

COT6410

Assignment # 6

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Question 01:

Consider the 3SAT instance:

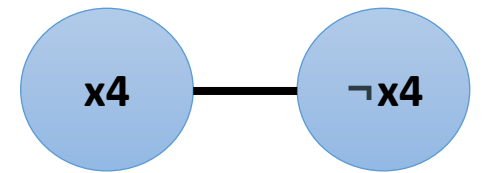
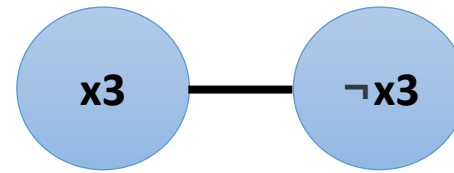
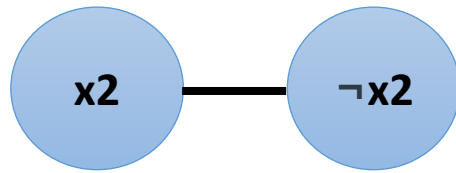
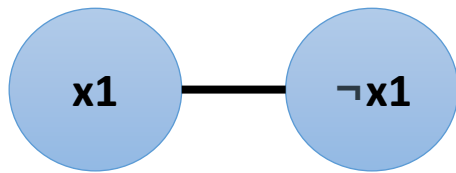
$$\mathbf{E} = (x_1 \vee x_1 \vee x_2) \ \& \ (\neg x_1 \vee \neg x_2 \vee \neg x_4) \ \& \ (\neg x_2 \vee \neg x_3 \vee x_4) \ \& \ (x_2 \vee \neg x_4 \vee \neg x_4)$$

- a. Recast **E** as an instance of k-Vertex Covering and present a solution to the latter
- b. Recast **E** as an instance of 3-Coloring and present a solution to the latter

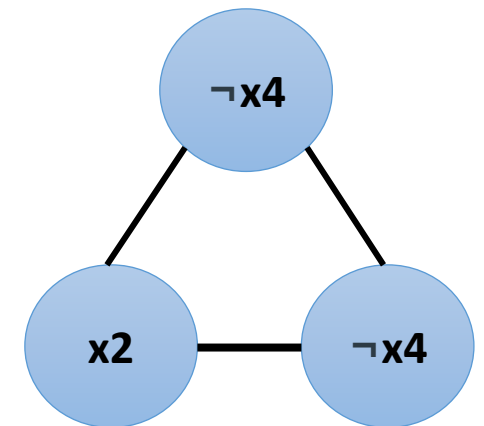
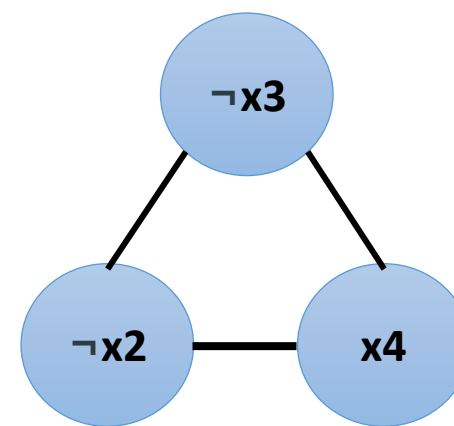
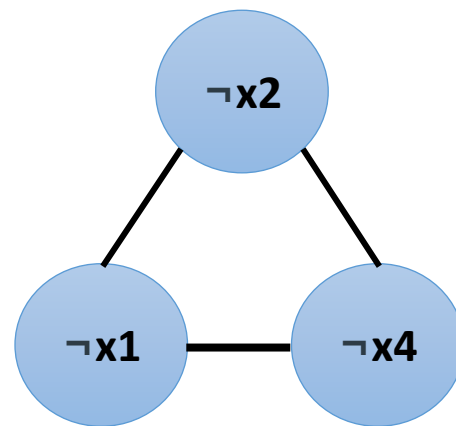
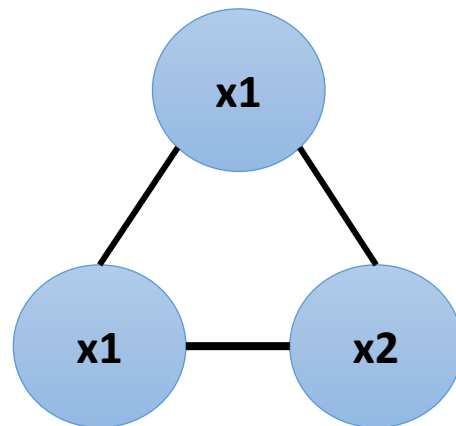
Question 01(a):

$$E = (x1 \vee x1 \vee x2) \& (\neg x1 \vee \neg x2 \vee \neg x4) \& (\neg x2 \vee \neg x3 \vee x4) \& (x2 \vee \neg x4 \vee \neg x4)$$

Variable Gadgets:

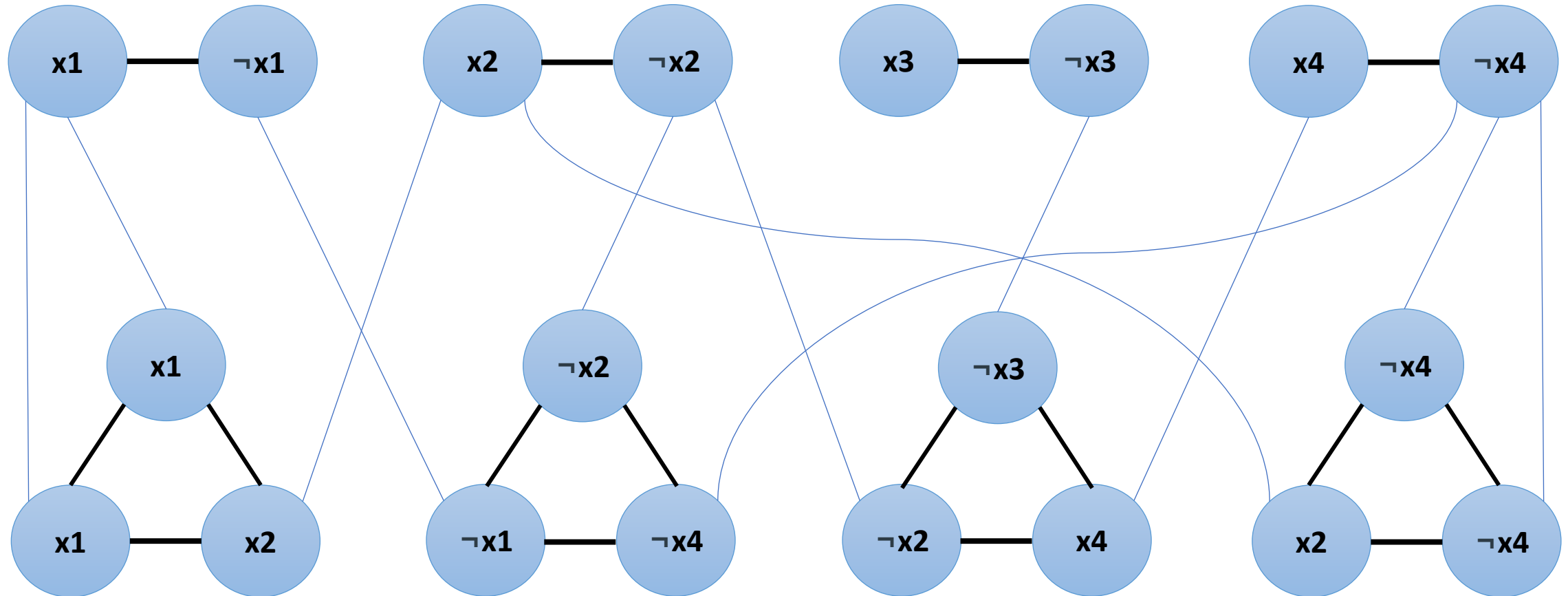


Clause Gadgets:



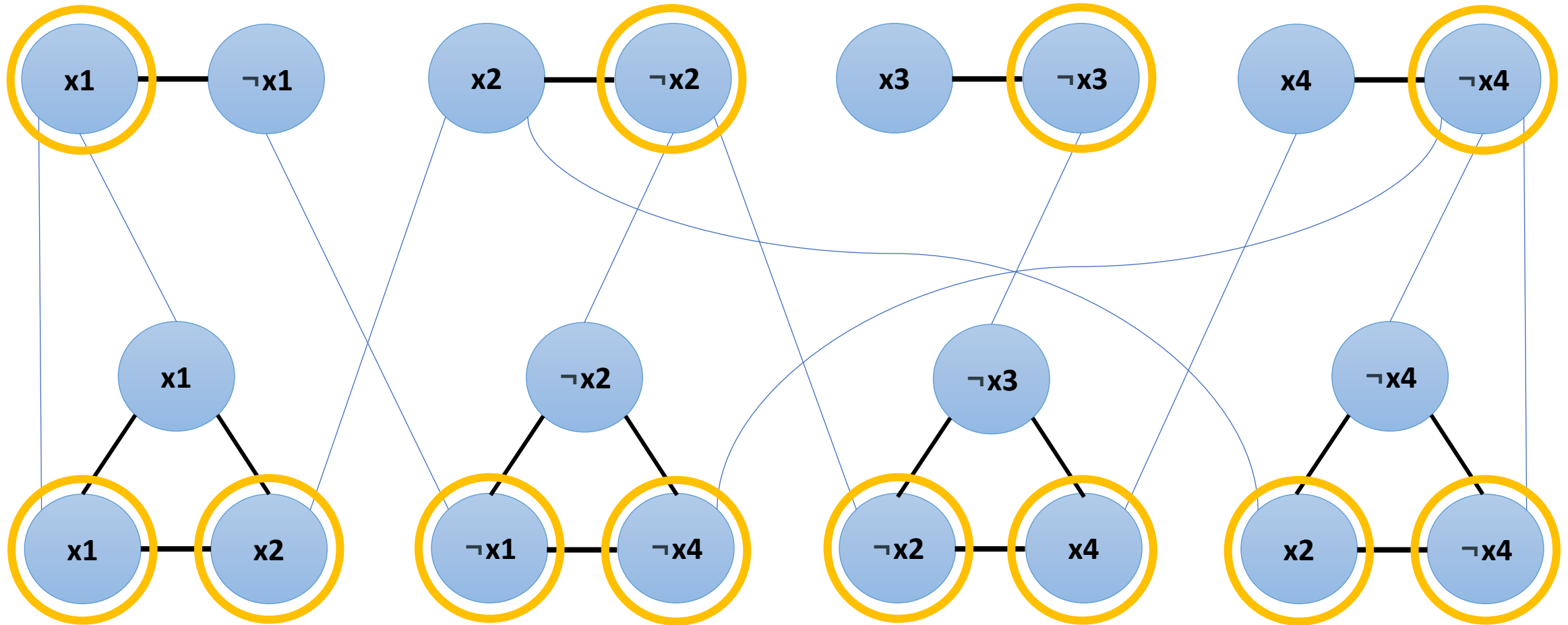
$$E = (x_1 \vee \neg x_1 \vee x_2) \& (\neg x_1 \vee \neg x_2 \vee \neg x_4) \& (\neg x_2 \vee \neg x_3 \vee x_4) \& (x_2 \vee \neg x_4 \vee \neg x_4)$$

Combined Gadgets:



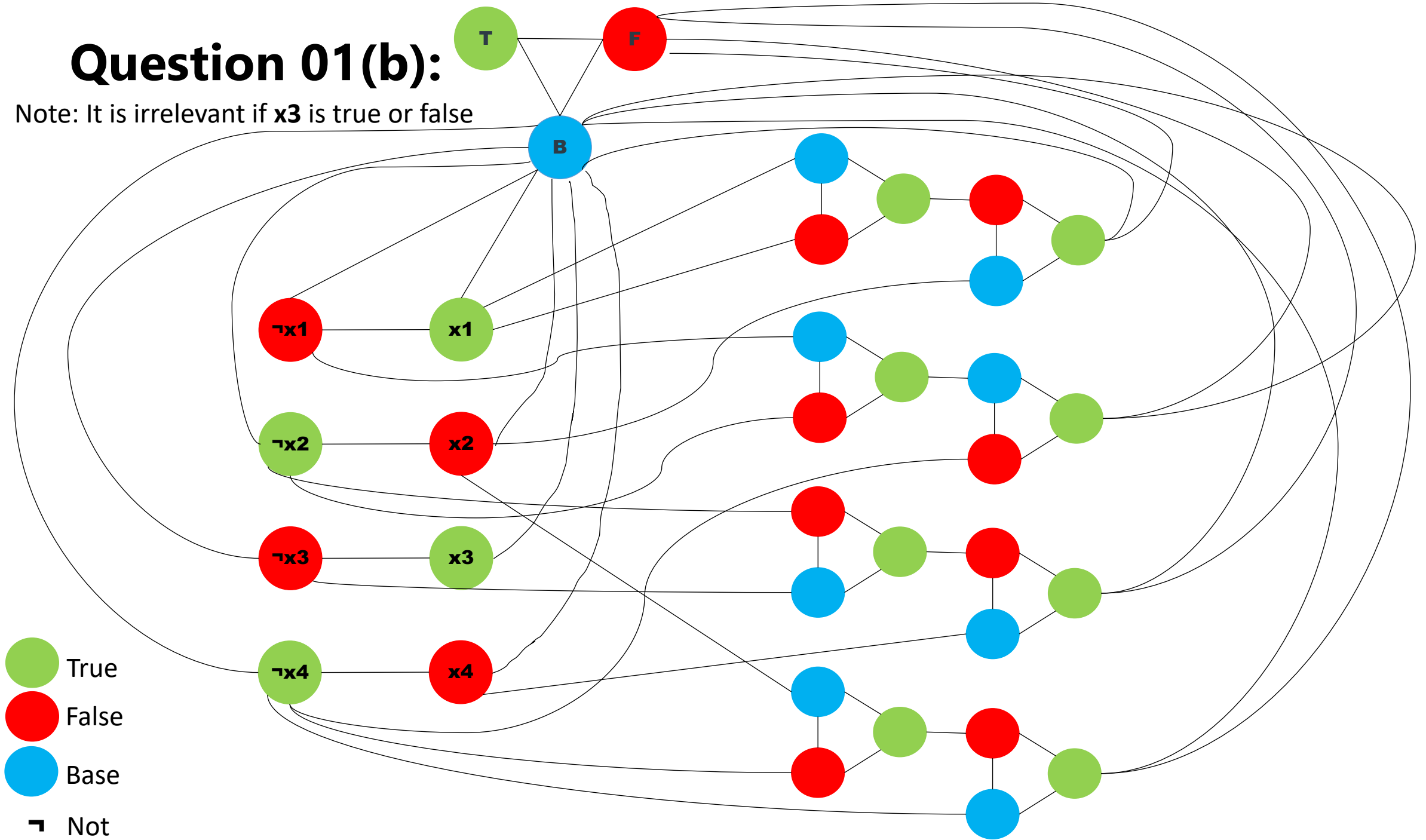
$$E = (x_1 \vee \neg x_1 \vee x_2) \& (\neg x_1 \vee \neg x_2 \vee \neg x_4) \& (\neg x_2 \vee \neg x_3 \vee x_4) \& (x_2 \vee \neg x_4 \vee \neg x_4)$$

Selecting Vertex Cover:



Question 01(b):

Note: It is irrelevant if x_3 is true or false



Question 02:

Consider the task list:

(T1,3), (T2,8), (T3,1), (T4,6), (T5,3), (T6,2), (T7,7)

- a. Fill in the schedules for these tasks under the associated strategies below.
- b. Greedy using a reordering of the list so that longest-running tasks appear earliest in the list (I did the sorting for you):

(T2,8), (T7,7), (T4,6), (T1,3), (T5,3), (T6,2), (T3,1)

Question 02(a):

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
T1	T1	T1	T3	T4	T4	T4	T4	T4	T4	T6	T6						
T2	T2	T2	T2	T2	T2	T2	T2	T5	T5	T5	T7	T7	T7	T7	T7	T7	T7

Question 03:

What if in the above case $(T1,3)$, $(T2,8)$, $(T3,1)$, $(T4,6)$, $(T5,3)$, $(T6,2)$, $(T7,7)$, we had that there is a partial order

$T1 < T3$; $T3 < T4$; $T3 < T7$; $T7 < T5$; $T6 < T2$?

- a. Draw the graph that depicts these relationships.
- b. Show the 2-processor schedule that results when the task number is the priority;
a smaller task number means higher priority.

Question 03(a):

$(T1,3), (T2,8), (T3,1), (T4,6), (T5,3), (T6,2), (T7,7)$
 $T1 < T3; T3 < T4; T3 < T7; T7 < T5; T6 < T2?$

