

## Written Notes from 9/1/2020 COT 3100 Lecture

I mostly went over the .pdf file with the notes on bitwise operators first and explained a few pieces of base conversion typing things below:

$$2 \times 2 \times 2 \times 2 \times 0 = 2 \times (2 \times 2 \times 2 \times 0)$$

Taking any number, dividing 2 and looking at the remainder isolates the last bit of that number (this is how we get the last bit of the binary).

Then, dividing by 2 gets rid of the last bit, so now, we can repeat the process with this new number, until we peel off all the bits.

Now, converting from base b to base 10

$$3ac \text{ in base } 16 = 3 \times 16^2 + 10 \times 16^1 + 12 \times 16^0$$

Now, to convert back from base 10 to base b:

Divide by b and keep track of the remainder, repeat over and over again until the quotient is 0. Then read the remainders in opposite order.

940 in base 10  $\rightarrow$  base 16

$$16 \mid 940$$

$$16 \mid 58 \quad R 12 \text{ (c)}$$

$$16 \mid 3 \quad R 10 \text{ (a)}$$

$$16 \mid 0 \quad R 3 \quad \text{base 16 value is 3ac.}$$

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78 & 63      (bitwise and)
78 in the computer is really 1001110
63           0111111
           -----
           0001110 = 14

```

Bitwise and looks at the bits in the two numbers and puts 1 in the corresponding place if the inputs are both 1s, then we reinterpret the result as a number.

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45 | 27      (bitwise or)
45           = 101101
27           = 011011
           -----
           111111

```

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17 | 39
           010001
           100111
           -----
           110111 = 55

```

45 ^ 27 (bitwise xor)

```

45           = 101101
27           = 011011
           -----
           110110 = 54

```

I typed all of these in IDLE so students could see these operators being used in a programming language (Python)

Proof problem using the rules of inference

$$(\neg p \vee q) \rightarrow r$$

$$r \rightarrow (s \vee t)$$

$$\neg s \wedge \neg u$$

$$\neg u \rightarrow \neg t$$

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$$\therefore p$$

- |                                      |  |
|--------------------------------------|--|
| 1. $\bar{s} \wedge \bar{u}$          | Premise                                    |
| 2. $\bar{u}$                         | Rule of Conjunctive Simplification with #1 |
| 3. $\bar{u} \rightarrow \bar{t}$     | Premise                                    |
| 4. $\bar{t}$                         | Modus Ponens with #2 and #3                |
| 5. $\bar{s}$                         | Rule of Conjunctive Simplification with #1 |
| 6. $\bar{s} \wedge \bar{t}$          | Rule of Conjunction with #4 and #5         |
| 7. $\overline{s \vee t}$             | DeMorgan's Law with #6                     |
| 8. $r \rightarrow (s \vee t)$        | Premise                                    |
| 9. $\bar{r}$                         | Modus Tollens with #7 and #8               |
| 10. $(\bar{p} \vee q) \rightarrow r$ | Premise                                    |
| 11. $\overline{\bar{p} \vee q}$      | Modus Tollens with #9 and #10              |
| 12. $\bar{\bar{p}} \wedge \bar{q}$   | De Morgan's Law with #11                   |
| 13. $\bar{\bar{p}}$                  | Conjunctive Simplification with #12        |
| 14. $p$                              | Double Negation with #13                   |

How can I derive the rules of inference?

(1) Truth Table

(2) Laws of Logic

$$[p \wedge (p \rightarrow q)] \rightarrow q$$

P	q	$p \rightarrow q$	$p \wedge (p \rightarrow q)$	$[p \wedge (p \rightarrow q)] \rightarrow q$
F	F	T	F	T
F	T	T	F	T
T	F	F	F	T
T	T	T	T	T

Use the laws of logic to show that the expression is a tautology, which is a statement that is always true.

$p \rightarrow q$  IS THE SAME AS  $\bar{p} \vee q$

Show that  $[p \wedge (p \rightarrow q)] \rightarrow q$  is a tautology.

$$[p \wedge (p \rightarrow q)] \rightarrow q$$

$$[p \wedge (\bar{p} \vee q)] \rightarrow q$$

Definition of Implication

$$\overline{p \wedge (\bar{p} \vee q)} \vee q$$

Definition of Implication

$$(\bar{p} \vee \overline{\bar{p} \vee q}) \vee q$$

Demorgan's

$$(\bar{p} \vee (\bar{\bar{p}} \wedge \bar{q})) \vee q$$

Demorgan's

$(\bar{p} \vee (p \wedge \bar{q})) \vee q$	Double Negation
$((\bar{p} \vee p) \wedge (\bar{p} \vee \bar{q})) \vee q$	Distributive Law
$(T \wedge (\bar{p} \vee \bar{q})) \vee q$	Inverse Law
$(\bar{p} \vee \bar{q}) \vee q$	Identity Law
$\bar{p} \vee (\bar{q} \vee q)$	Associative Law
$\bar{p} \vee T$	Inverse Law
$T$	Domination law