

Iterator Proof Rules for C#

V2.0

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Outline

- Iterators in C#
- How to specify and verify iterators and foreach loops?
- How to prevent interference between iterators and foreach loops?

The Iterator pattern in C# 2.0

```
public interface IEnumerator<T> {  
    T Current { get; }  
    bool MoveNext();  
}
```

```
public interface IEnumerable<T> {  
    IEnumerator<T> GetEnumerator();  
}
```

Foreach Loops

foreach (T x in C) S

is implemented as

```
IEnumerable<T> c = C;  
IEnumerator<T> e = c.GetEnumerator();  
while (e.MoveNext())  
{ T x = e.Current; S }
```

C# 2.0 Iterator Methods

```
IEnumerable<int> FromTo(int a, int b) {  
    for (int x = a; x < b; x++)  
        yield return x;  
}
```

is implemented as

```
IEnumerable<int> FromTo(int a, int b)  
{ return new FromTo_Enumerable(a, b); }
```

Compiler-generated class

C# 2.0 Iterator Methods

```
class FromTo_Enumerator : IEnumerator<int> {
    int a; int b; int pc; int x; int current;
    public FromTo_Enumerator(int _a, int _b) { a = _a;
        b = _b; }
    public int Current { get { return current; } }
    public bool MoveNext() {
        switch (pc) {
            case 0: x = a; goto case 1;
            case 1: if (!(x < b)) goto case 4;
            case 2: current = x; pc = 3; return true;
            case 3: x++; goto case 1;
            case 4: pc = 4; return false;
        }
    }
}
```

How to specify and verify iterators?

```
static IEnumerable<int> FromTo(int a, int b)
    requires a <= b;
    invariant forall{int i in (0; b - a); values[i] == a + i};
    invariant values.Count <= b - a;
    ensures values.Count == b - a;
```

```
{
```

```
    for (int x = a; x < b; x++)
```

Enumeration invariant must be proved at start of iterator method...

```
        invariant values.Count == x - a;
```

```
        { yield return x; }
```

... and after each yield return statement.

```
}
```

Ensures clause must be proved at end of method (and at yield break statements)

How to specify and verify foreach loops?

```
int sum = 0;
Seq<int> values = new Seq<int>();
while (*)
    invariant sum == Math.Sum(values);
    free invariant forall{int i in (0:values.Count); values[i]==1+i};
    free invariant values.Count <= 3 - 1;
{
    int x; havoc x; values.Add(x);
    assume forall{int i in (0:values.Count); values[i]==1+i};
    assume values.Count <= 3 - 1;
    sum += x;
}
assume values.Count == 3 - 1;
assert sum == 6;
```

Interference

```
List<int> xs = new List<int>();    class List<T> : IEnumerable<T> {  
    xs.Add(1); xs.Add(2);        ArgumentOutOfRangeException !  
    xs.Add(3);  
    int sum = 0;  
    foreach (int x in xs)  
    { sum += x; xs.Remove(0); }  
    //assert sum == 6;  
    I IEnumerator<T>  
    GetEnumerator() {  
        int n = Count;  
        for (int i = 0; i < n; i++)  
            yield return this[i];  
    }  
}
```

Parties execute in an interleaved fashion

But we wish to verify them as if they executed in isolation

Proposed solution:
Prevent either party from seeing the other party's effects

Error: unsatisfied
requires *this.readCount == 0;*

Proposed solution

Enforced using an extension
of the Boogie methodology

```
List<int> xs = new List<int>();  
xs.Add(1); xs.Add(2);  
  xs.Add(3);  
int sum = 0;  
foreach (int x in xs)  
{ sum += x; xs.Remove(0); }  
//assert sum == 6;
```

reads clause declares the set of
pre-existing objects the iterator
method wishes to read

The iterator method
may not read or write
any other pre-existing
objects

```
class List<T> : IEnumerable<T> {  
...  
IEnumerator<T>  
GetEnumerator()  
  reads this; {  
    int n = Count;  
    for (int i = 0; i < n; i++)  
      yield return this[i];  
  }  
}
```

And the foreach
loop body may not
write the objects
in the **reads** clause

The Boogie methodology

- Enforces object invariants
- Uses a dynamic ownership system
- Each object gets two extra fields:
 - **bool inv;**
 - **bool writable;**
- **o.f := x;** requires **o.writable && !o.inv**
- **unpack o;** requires **o.writable && o.inv**
 - Sets **o.inv := false;**
 - Makes owned objects writable
- **pack o;** reverses the effect of **unpack o;**

Adding read-only objects to the Boogie methodology

- Each object gets three special fields:
 - **bool inv;**
 - **bool writable;**
 - **int readCount; // never negative**
- **o.f = x;** requires
o.writable && o.readCount == 0 && !o.inv
- **x = o.f;** requires
o.writable || 0 < o.readCount

Read-only

```
partial class List<T> {
    [Owned] T[] elems;
    T this[int index] {
        get
            requires
                inv &&
                (writable || 0 < readCount);
        { read (this)
            { return elems[index]; }
        }
    }
}
```

read (*o*) S

means

```
assert o.writable || 0 < o.readCount;
assert o.inv;
o.readCount++;
foreach ([Owned] field f of o)
    o.f.readCount++;
S
foreach ([Owned] field f of o)
    o.f.readCount--;
o.readCount--;
for (int i = 0; i < n; i++)
    yield return this[i];
}
```

How is this call verified?

Thank you