



Alpha-Beta Pruning

General configuration (MIN version)

- We're computing the MIN-VALUE at some node *n*
- We're looping over *n*'s children
- n's estimate of the childrens' min is dropping
- Who cares about n's value? MAX
- Let *a* be the best value that MAX can get at any choice point along the current path from the root
- If n becomes worse than a, MAX will avoid it, so we can stop considering n's other children (it's already bad enough that it won't be played)
- MAX version is symmetric



Alpha-Beta Implementation

α: MAX's best option on path to root β : MIN's best option on path to root

```
\begin{array}{l} \mbox{def max-value(state, $\alpha$, $\beta$):} \\ \mbox{initialize $v$ = -$\pi$} \\ \mbox{for each successor of state:} \\ \mbox{v = max($v$, min-value(successor, $\alpha$, $\beta$))} \\ \mbox{if $v$ \ge $\beta$ return $v$} \end{array}
```

 $\alpha = \max(\alpha, v)$

return v

```
def min-value(state , \alpha, \beta):

initialize v = +\infty

for each successor of state:

v = min(v, max-value(successor, \alpha,

\beta))

if v \leq \alpha return v

\beta = min(\beta, v)

return v
```

Alpha-Beta Pruning Properties

- This pruning has no effect on minimax value computed for the root!
- Values of intermediate nodes might be wrong
 - Important: children of the root may have the wrong value
 - So the most naïve version won't let you do action selection
- Good child ordering improves effectiveness of pruning
- With "perfect ordering":
 - Time complexity drops to O(b^{m/2})
 - Doubles solvable depth!
 - Full search of, e.g. chess, is still hopeless...
- This is a simple example of metareasoning (computing about what to compute)





