Assignment#1; Due January 16 at start of class Review of Formal Languages

Consider some language L. For each of the following cases, write in one of (i) through (vi), to indicate what you can say conclusively about L's complexity, where

- (i) L is definitely regular
- (ii) L is context-free, possibly not regular, but then again it might be regular
- (iii) L is context-free, and definitely not regular
- (iv) L might not even be context-free, but then again it might even be regular
- (v) L is definitely not regular, and it may or may not be context-free
- (vi) L definitely is not even context-free

Follow each answer with example languages A (and B, where appropriate) to back up the complexity claims inherent in your answer; and/or state some known closure property that reflects a bound on the complexity of L.

Example.) $L = A \cup B$, where A and B are both context free, and definitely not regular

L can be characterized by **Property (ii)**, above.

L is context-free, since the class of context-free languages is closed under union.

L can be regular. For example,

$$A = \{ a^n b^m \mid m \ge n \}, B = \{ a^n b^m \mid m \le n \},\$$

 $L = A \cup B = \{ a^n b^m \mid n, m \ge 0 \}$, which is regular since it can be represented by the regular expression a^*b^* .

But L is in general not guaranteed to be regular, e.g., if we just make A and B the same contextfree, non-regular set, then $L = A \cup A = A$, which is not regular.

- **a.**) L = A B, where A is context-free, non-regular and B is regular
- **b.)** L = B A, where A is context-free, non-regular and B is regular
- c.) A = L B, where A is context-free, non-regular and B is regular
- **d.)** $L \subset A$, where **A** is not context-free