



CAP 4453 Robot Vision

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Administrative details

- Allow grader to review your homework:
 - moazam4453@gmail.com
- Homework 1 review
- Any issues with hw3?



Credits

- Some slides comes directly from:
 - Yogesh S Rawat (UCF)
 - Noah Snavely (Cornell)
 - Ioannis (Yannis) Gkioulekas (CMU)
 - Mubarak Shah (UCF)
 - S. Seitz
 - James Tompkin
 - Ulas Bagci
 - L. Lazebnik





Short Review from last class



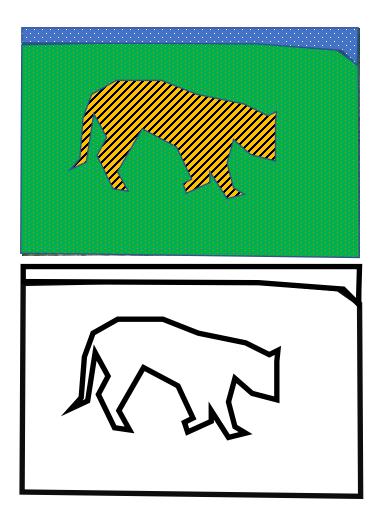
Last 2 classes

- Gradient operators
 - Prewit
 - Sobel
- Marr-Hildreth (Laplacian of Gaussian)
- Canny (Gradient of Gaussian)



Regions - Boundaries









Robot Vision

7. Segmentation I



Outline

- Image segmentation basics
- Thresholding based
 - Binarization
 - Otsu
- Region based
 - Merging
 - Splitting
- Clustering based
 - K-means (SLIC)



Outline

- Image segmentation basics
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- Partition an image into a collection of set of pixels
 - Meaningful regions (coherent objects)
 - Linear structures (line, curve, ...)
 - Shapes (circles, ellipses, ...)





- Content base image retrieval
- Machine vision
- Medical imaging applications
- Object detection (face detection, ..)
- 3D reconstruction
- Object/motion tracking
- •



- In computer vision, image segmentation is one of the oldest and most widely studied problems
 - Early techniques -> region splitting or merging
 - Recent techniques -> Energy minimization, hybrid methods, and deep learning

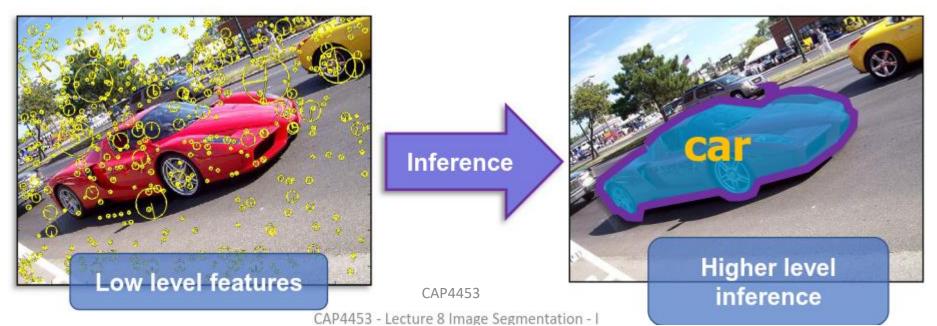
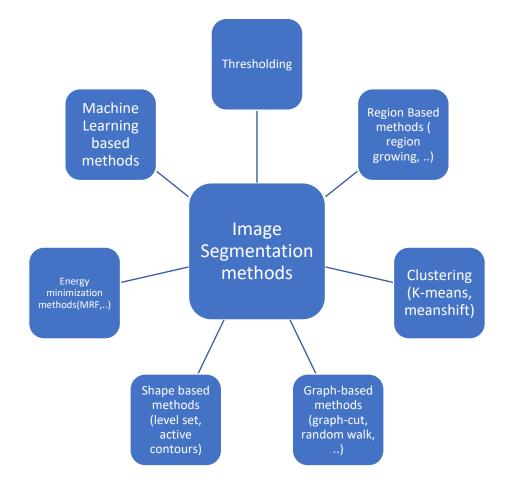


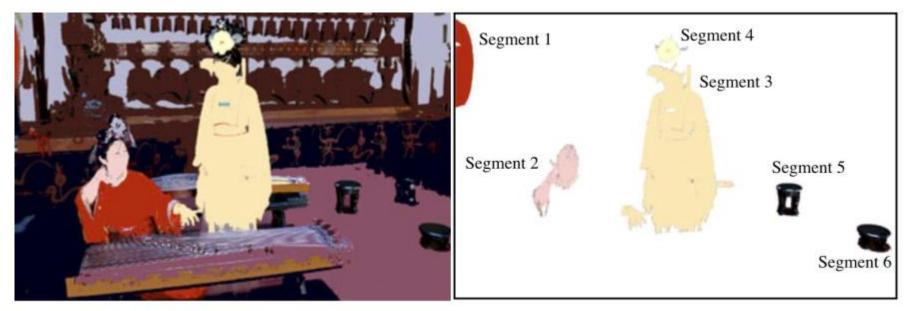


Image segmentation methods



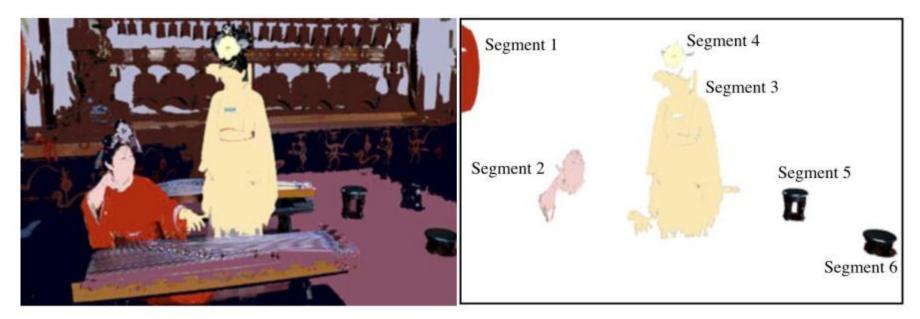


• Image segmentation partitions an image into regions called segments.





• Image segmentation partitions an image into regions called segments.



- Image segmentation creates segments of connected pixels by analyzing some similarity criteria:
 - intensity, color, texture, histogram, features



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 Image binarization applies often just one global threshold T for mapping a scalar image I into a binary image





 Image binarization applies often just one global threshold T for mapping a scalar image I into a binary image

$$J(x,y) = \begin{cases} 0 & \text{if } I(x,y) < T \\ 1 & \text{otherwise.} \end{cases}$$



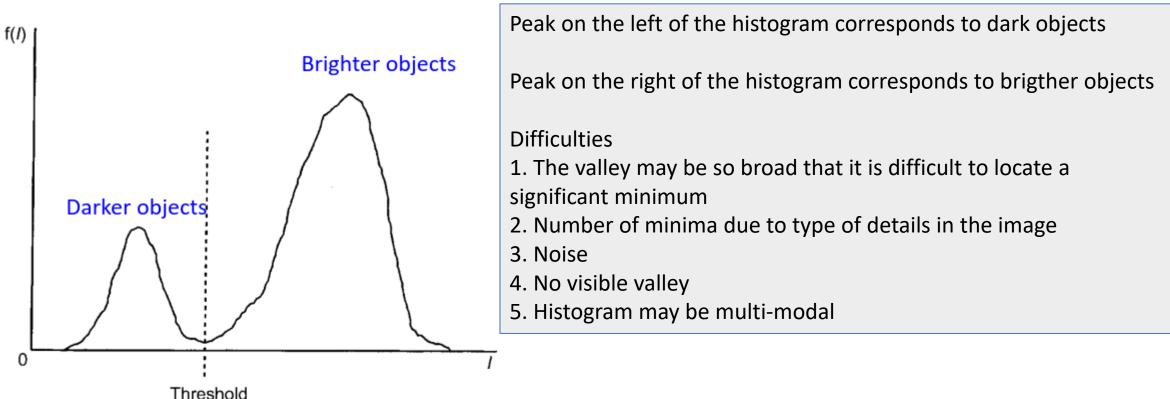
 Image binarization applies often just one global threshold T for mapping a scalar image I into a binary image

$$J(x,y) = \begin{cases} 0 & \text{if } I(x,y) < T \\ 1 & \text{otherwise.} \end{cases}$$

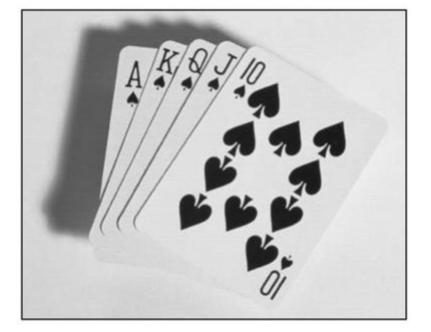
• The global threshold can be identified by an optimization strategy aiming at creating "large" connected regions and at reducing the number of small-sized regions, called artifacts.

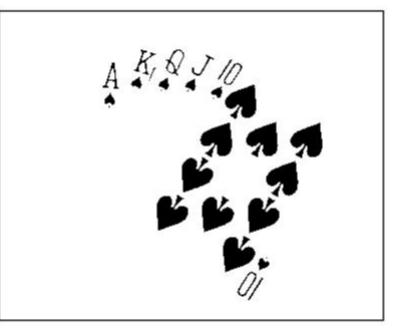


• Thresholding: Most frequently employed method for determining threshold is based on histogram analysis of intensity levels





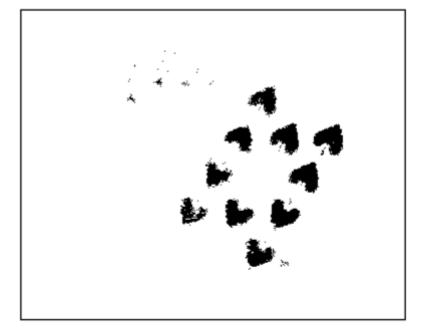


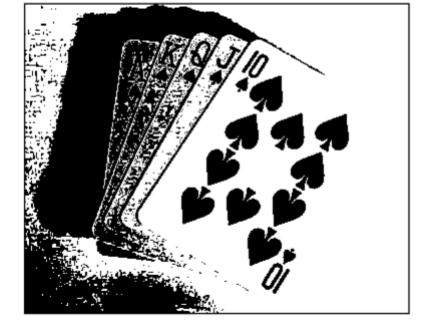


Original Image

Thresholded Image



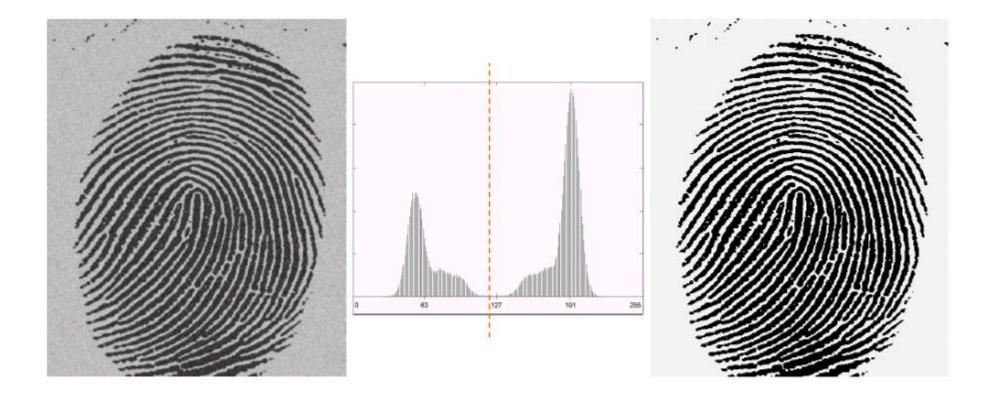




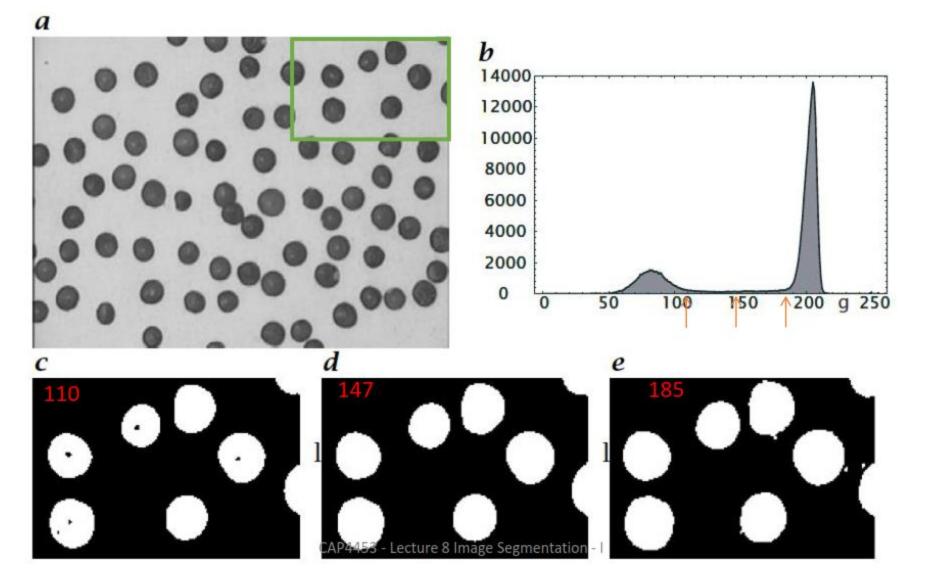
Threshold Too Low

Threshold Too High











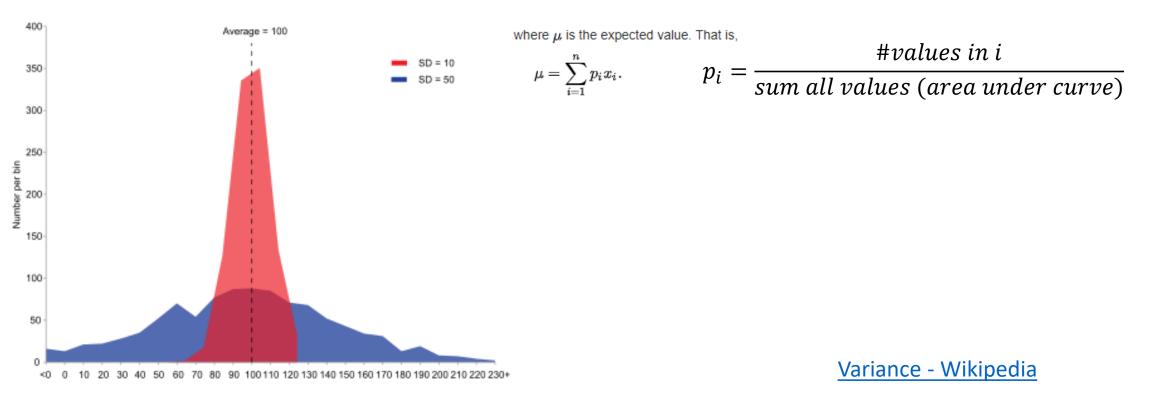
Outline

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Variance

$\operatorname{Var}(X) = \operatorname{E}\left[(X - \mu)^2\right] = \sigma_X^2$



Variance

400

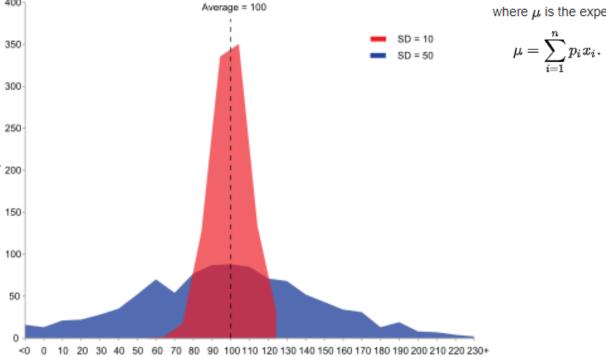
Number per bin

$$\operatorname{Var}(X) = \operatorname{E} \left[(X - \mu)^2 \right] = \sigma_X^2$$

Discrete random variable [edit]

If the generator of random variable X is discrete with probability mass function $x_1 \mapsto p_1, x_2 \mapsto p_2, \ldots, x_n \mapsto p_n$, then $\mathrm{Var}(X) = \sum_{i=1}^n p_i \cdot (x_i - \mu)^2,$

where μ is the expected value. That is,





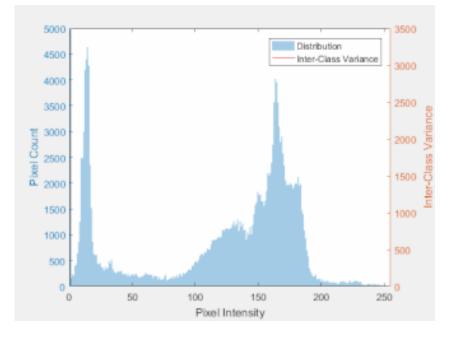


Otsu thresholding

 Definition: The method uses grey-value histogram of the given image I as input and aims at providing the best threshold (foreground/background)

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- Otsu's algorithm selects a threshold that maximizes the betweenclass variance σ_b^2 or minimize within-class variance σ_w^2
- For each threshold t in [0, 255], pixels can be separated into two classes, C1 and C2; those pixels whose Pi < t are put into C1, otherwise into C2
- The possibilities of C1 and C2 separated by t, denoted as W1 and W2, respectively. For example,
 W1 = (#pixels in C1) / (total pixels count).
- Given *H*, *W*1, and *W*2, for each *t*, compute the between-class variance σ_b^2 or within-class variance σ_w^2 ($\sigma_b^2 \rightarrow$ red curve)
- optimal cut t^* corresponds to t whose σ_b^2 is maximum or σ_w^2 is minimum.





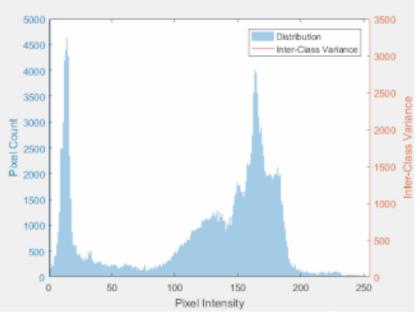
Otsu thresholding

- Definition: The method uses grey-value histogram of the given image I as input and aims at providing the best threshold (foreground/background)
- Otsu's algorithm selects a threshold that maximizes the between class variance σ_b^2

Option 1: maximum of:

$$\sigma_b^2(t) = w_1(t)w_2(t)[\mu_1(t) - \mu_2(t)]^2$$

$$\mu_1(t) = \sum_{i=1}^t \frac{iP(i)}{w_1(t)} \qquad w_1(t) = \sum_{i=1}^t P(i)$$
$$\mu_2(t) = \sum_{i=t+1}^I \frac{iP(i)}{w_2(t)} \qquad w_2(t) = \sum_{i=t+1}^I P(i)$$





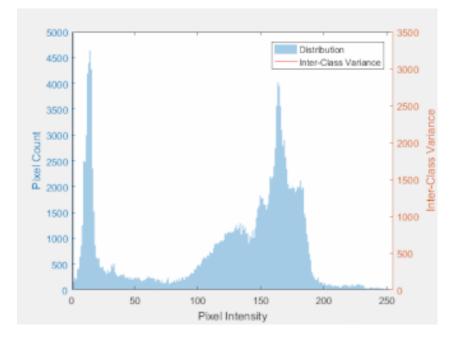
Otsu thresholding

- Definition: The method uses grey-value histogram of the given image I as input and aims at providing the best threshold (foreground/background)
- Otsu's algorithm selects a threshold that maximizes the betweenclass variance σ_w^2 or minimize within-class variance σ_w^2

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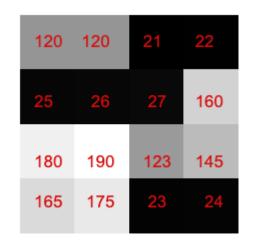
Option 2: minimum of:

 $\sigma_w^2(t) = w_1(t)\sigma_1^2(t) + w_2(t)\sigma_2^2(t)$ $w_1(t) = \sum_{i=1}^t P(i) \qquad P(i) = \frac{n_i}{n}$ $w_2(t) = \sum_{i=t+1}^I P(i)$ $\sigma_1^2(t) = \sum_{i=1}^t [i - \mu_1(t)]^2 \frac{P(i)}{w_1(t)}$ $\sigma_2^2(t) = \sum_{i=t+1}^I [i - \mu_2(t)]^2 \frac{P(i)}{w_2(t)}$



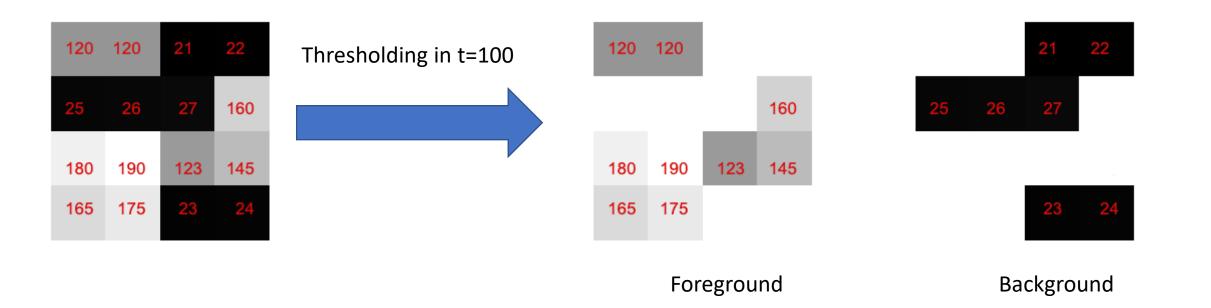


• Find Otsu threshold for this image

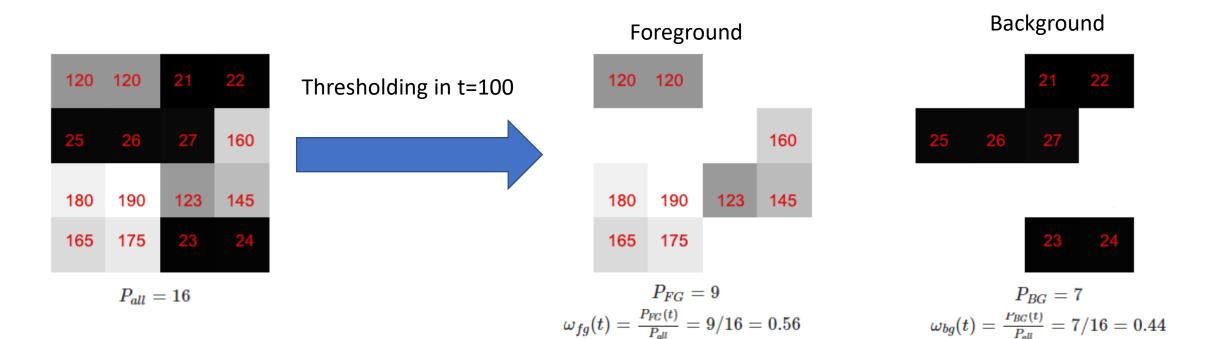


• By minimizing within-class variance



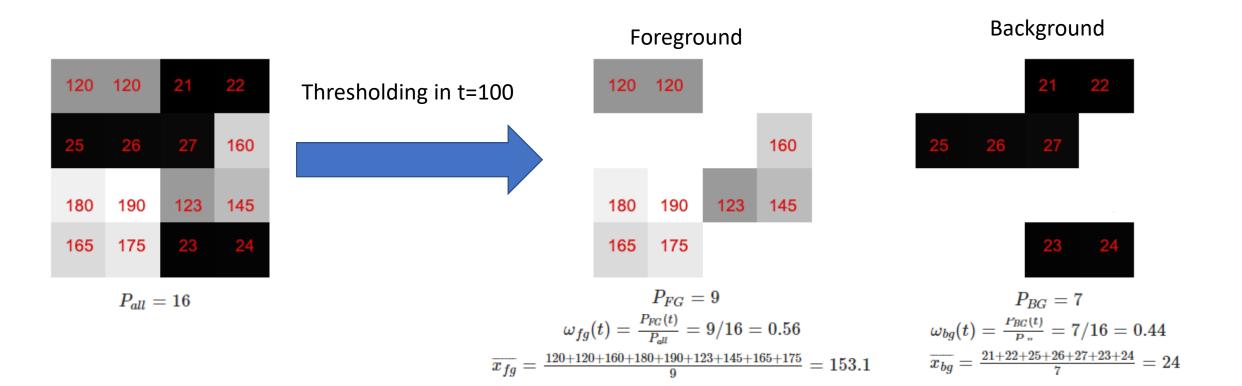






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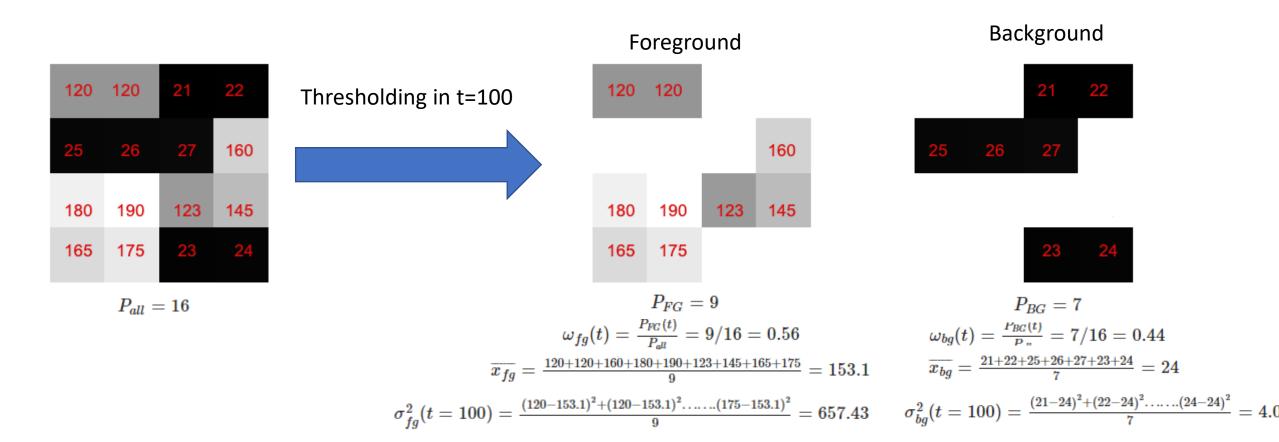




<u>Otsu's method for image thresholding explained and</u> <u>implemented – Muthukrishnan</u>

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<u>Otsu's method for image thresholding explained and</u> <u>implemented – Muthukrishnan</u>

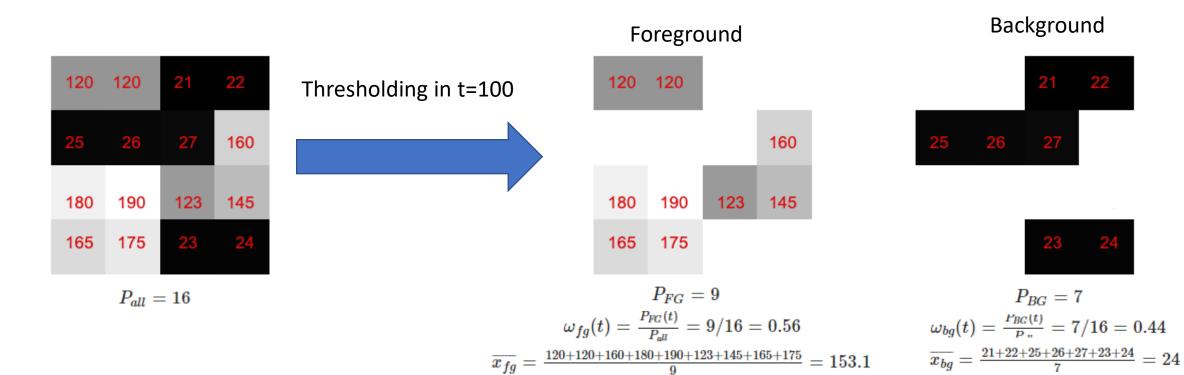
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within-class variance

 $w_1(t)\sigma_1^2(t)$ + $w_2(t)\sigma_2^2(t)$





$$\sigma_{fg}^2(t=100) = \frac{(120-153.1)^2 + (120-153.1)^2 \dots \dots (175-153.1)^2}{9} = 657.43 \qquad \sigma_{bg}^2(t=100) = \frac{(21-24)^2 + (22-24)^2 \dots \dots (24-24)^2}{7} = 4.000$$

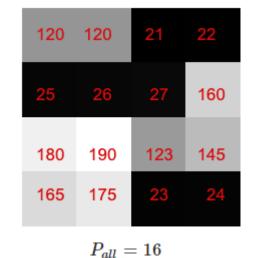
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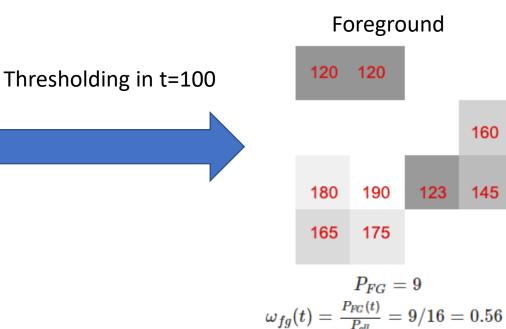
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within-class variance $W_2(t)\sigma_2^2(t)$ $w_1(t)\sigma_1^2(t) +$ 0.44 * 4.0 + 0.56 * 657.43

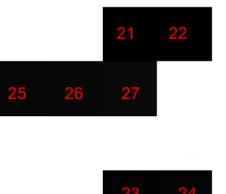


= 369.9208





Background





$$\begin{array}{l} P_{FG} = 9 & P_{BG} = 7 \\ \omega_{fg}(t) = \frac{P_{FC}(t)}{P_{all}} = 9/16 = 0.56 & \omega_{bg}(t) = \frac{P_{BG}(t)}{P_{all}} = 7/16 = 0.44 \\ \overline{x_{fg}} = \frac{120+120+160+180+190+123+145+165+175}{9} = 153.1 & \overline{x_{bg}} = \frac{21+22+25+26+27+23+24}{7} = 24 \\ \sigma_{fg}^2(t = 100) = \frac{(120-153.1)^2+(120-153.1)^2\dots(175-153.1)^2}{9} = 657.43 & \sigma_{bg}^2(t = 100) = \frac{(21-24)^2+(22-24)^2\dots(24-24)^2}{7} = 0.24 \end{array}$$

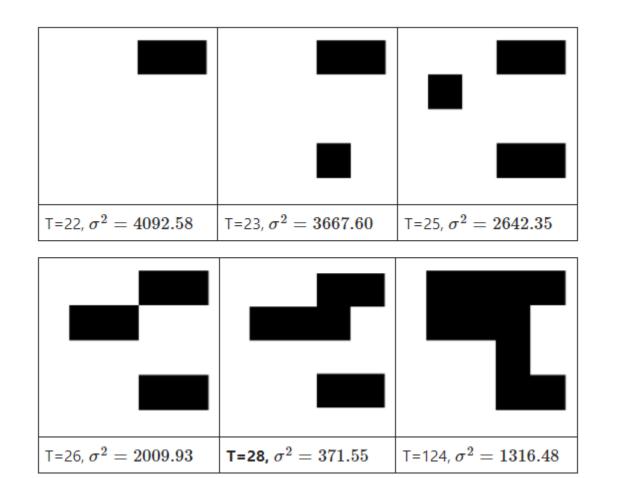
Otsu's method for image thresholding explained and implemented – Muthukrishnan

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 $\overline{x_{fg}} = rac{120+120+160+180+190+123+145+165+175}{9} =$



Step by step (otsu thresholding)



Minimize within-class variance

- The value of variance remains the same from 28 and 120.
- within-class variance is least at t=28 or more precisely between 28 to 120.
- Otsu threshold = 28.

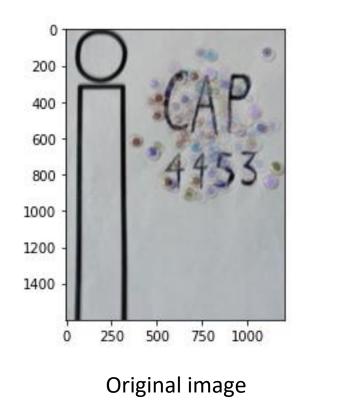


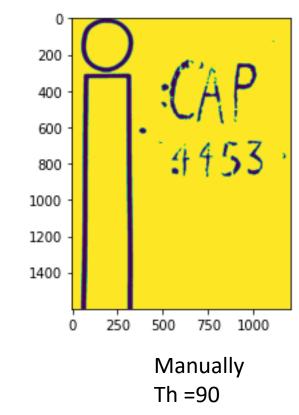
Otsu threshold implementation

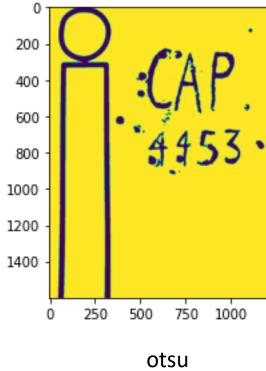
1	# Set total number of bins in the histogram	0 * 🖨	0
2	bins_num = 256	~ ~ •	
3			
4	# Get the image histogram		
- 5	hist, bin_edges = np.histogram(image, bins=bins_num)		
6			
7	# Get normalized histogram if it is required		
8	if is_normalized:		
9	hist = np.divide(hist.ravel(), hist.max())		
10			
11	# Calculate centers of bins		
12	<pre>bin_mids = (bin_edges[:-1] + bin_edges[1:]) / 2.</pre>		
13			
14	# Iterate over all thresholds (indices) and get the probabilities w1	.(t), w2(t)
15	weight1 = np.cumsum(hist)		
16	weight2 = np.cumsum(hist[::-1])[::-1]		
17			
18	# Get the class means mu0(t)		
19	<pre>mean1 = np.cumsum(hist * bin_mids) / weight1</pre>		
20	# Get the class means mu1(t)		
21	<pre>mean2 = (np.cumsum((hist * bin_mids)[::-1]) / weight2[::-1])[::-1]</pre>		
22			
23	<pre>inter_class_variance = weight1[:-1] * weight2[1:] * (mean1[:-1] - me 2</pre>	an2[1:])	**
24	2		
24	<pre># Maximize the inter_class_variance function val</pre>		
26	index_of_max_val = np.argmax(inter_class_variance)		
20	THREY OF HUY AT - Hh at BHAY (THREU CLASS AGUIDANCE)		
28	threshold - bin mids[:_1][index of may yal]		
20	<pre>threshold = bin_mids[:-1][index_of_max_val] print("Otsu's plannithm implementation thresholding pasults "thresholding</pre>	(hold)	
29	print("Otsu's algorithm implementation thresholding result: ", three	notu)	



Otsu threshold implementation







Th =127

Otsu's Thresholding Technique | LearnOpenCV

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Otsu threshold implementation

1 # Applying Otsu's method setting the flag value into cv.THRESH_OTSU. 2 # Use a bimodal image as an input. 3 # Optimal threshold value is determined automatically. 4 otsu_threshold, image_result = cv2.threshold(5 image, 0, 255, cv2.THRESH_BINARY + cv2.THRESH_OTSU, 6) 7 print("Obtained threshold: ", otsu_threshold)

Obtained threshold: 132.0



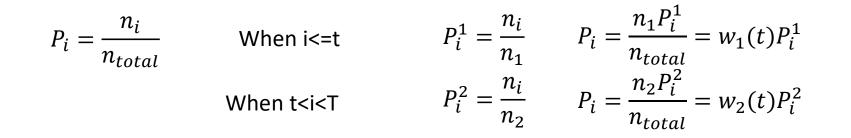
Otsu thresholding example





$$egin{aligned} & \mathrm{Var}(X) = \mathrm{E}ig[(X - \mathrm{E}[X])^2ig] \ &= \mathrm{E}ig[X^2 - 2X\,\mathrm{E}[X] + \mathrm{E}[X]^2ig] \ &= \mathrm{E}ig[X^2ig] - 2\,\mathrm{E}[X]\,\mathrm{E}[X] + \mathrm{E}[X]^2 \ &= \mathrm{E}ig[X^2ig] - \mathrm{E}[X]^2 \end{aligned}$$

 $\sigma_{total}^{2} = E[(X - E[X])^{2}] = E[X_{total}^{2}] - \mu_{total}^{2}$



$$E[X_{total}^{2}] = \sum_{i=1}^{T} P_{i} x_{i}^{2} = \sum_{i=1}^{t} P_{i} x_{i}^{2} + \sum_{i=t+1}^{T} P_{i} x_{i}^{2} = w_{1}(t) \sum_{i=1}^{t} P_{i}^{1} x_{i}^{2} + w_{2}(t) \sum_{i=t+1}^{T} P_{i}^{1} x_{i}^{2} = w_{1}(t) E[X_{1}^{2}] + w_{2}(t) E[X_{2}^{2}]$$
(2)

(1)

 $\mu_{total}^{2} = (w_{1}(t)\mu_{1} + w_{2}(t)\mu_{2})^{2} = w_{1}^{2}\mu_{1}^{2} + 2w_{1}w_{2}\mu_{1}\mu_{2} + w_{2}^{2}\mu_{2}^{2} = w_{1}(1 - w_{2})\mu_{1}^{2} + 2w_{1}w_{2}\mu_{1}\mu_{2} + w_{2}(1 - w_{1})\mu_{2}^{2}$ (3)



The math !

$$egin{aligned} & \mathrm{Var}(X) = \mathrm{E}ig[(X - \mathrm{E}[X])^2ig] \ &= \mathrm{E}ig[X^2 - 2X\,\mathrm{E}[X] + \mathrm{E}[X]^2ig] \ &= \mathrm{E}ig[X^2ig] - 2\,\mathrm{E}[X]\,\mathrm{E}[X] + \mathrm{E}[X]^2 \ &= \mathrm{E}ig[X^2ig] - \mathrm{E}[X]^2 \end{aligned}$$

$$\sigma_{total}^2 = E[(X - E[X])^2] = E[X_{total}^2] - \mu_{total}^2$$
(1)

$$E[X_{total}^{2}] = w_{1}(t)E[X_{1}^{2}] + w_{2}(t)E[X_{2}^{2}]$$
(2)
$$\mu_{total}^{2} = w_{1}(1 - w_{2})\mu_{1}^{2} + 2w_{1}w_{2}\mu_{1}\mu_{2} + w_{2}(1 - w_{1})\mu_{2}^{2}$$
(3)

$$\sigma_{total}^{2} = w_{1}E[X_{1}^{2}] + w_{2}E[X_{2}^{2}] - [w_{1}\mu_{1}^{2} + w_{1}w_{2}\mu_{1}^{2} + 2w_{1}w_{2}\mu_{1}\mu_{2} + w_{2}\mu_{2}^{2} - w_{1}w_{2}\mu_{2}^{2}]$$

$$\sigma_{total}^{2} = w_{1}E[X_{1}^{2}] - w_{1}\mu_{1}^{2} + w_{2}E[X_{2}^{2}] - w_{2}\mu_{2}^{2} + [-w_{1}w_{2}\mu_{1}^{2} - 2w_{1}w_{2}\mu_{1}\mu_{2} + w_{1}w_{2}\mu_{2}^{2}]$$

$$\sigma_{total}^{2} = w_{1}(t)(E[X_{1}^{2}] - \mu_{1}^{2}) + w_{2}(t)(E[X_{2}^{2}] - \mu_{2}^{2}) + w_{1}(t)w_{2}(t)(\mu_{2}^{2} - \mu_{1}^{2})$$
(4)



The math !

$$= E[X^{2} - 2X E[X] + E[X]^{2}]$$

$$= E[X^{2} - 2E[X] E[X] + E[X]^{2}$$

$$= E[X^{2}] - 2E[X] E[X] + E[X]^{2}$$

$$= E[X^{2}] - 2E[X] E[X] + E[X]^{2}$$

$$= E[X^{2}] - E[X]^{2}$$

$$= E[X^{2}] - E[X]^{2}$$

$$(1)$$

$$\sigma_{total}^{2} = w_{1}(t)(E[X_{1}^{2}] - \mu_{1}^{2}) + w_{2}(t)(E[X_{2}^{2}] - \mu_{2}^{2}) + w_{1}(t)w_{2}(t)(\mu_{2}^{2} - \mu_{1}^{2})$$

$$\sigma_{total}^{2} = w_{1}(t)\sigma_{1}^{2}(t) + w_{2}(t)\sigma_{2}^{2}(t) + w_{1}(t)w_{2}(t)(\mu_{2}^{2}(t) - \mu_{1}^{2}(t))$$

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 $\operatorname{Var}(X) = \operatorname{E}ig[(X - \operatorname{E}[X])^2ig]$



Questions?