)  
adv(a ->call<b>)

[*adv(a ->call<b>)*]call<b><a>;



new a;  
new b;  
new c;

adv(b ->call<c>)  
adv(a ->call<b>)

call<b>;

advice  
evaluation



$\mu$ ABC

```
new a;  
new b;  
new c;  
adv(b ->call<c>)  
adv(a ->call<b>)  
[adv(b ->call<c>)] <b>;
```



```
new a;  
new b;  
new c;  
adv(b ->call<c>)  
adv(a ->call<b>)  
call<c>;
```

# $\mu$ ABC

“proceed” variable, hierarchical roles:

declarations

```
{  
  new c;  
  new f;  
  new int;  
  new 10:int;  
  adv(f,x:int -> call<c,x>);  
  adv(z;f,x:int -> z<f,x+1>);  
  call<f, 10>;  
}
```



$\mu$ ABC

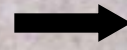
declarations  
remain  
constant

```
new c;  
new f;  
new int;  
new 10:int;  
adv(f,x:int -> call<c,x>);  
adv(z.f,x:int -> z<f,x+1>);  
call<f, 10>;
```

```
new c;  
new f;  
new int;  
new 10:int;  
adv(f,x:int -> call<c,x>);  
adv(z.f,x:int -> z<f,x+1>);  
[adv(f,x:int -> call<c,x>);  
adv(z.f,x:int -> z<f,x+1>);]  
<f, 10>;
```

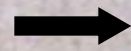
Advice  
"queue"

Current  
event



# $\mu$ ABC

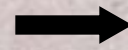
```
new c;  
new f;  
new int;  
new 10:int;  
adv(f,x:int -> call<c,x>);  
adv(z.f,x:int -> z<f,x+1>);  
[adv(f,x:int -> call<c,x>);  
adv(z.f,x:int -> z<f,x+1>);]  
<f, 10>;
```



```
new c;  
new f;  
new int;  
new 10:int;  
adv(f,x:int -> call<c,x>);  
adv(z.f,x:int -> z<f,x+1>);  
[adv(f,x:int -> call<c,x>);]  
<f, 10+1>;
```

# μABC

```
new c;  
new f;  
new int;  
new 10:int;  
adv(f,x:int -> call<c,x>);  
adv(z.f,x:int -> z<f,x+1>);  
[adv(f,x:int -> call<c,x>);]  
  <f, 10+1>;
```



```
new c;  
new f;  
new int;  
new 10:int;  
adv(f,x:int -> call<c,x>);  
adv(z.f,x:int -> z<f,x+1>);  
call<c,10+1>;
```

Note: We have:

- Obliviousness:
  - advice body localized within advice
  - advice can be added without altering program text
- Quantification
  - pointcuts specify which events trigger advice

# Typing

How can a term get stuck?

1.

```
new f;  
adv(z;f ->z<f>)  
call<f>
```



```
new f;  
adv(z;f ->z<f>)  
[adv(z;f ->z<f>)]<f>
```



```
new f;  
adv(z;f ->z<f>)  
[]<f>
```



- Advice proceeds, but with no enqueued advice.

# Typing

How can a term get stuck?

2.

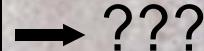
```
...  
new f;  
new g;  
adv(z;f,x,c ->call<c,x>)  
adv(z;f,x,c ->z<g,x>)  
call<f,10,k>
```



```
...  
adv(z;f,x,c ->call<c,x>)  
adv(z;f,x,c ->z<g,x>)  
[adv(z;f,x,c ->call<c,x>)  
adv(z;f,x,c ->z<g,x>)]  
<f,10,k>
```



```
...  
adv(z;f,x,c ->call<c,x>)  
adv(z;f,x,c ->z<g,x>)  
[adv(z;f,x,c ->call<c,x>)]  
<g,10>
```



-Advice:

- proceeds
- alters event
- new event no longer compatible with remaining advice

# Typing

How can a term get stuck?

3.

```
new f:int->int;  
new 10:int;  
new k:int1;  
call<f,10,k>;
```



Bad: call returns  
nothing :-)

# $\mu$ ABC

Idea:

- Type events
- Type advice
- Ensure all types "agree"

Event Types:

Example:

```
_____ new int;          new 5:int;          new f;  
adv(f, x:int -> M);  
call<f,5>
```

<f,5> has type <f, int>

Advice Types:

Example:

adv(f, x:int -> M) also has same type

# Typing

*A note on our running example...*

**Roles:**

**int:** "Integer"  
**int->int:** "Function  
taking an int, returning  
an int"  
**int<sup>-1</sup>:** "Continuation  
(c.f. CPS) of type int"

```
new int : top;  
new int->int : top;  
new int-1:top  
new f:int->int;  
new 10:int;  
new k:int-1;  
adv(z;f,x:int,c: int-1 -> z<f,x,c>)  
call<f,10,k>;
```



# Typing

“Advice proceeds, but with no enqueued advice”

Solution: advice “finality” (=doesn't proceed)

**red** advice is *final*;  
<f,int, int<sup>-1</sup>> has been *finalized*

```
new f:int->int;  
new 10:int;  
new k:int-1;  
adv(z;f,x:int,c: int-1 -> z<f,x,c>)  
call<f,10,k>;
```

i.e., this is bad...

```
new f:int->int;  
new 10:int;  
new k:int-1;  
adv(z;f,x:int,c: int-1 -> z<f,x,c>)  
adv(f,x:int,c: int-1 -> call<c,x>)  
adv(z;f,x:int,c: int-1 -> z<f,x,c>)  
call<f,10,k>;
```

...but this is OK.

# Typing

**red** advice has type  $\langle f, \text{int}, \text{int}^{-1} \rangle$   
(same type as event)

```
new f:int->int;  
new 10:int;  
new k:int-1;  
call<f,10,k>;
```

Also bad: call returns  
nothing :-)

```
new f:int->int;  
new 10:int;  
new k:int-1;  
adv(f,x:int,c: int-1 -> call<c,x>)  
call<f,10,k>;
```

...but this is OK;  
red advice has  
type  $\langle f, x:\text{int}, c: \text{int}^{-1} \rangle$

# Typing

*“Advice proceeds, alters event, new event no longer compatible with remaining advice”*

**Solution**: *Ensure that:*

1. *Events always agree with enqueued advice*
2. *Proceeds always agree with enqueued advice*

```
[adv(z;f,x:int,c: int1 -> M,  
adv(z;g,g,g,g -> N)]  
<g,39>;
```

i.e., this is bad (pointcuts  
not compatible w/ event,  
not compatible w/ each other)

```
[adv(z;g,y:int -> M,  
adv(z;g, x:int -> N)]  
<g,39>;
```

- Solution: Constraint:
1. pointcuts must agree with each other
  2. pointcuts must agree with event.

# Typing

```
[adv(z;f,x:int,c: int1 -> z<3>)  
 <f,39,k>;
```

```
[adv(z;f,x:int,c: int1 -> z<f>)  
 <f,39,k>;
```

i.e., this is bad (proceeds to  
incompatible event)

Solution: If it proceeds, must  
proceed to event of same  
type.

# Typing

```
[adv(z;f,x:int,c: int1 -> call<g>)]  
<f,39,k>;
```

If it doesn't proceed,  
event type can change...

...but it still must be well typed!  
e.g.: bad:

```
[adv(z;f,x: int, c: int1 ->  
  [adv(f -> M)]<g>]  
<f,39,k>;
```

```
[adv(z;f,x:int,c: int1 ->  
  [adv(g -> M)]<g>]  
<f,39,k>;
```

...OK

# Typing

Rules look like this:

As  $\langle Us \rangle$  "ok" if:

1. All advice in  $As$  have same type as  $Us$
2. There is some nonproceeding advice in  $As$
3. All advice in  $As$  is well-typed

$\text{adv}(z; f, x:\text{int}, c:\text{int}^{-1} \rightarrow M)$  well typed if:

1.  $M$  "ok" with  $x:\text{int}, c:\text{int}^{-1}$

$\text{call}\langle Us \rangle$  "ok" if exists some advice of same type as  $Us$ .

# Types

Why distinguish between exact/inexact advice?

Suppose we don't distinguish:

```
new f:int->int; new g:int->int;
```

```
adv( g, x:int, y:int-1 -> M);
```

```
// would have type <int->int, int, int-1>
```

```
// therefore, <int->int, int, int-1> finalized.
```

```
call<f, 40, k>;
```

```
// would have type <int->int, int, int-1>
```

Since  $\langle \text{int} \rightarrow \text{int}, \text{int}, \text{int}^{-1} \rangle$  finalized, and event has same type, this is well-typed!

# Types

Why distinguish between exact/inexact advice?

Thus we make the distinction:

```
new f:int->int; new g:int->int;
```

```
adv( g, x:int, y:int-1 -> M);
```

```
// has type <g, int, int-1>
```

```
call<f, 40, k>;
```

```
// has type <f, int, int-1>
```

<g, int, int<sup>-1</sup>> finalized, <**f**, int, int<sup>-1</sup>> not. Therefore not well typed.



# Types

Why distinguish between exact/inexact advice?

Note: Requires caller, advice to “agree” on “calling protocol”. e.g.: caller must know when to mark roles exact.

Future work: redefine type system to allow for completely oblivious calling convention

Translation: Advised  $\lambda$ -Calculus  $\rightarrow$   $\mu$ ABC

$\lambda$ -Calculus Syntax:

$A ::= \lambda x.M$

$D ::= \text{fun } f=A \mid$   
 $\quad \text{adv}(z.f \rightarrow A)$

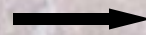
$U, V ::= n \mid \text{unit} \mid A$

$M, N ::= V \mid UV \mid zU \mid D;M \mid \text{let } x=M;N$

Translation: Advised  $\lambda$ -Calculus -  
->  $\mu$ ABC

Example:

```
fun f= $\lambda$ x.x2;  
f(10)
```

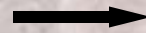


```
fun f= $\lambda$ x.x2;  
102
```

Translation of  $\lambda$ -term  
with continuation  $k$

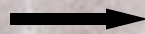
## Translation: Advised $\lambda$ -Calculus - -> $\mu$ ABC

```
fun f= $\lambda x.x^2$ ;  
f(10)
```



```
fun f= $\lambda x.x^2$ ;  
102
```

```
new f;  
adv(f,x,c->call<c,x2>);  
call<f,10,k>
```

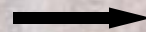


```
new f;  
adv(f,x,c->call<c,x2>);  
[adv(f,x,c->call<c,x2>)]<f,10,k>
```

“Protocol”  $\langle$ function, arg, continuation $\rangle$

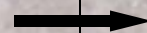
# Translation: Advised $\lambda$ -Calculus - -> $\mu$ ABC

```
fun f= $\lambda x.x^2$ ;  
f(10)
```



```
fun f= $\lambda x.x^2$ ;  
 $10^2$ 
```

```
new f;  
adv(f,x,c->call<c,x^2>);  
[adv(f,x,c->call<c,x^2>)]<f,10,k>
```

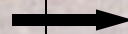


```
new f;  
adv(f,x,c->call<c,x^2>);  
call<k, $10^2$ >
```

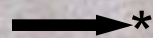
# Translation: Advised $\lambda$ -Calculus - -> $\mu$ ABC

Example with advice:

```
fun f= $\lambda x.x^2$ ;  
adv (z.f ->  $\lambda y.z(y+1)$ );  
f(10)
```



```
fun f= $\lambda x.x^2$ ;  
adv (z.f ->  $\lambda y.z(y+1)$ );  
( $\lambda y. (\lambda x.x^2)(y+1)$ ) 10
```



```
fun f= $\lambda x.x^2$ ;  
adv (z.f ->  $\lambda y.z(y+1)$ );  
(10+1)2
```

*(semantics c.f. Walker  
et.al. (minAML))*

# Translation: Advised $\lambda$ -Calculus - -> $\mu$ ABC

```
fun f= $\lambda x.x^2$ ;  
adv (z.f ->  $\lambda y.z(y+1)$ );  
f(10)
```

```
fun f= $\lambda x.x^2$ ;  
adv (z.f ->  $\lambda y.z(y+1)$ );  
( $\lambda y. (\lambda x.x^2)(y+1)$ ) 10
```

```
new f;  
adv(z.f,x,c -> call<c,x2>);  
adv(z.f,y,c -> z(f,y+1,c) );  
call<f,10,k>;
```

```
new f;  
adv(z.f,x,c -> call<c,x2>);  
adv(z.f,y,c -> z(f,y+1,c) );  
[adv(z.f,x,c -> call<c,x2>);  
adv(z.f,y,c ->  
z<f,y+1,c>)]<f,10,k>;
```

# Translation: Advised $\lambda$ -Calculus - -> $\mu$ ABC

```
fun f= $\lambda x.x^2$ ;  
adv (z.f ->  $\lambda y.z(y+1)$ );  
( $\lambda y.(\lambda x.x^2)(y+1)$ ) 10
```

```
fun f= $\lambda x.x^2$ ;  
adv (z.f ->  $\lambda y.z(y+1)$ );  
( $\lambda x.x^2$ )(10+1)
```

```
new f;  
adv(z.f,x,c -> call<c,x2>);  
adv(z.f,y,c -> z(f,y+1,c) );  
[adv(z.f,x,c -> call<c,x2>);  
adv(z.f,y,c ->  
z<f,y+1,c>)]<f,10,k>;
```

```
new f;  
adv(z.f,x,c -> call<c,x2>);  
adv(z.f,y,c -> z(f,y+1,c) );  
[adv(z.f,x,c -> call<c,x2>);]  
<f,10+1,k>;
```



# Translation: Advised $\lambda$ -Calculus - -> $\mu$ ABC

```
fun f= $\lambda x.x^2$ ;  
adv (z.f ->  $\lambda y.z(y+1)$ );  
( $\lambda x.x^2$ )(10+1)
```

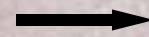
```
fun f= $\lambda x.x^2$ ;  
adv (z.f ->  $\lambda y.z(y+1)$ );  
(10+1)2
```

```
new f;  
adv(z.f,x,c -> call<c,x2>);  
adv(z.f,y,c -> z(f,y+1,c) );  
[adv(z.f,x,c -> call<c,x2>);]  
<f,10+1,k>;
```

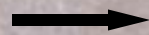
```
new f;  
adv(z.f,x,c -> call<c,x2>);  
adv(z.f,y,c -> z(f,y+1,c) );  
call <k,(10+1)2>;
```

## Translation: Another Example

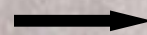
```
fun f= $\lambda x.x^2$ ;  
fun g= $\lambda x.x^3$ ;  
adv(z.f ->  $\lambda y.$ let v=g(y);  
      z(v);)  
f(10)
```



```
fun f= $\lambda x.x^2$ ;  
fun g= $\lambda x.x^3$ ;  
adv(z.f ->  $\lambda y.$ let v=g(y);  
      z(v);)  
( $\lambda y.$ let v=g(y);  
  ( $\lambda x.x^2$ ) v) 10
```



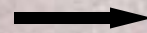
```
fun f= $\lambda x.x^2$ ;  
fun g= $\lambda x.x^3$ ;  
adv(z.f ->  $\lambda y.$ let v=g(y);  
      z(v);)  
let v=g(10);  
  ( $\lambda x.x^2$ ) v
```



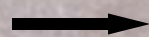
```
fun f= $\lambda x.x^2$ ;  
fun g= $\lambda x.x^3$ ;  
adv(z.f ->  $\lambda y.$ let v=g(y);  
      z(v);)  
let v=( $\lambda x.x^3$ ) 10;  
  ( $\lambda x.x^2$ ) v
```

## Translation: Another Example

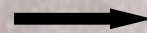
```
fun f= $\lambda x.x^2$ ;  
fun g= $\lambda x.x^3$ ;  
adv(z.f ->  $\lambda y.$ let v=g(y);  
      z(v);)  
let v=( $\lambda x.x^3$ ) 10;  
      ( $\lambda x.x^2$ ) v
```



```
fun f= $\lambda x.x^2$ ;  
fun g= $\lambda x.x^3$ ;  
adv(z.f ->  $\lambda y.$ let v=g(y);  
      z(v);)  
let v= $10^3$ ;  
      ( $\lambda x.x^2$ ) v
```



```
fun f= $\lambda x.x^2$ ;  
fun g= $\lambda x.x^3$ ;  
adv(z.f ->  $\lambda y.$ let v=g(y);  
      z(v);)  
      ( $\lambda x.x^2$ ) ( $10^3$ )
```



```
fun f= $\lambda x.x^2$ ;  
fun g= $\lambda x.x^3$ ;  
adv(z.f ->  $\lambda y.$ let v=g(y);  
      z(v);)  
      ( $10^3$ )2
```

Translation: Advised Object Language -->  
 $\mu\text{ABC}$

Object Language Syntax:

$A ::= \lambda x.M$

$C ::= \text{cls } a:b(l_s = A_s);$

$D, E ::= \text{obj } p:a \mid \text{adv } \{z;a.l \rightarrow A\}$

$M, N ::= v \mid v.l(us) \mid z(us) \mid A(us) \mid D;M \mid$   
 $\text{let } x=M;N$

# Translation: Advised Object Language --> $\mu$ ABC

## Example:

<pre>cls c( l=<math>\lambda</math>x.x<sup>2</sup>); obj o:c; advc(z;c.l-&gt;<math>\lambda</math>y.z(y+1)) o.l(5);</pre>	$\longrightarrow$	<pre>cls c( l=<math>\lambda</math>x.x<sup>2</sup>); obj o:c; advc(z;c.l-&gt;<math>\lambda</math>y.z(y+1)) (<math>\lambda</math>y.<math>\lambda</math>x.x<sup>2</sup>(y+1)) 5</pre>	$\xrightarrow{*}$	<pre>cls c( l=<math>\lambda</math>x.x<sup>2</sup>); obj o:c; advc(z;c.l-&gt;ly.z(y+1)) (5+1)<sup>2</sup></pre>
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# Translation: Advised Object Language --> $\mu$ ABC

```
cls c( l=lx.x^2);  
obj o:c;  
advc(z;c.l-> $\lambda y.z(y+1)$ )  
o.l(5);
```

```
new c; new l;  
adv(self:c, l,x,d-> call<d,x^2>);  
new o:c;  
adv(z; self:c,l,y,d-> z<c,l,y+1,d>;  
call<o,l,5,k>;
```



```
new c; new l;  
adv(self:c, l,x,d-> call<d,x^2>);  
new o:c;  
adv(z; self:c,l,y,d-> z<c,l,y+1,d>;  
[adv(self:c, l,x,d-> call<d,x^2>),  
adv(z; self:c,l,y,d-> z<c,l,y+1,d>)]  
<o,l,5,k>;
```



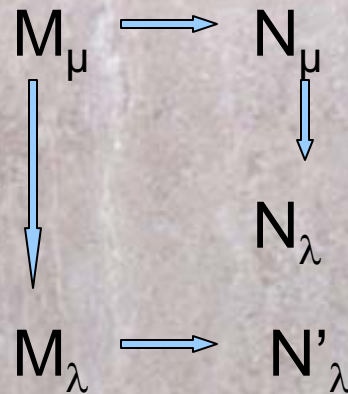
```
new c; new l;  
adv(self:c, l,x,c-> call<c,x^2>);  
new o:c;  
[adv(self:c, l,x,d->  
call<d,x^2>)]
```



```
new c; new l;  
adv(self:c, l,x,c-> call<c,x^2>);  
new o:c;  
call <k,(5+1)^2>
```

# Correctness of Translations

Establish "correctness" by showing translation preserved by evaluation:



Then  $N_\lambda \sim N'_\lambda$

# Correctness of Translations

'~' defined via "structural congruence":

- "in certain cases, order is irrelevant":

```
new f;    new g;  
new g;   ~  new f;
```

- "in certain cases, we can hoist stuff out of advice bodies"

```
adv(f)->{new g; call<x>;} ~ new g;  
...                       adv(f)->{call<x>;}  
...                       ...
```



# Correctness of Traslations

Biggest hurdle: advice lookup

```
fun f= $\lambda x.x$ ;  
adv(z.f- $\lambda y.z(y+1)$ );  
f(3);
```

$\longrightarrow$   $(\lambda y. (\lambda x.x)(y+1))3$

```
new g;  
adv(g,y,c- $\rightarrow$ new h;...);  
call <g,3,k>
```

$\updownarrow$  ~ (!)

```
new f;  
adv(f,x,c- $\rightarrow$ call<c,x>);  
adv(z.f,y,c- $\rightarrow$ z<f,y+1,c>);  
call<f,3,k>
```

$\longrightarrow$

```
...  
[adv(f,x,c- $\rightarrow$ call<c,x>),  
adv(z.f,y,c- $\rightarrow$ z<f,y+1,c>)]  
<f,3,k>
```



## Future work

- Establish semantic equivalence between  $\mu$ ABC terms (e.g., formalize correctness of ' $\sim$ ')
- Redefine  $\lambda$ -semantics
  - "slow down" advice substitution in  $\lambda$  to be more like  $\mu$ ABC semantics

END

