## **Assignment #8 Sample**

- 1. Use reduction from Halt to show that one cannot decide REPEATS, where REPEATS = { f | for some x and y, x  $\neq$  y,  $\varphi_f(x) \downarrow$ ,  $\varphi_f(y) \downarrow$  and  $\varphi_f(x) == \varphi_f(y)$  }
- 2. Show that REPEATS reduces to Halt. (1 plus 2 show they are equally hard)
- 3. Use Reduction from Total to show that DOUBLES is not even re, where DOUBLES = { f | for all x,  $\phi_f(x) \downarrow$ ,  $\phi_f(x+1) \downarrow$  and  $\phi_f(x+1)=2*\phi_f(x)$  }
- 4. Show DOUBLES reduces to Total. (3 plus 4 show they are equally hard)
- 5. Use Rice's Theorem to show that REPEATS is undecidable
- 6. Use Rice's Theorem to show that DOUBLES is undecidable