

Assignment # 10.1 Key

1. Recast the decision problem for the Boolean expression $(p+q+\sim r)(p+\sim q)r$ as a SubsetSum problem using the construction discussed in class. Indicate what rows would need to be chosen for a solution.

	p	q	r	$p+q+\sim r$	$p+p+\sim q$	$r+r+r$
p	1	0	0	1	1 (or 2)	0
$\sim p$	1	0	0	0	0	0
q	0	1	0	1	0	0
$\sim q$	0	1	0	0	1	0
r	0	0	1	0	0	1 (or 3)
$\sim r$	0	0	1	1	0	0
$C1$	0	0	0	1	0	0
$C1'$	0	0	0	1	0	0
$C2$	0	0	0	0	1	0
$C2'$	0	0	0	0	1 (0 if 2)	0
$C3$	0	0	0	0	0	1 (0 if 3)
$C3'$	0	0	0	0	0	1 (0 if 3)
	1	1	1	3	3	3

Used Red Colored rows for ones chosen

Assignment # 10.2 Key

2. Recast the SubsetSum problem $\{7, 17, 4, 11, 6, 2, 7\}$, $G=36$ as a Partition Problem using the construction discussed in class. Indicate what values would need to be chosen to equal 36. Indicate the partitions that evenly divide the Partition Problem you posed

$$\{7, 17, 4, 11, 6, 2, 7\} \quad 7+17+4+6+2 = 36$$

$$\{15, 7, 12, 4, 11, 6, 4, 12, 3, 2, 72, 90\}$$

$$\text{Can partition as } \{7, 17, 4, 6, 2, 72\} = 108;$$
$$\{11, 7, 90\} = 108$$

Assignment # 10.3 Key

3. Recast the decision problem for the Boolean expression $(p+q+\sim r)(p+\sim q)(r)$ as a 0,1-Integer Linear Programming problem using the construction discussed in class. Indicate what binary (0,1) values of p , q , and r give rise to a solution to the Integer Linear Programming problem you posed.

$$0 \leq p \leq 1; 0 \leq q \leq 1; 0 \leq r \leq 1$$

$$p + q + (1-r) \geq 1$$

$$p + (1-q) \geq 1$$

$$r \geq 1$$

Solution: $p = 1; q = 1; r = 1$ – Lots of other solutions