



# CAP 4453 Robot Vision

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#### Administrative details

#### • Homework 1 doubts

- Should we convert the default BGR images to RGB before displaying them? In part 4 we're instructed to "convert it back to BGR to visualize it," does that mean we should keep all the images as BGR instead of converting to RGB to display them as they were originally?
- For parts 3, 4, and 5, should we be modifying/plotting the red-green swapped image we created in part 2, or using the original image (without those channels swapped)?



# Questions?





# Robot Vision

4. Image Filtering II



#### Credits

- Some slides comes directly from:
  - Yogesh S Rawat (UCF)
  - Noah Snavely (Cornell)
  - Ioannis (Yannis) Gkioulekas (CMU)
  - Mubarak Shah (UCF)
  - S. Seitz
  - James Tompkin
  - Ulas Bagci
  - L. Lazebnik



#### Outline

- Image as a function
- Extracting useful information from Images
  - Histogram
  - Filtering (linear)
  - Smoothing/Removing noise
  - Convolution/Correlation
  - Image Derivatives/Gradient
  - Edges



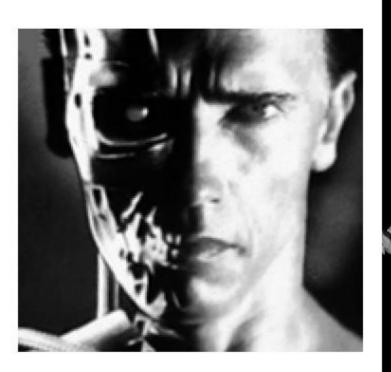
## Edge Detection

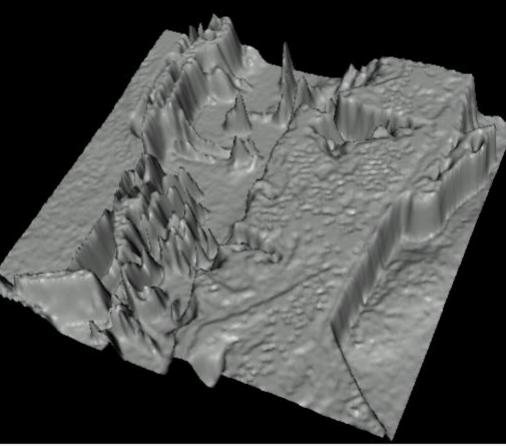
- Identify sudden changes in an image
  - Semantic and shape information
  - Marks the border of an object
  - More compact than pixels



#### Images as functions...





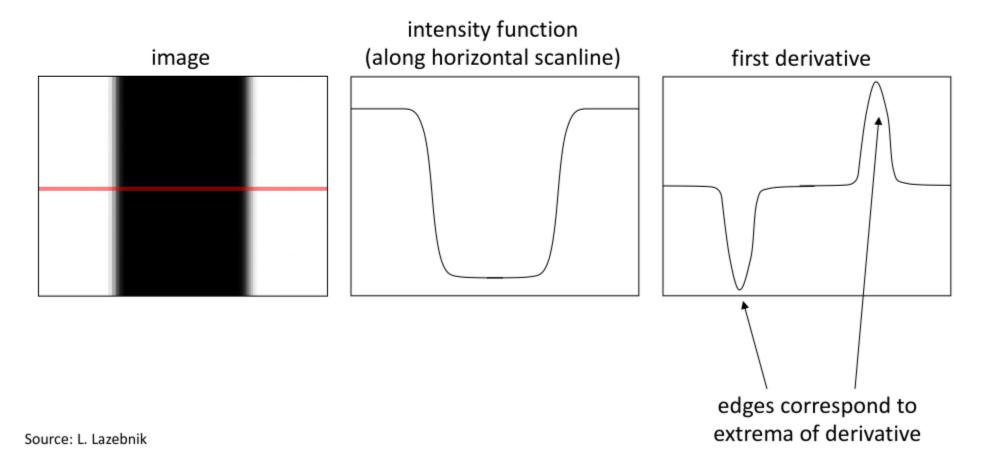


 Edges look like steep cliffs



#### Characterizing edges

• An edge is a place of *rapid change* in the image intensity function



#### Detecting edges



How would you go about detecting edges in an image (i.e., discontinuities in a function)?

✓ You take derivatives: derivatives are large at discontinuities.

How do you differentiate a discrete image (or any other discrete signal)?

#### Detecting edges



How would you go about detecting edges in an image (i.e., discontinuities in a function)?

✓ You take derivatives: derivatives are large at discontinuities.

How do you differentiate a discrete image (or any other discrete signal)?

 $\checkmark$  You use finite differences.

#### Finite differences



High-school reminder: definition of a derivative using forward difference

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

#### Finite differences



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$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

Alternative: use central difference

$$f'(x) = \lim_{h \to 0} \frac{f(x+0.5h) - f(x-0.5h)}{h}$$

For discrete signals: Remove limit and set h = 2

$$f'(x) = \frac{f(x+1) - f(x-1)}{2}$$

What convolution kernel does this correspond to?

#### Finite differences



High-school reminder: definition of a derivative using forward difference

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

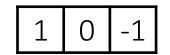
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$$f'(x) = \lim_{h \to 0} \frac{f(x+0.5h) - f(x-0.5h)}{h}$$

For discrete signals: Remove limit and set h = 2

$$f'(x) = \frac{f(x+1) - f(x-1)}{2}$$

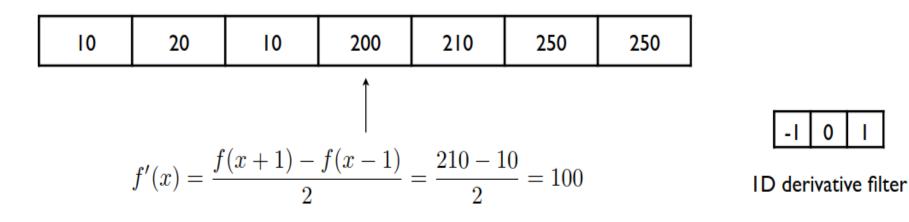
-1	0	1
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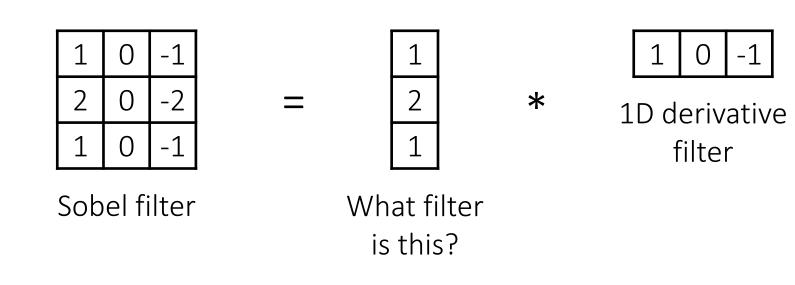


#### Example 1D signal

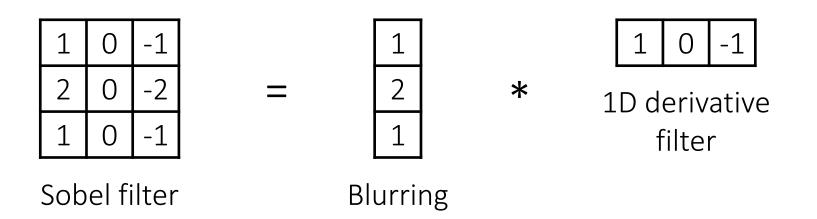
#### How do we compute the derivative of a discrete signal?





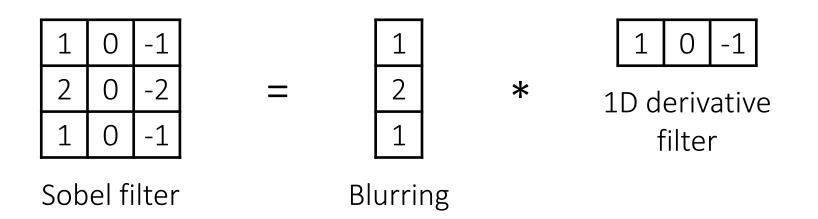






In a 2D image, does this filter responses along horizontal or vertical lines?

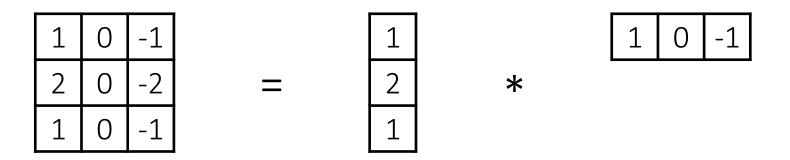




Does this filter return large responses on vertical or horizontal lines?



Horizontal Sober filter:

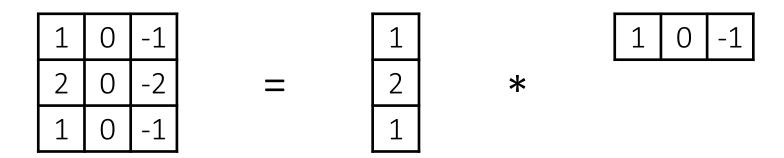


What does the vertical Sobel filter look like?

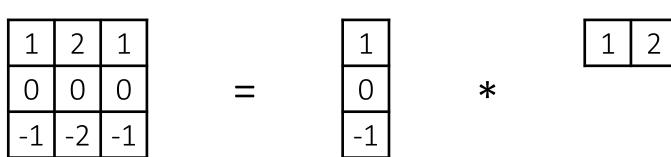


1

Horizontal Sober filter:

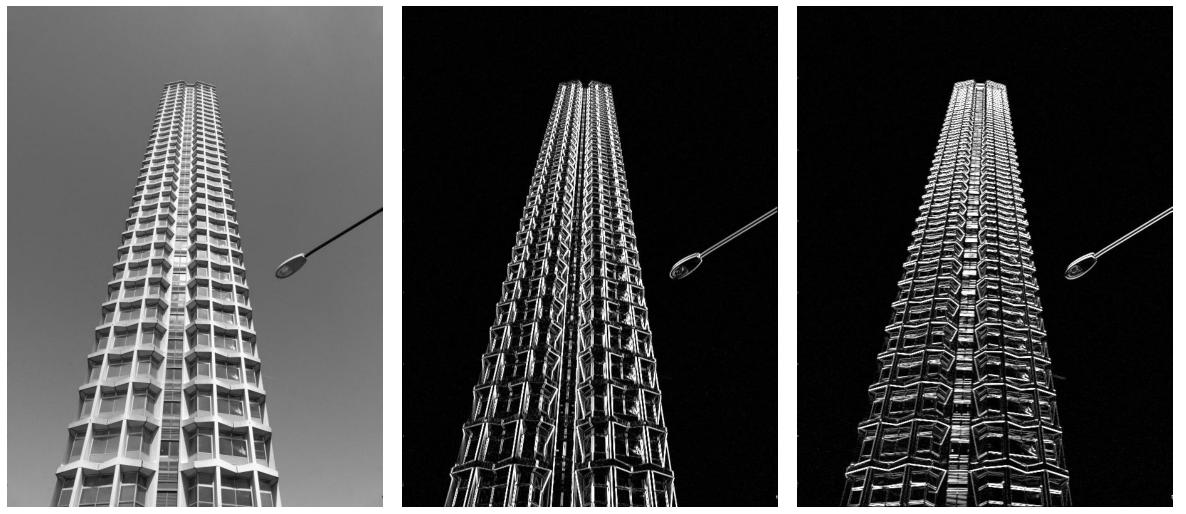


Vertical Sobel filter:



## Sobel filter example





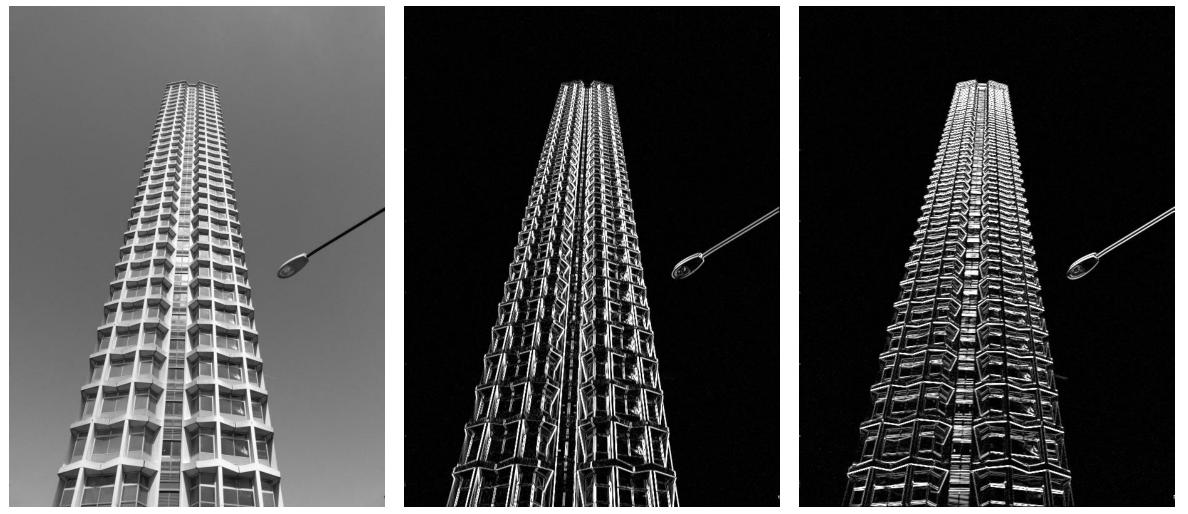
original

which Sobel filter?

which Sobel filter?

## Sobel filter example





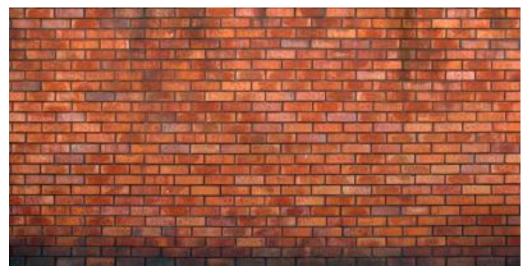
original

horizontal Sobel filter

vertical Sobel filter

#### Sobel filter example





#### original



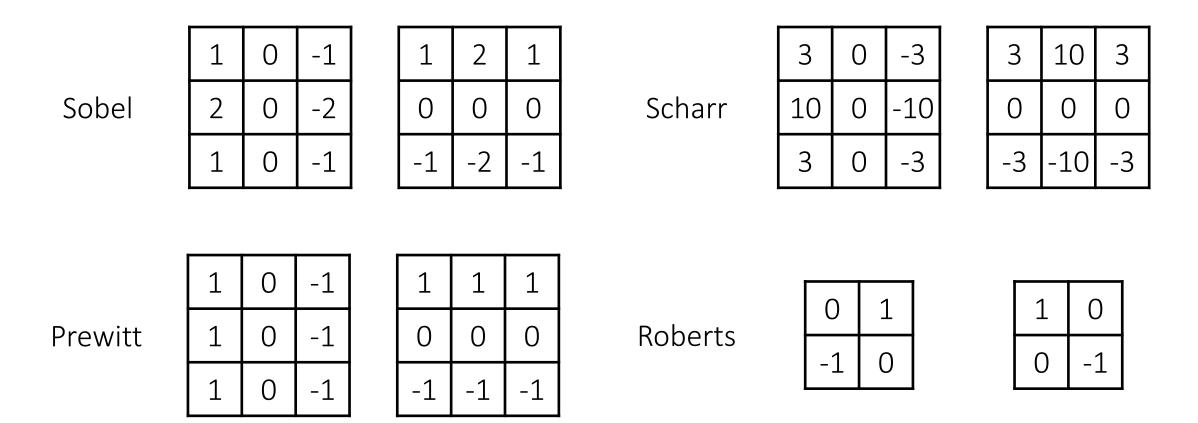
#### horizontal Sobel filter





#### Several derivative filters



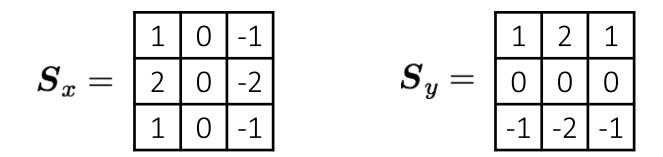


- How are the other filters derived and how do they relate to the Sobel filter?
- How would you derive a derivative filter that is larger than 3x3?



## Computing image gradients

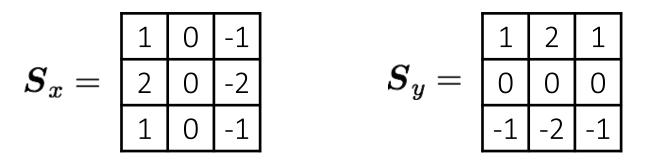
1. Select your favorite derivative filters.





## Computing image gradients

1. Select your favorite derivative filters.



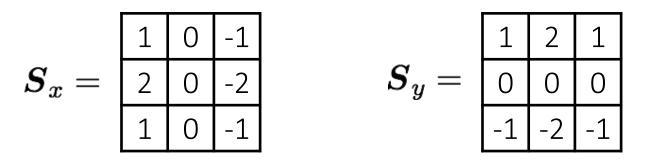
2. Convolve with the image to compute derivatives.

$$rac{\partial f}{\partial x} = S_x \otimes f$$
  $rac{\partial f}{\partial y} = S_y \otimes f$ 



## Computing image gradients

1. Select your favorite derivative filters.



2. Convolve with the image to compute derivatives.

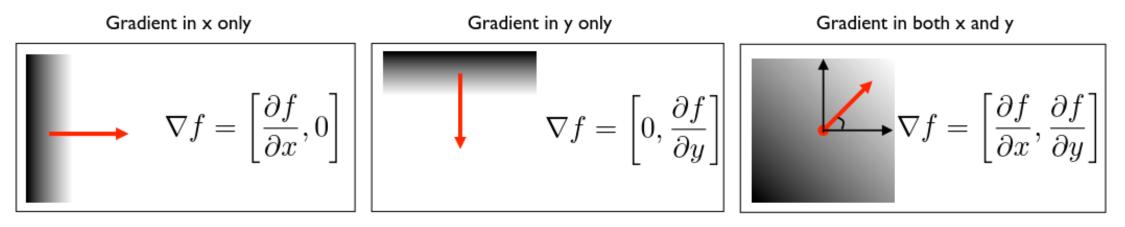
$$rac{\partial \boldsymbol{f}}{\partial x} = \boldsymbol{S}_x \otimes \boldsymbol{f} \qquad \qquad rac{\partial \boldsymbol{f}}{\partial y} = \boldsymbol{S}_y \otimes \boldsymbol{f}$$

3. Form the image gradient, and compute its direction and amplitude.

$$\nabla \boldsymbol{f} = \begin{bmatrix} \frac{\partial \boldsymbol{f}}{\partial x}, \frac{\partial \boldsymbol{f}}{\partial y} \end{bmatrix} \qquad \theta = \tan^{-1} \left( \frac{\partial f}{\partial y} / \frac{\partial f}{\partial x} \right) \qquad ||\nabla f|| = \sqrt{\left( \frac{\partial f}{\partial x} \right)^2 + \left( \frac{\partial f}{\partial y} \right)^2}$$
gradient direction amplitude



Image Gradient



Gradient direction  $\theta = \tan^{-1} \left( \frac{\partial f}{\partial y} / \frac{\partial f}{\partial x} \right)$ 

How does the gradient direction relate to the edge?

#### Gradient magnitude

$$||\nabla f|| = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$$

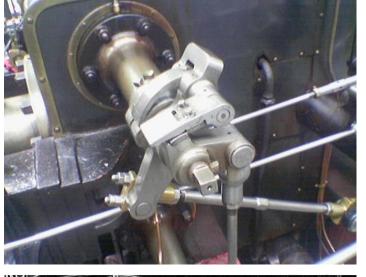
What does a large magnitude look like in the image?

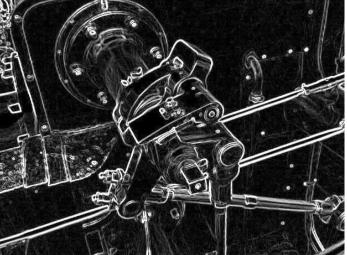
#### Image gradient example





#### gradient amplitude





vertical derivative



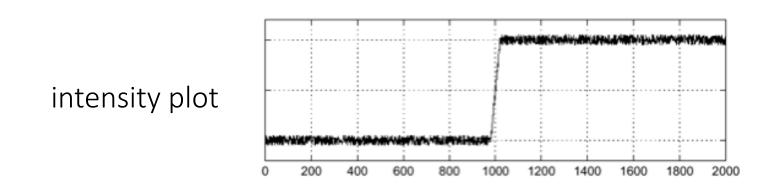
horizontal derivative



How does the gradient direction relate to these edges?

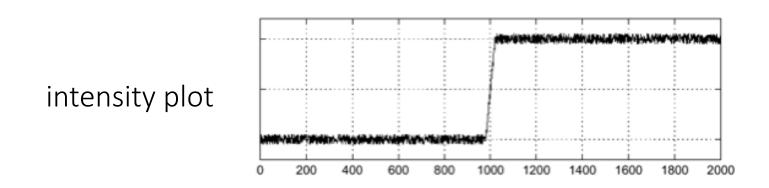


## How do you find the edge of this signal?

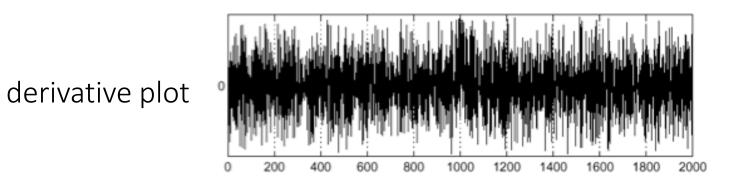




## How do you find the edge of this signal?



Using a derivative filter:

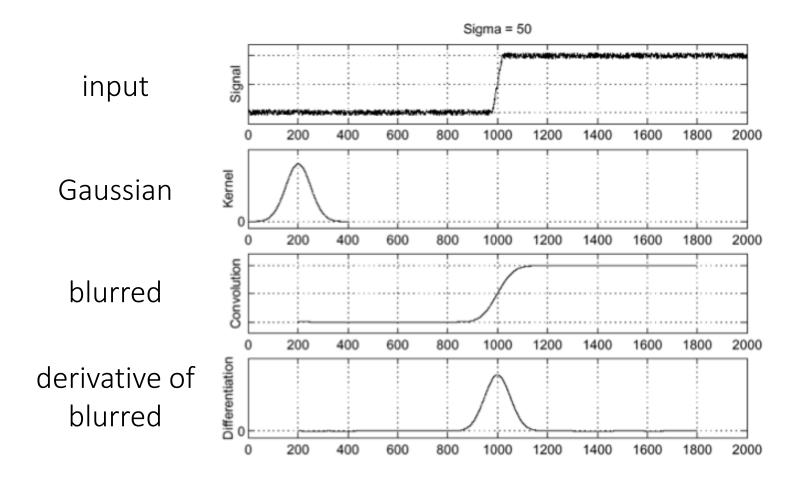


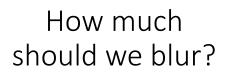
What's the problem here?

#### Differentiation is very sensitive to noise



When using derivative filters, it is critical to blur first!



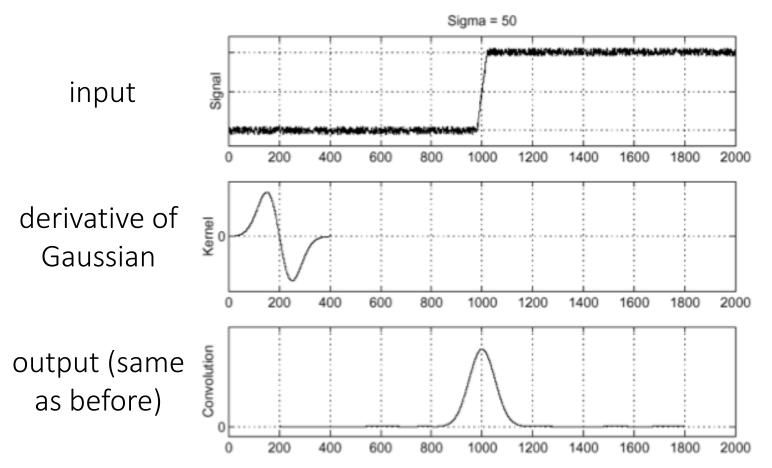




#### Derivative of Gaussian (DoG) filter

Derivative theorem of convolution:

$$\frac{\partial}{\partial x}(h \star f) = (\frac{\partial}{\partial x}h) \star f$$



- How many operations did we save?
- Any other advantages beyond efficiency?



# Laplace filter

#### A.K.A. Laplacian, Laplacian of Gaussian (LoG), Marr filter, Mexican Hat Function



#### Laplace filter



Basically a second derivative filter.

• We can use finite differences to derive it, as with first derivative filter.

first-order  
finite difference 
$$f'(x) = \lim_{h \to 0} \frac{f(x+0.5h) - f(x-0.5h)}{h} \longrightarrow 1D$$
 derivative filter  
 $1 \quad 0 \quad -1$   
second-order  
finite difference  $f''(x) = \lim_{h \to 0} \frac{f(x+h) - 2f(x) + f(x-h)}{h^2} \longrightarrow Laplace filter$ ?

#### Laplace filter



Basically a second derivative filter.

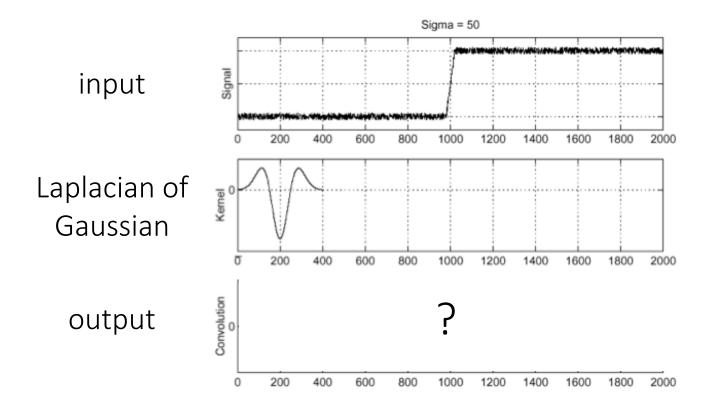
• We can use finite differences to derive it, as with first derivative filter.

first-order  
finite difference 
$$f'(x) = \lim_{h \to 0} \frac{f(x+0.5h) - f(x-0.5h)}{h} \longrightarrow 1D$$
 derivative filter  
 $1 \quad 0 \quad -1$   
second-order  
finite difference  $f''(x) = \lim_{h \to 0} \frac{f(x+h) - 2f(x) + f(x-h)}{h^2} \longrightarrow 1D$  derivative filter  
 $1 \quad 0 \quad -1$ 

## Laplacian of Gaussian (LoG) filter



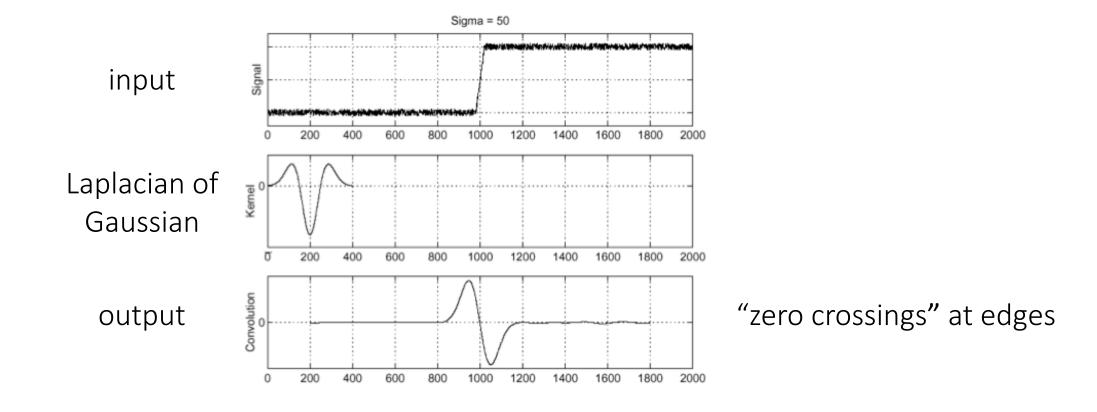
As with derivative, we can combine Laplace filtering with Gaussian filtering



## Laplacian of Gaussian (LoG) filter



As with derivative, we can combine Laplace filtering with Gaussian filtering



#### Laplace and LoG filtering examples

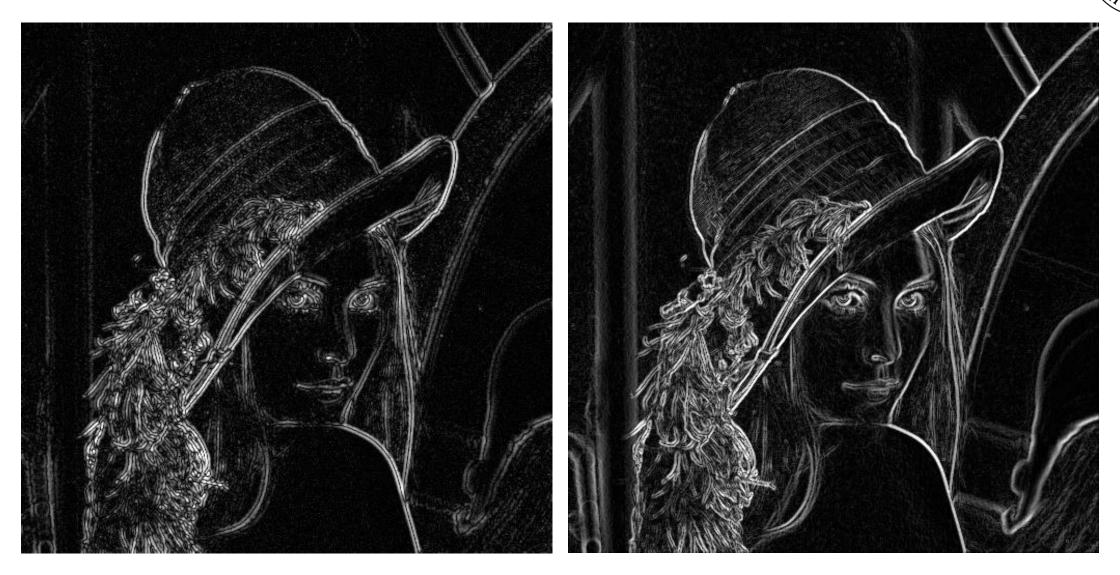




#### Laplacian of Gaussian filtering

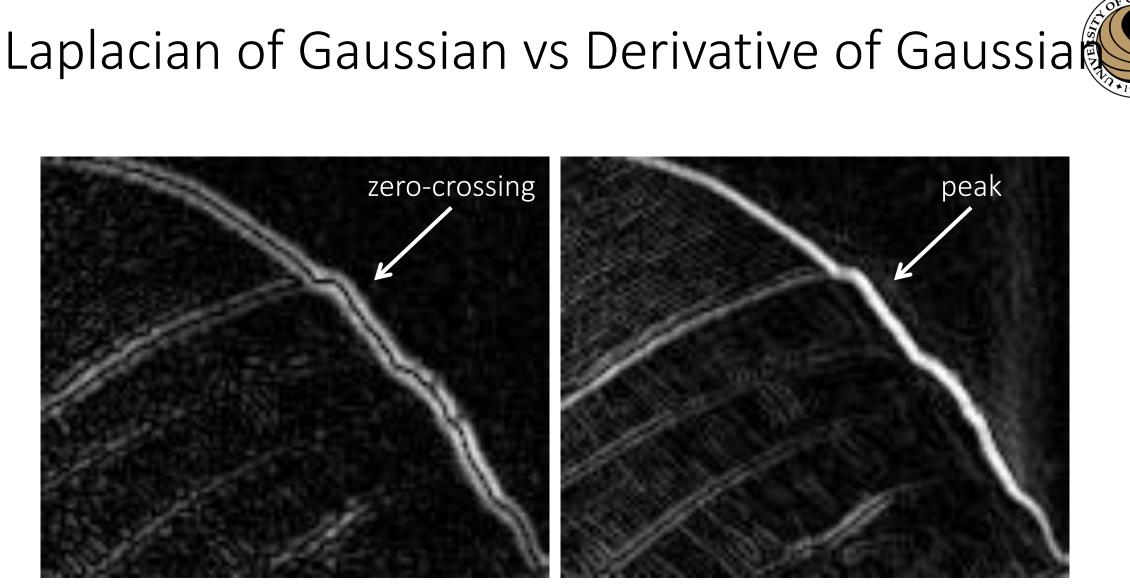
Laplace filtering

## Laplacian of Gaussian vs Derivative of Gaussia



#### Laplacian of Gaussian filtering

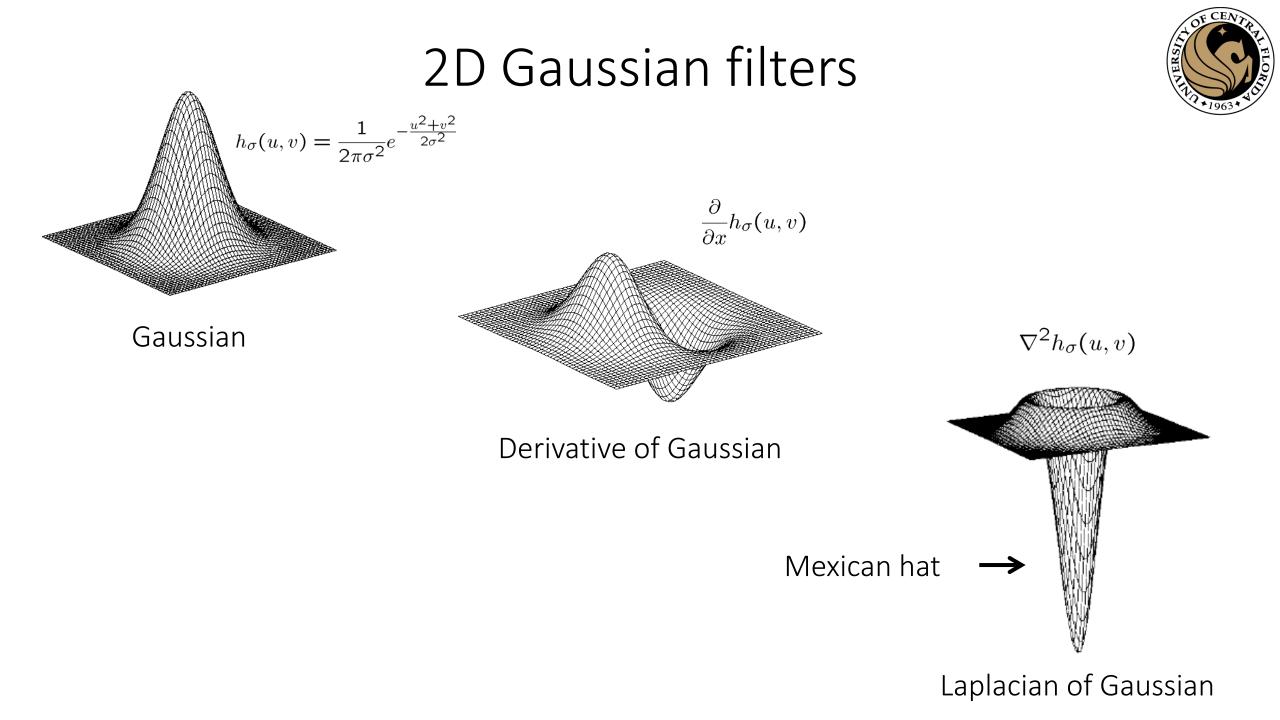
Derivative of Gaussian filtering



Laplacian of Gaussian filtering

Derivative of Gaussian filtering

Zero crossings are more accurate at localizing edges (but not very convenient).



#### References



Basic reading:

• Szeliski textbook, Section 3.2



# Questions?