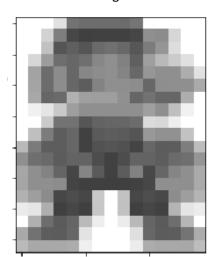
## Homework 2

## CAP 4453

## Spring 2022

1. Considers the image below. What is the dimension of the matrix that represents the image? [10%]



[255 255 255 225 115 109 109 109 108 117 254 255 254 255 255]															
į	[255	255	255	225	115	109	109	109	108	117	254	255	254	255	255]
	[255	255	210	126	71	64	65	65	65	70	143	140	214	255	255]
	[255	255	193	85	95	85	106	112	104	87	124	149	221	255	255]
	[255	215	156	110	103	111	135	143	129	95	159	185	203	224	255]
	[255	163	108	140	103	135	141	143	132	104	150	143	143	173	225]
	[255	164	108	141	103	93	131	143	143	141	103	142	143	143	170]
	[255	168	102	106	177	159	158	158	144	102	114	102	102	174	255]
	[255	240	229	201	158	143	143	143	143	143	159	143	191	241	255]
	[255	255	202	115	114	86	99	102	102	108	219	216	239	255	255]
	[255	191	124	93	103	65	90	93	91	85	152	145	145	194	255]
	[185	123	93	93	103	65	82	85	81	68	103	92	93	126	189]
	[143	111	106	92	99	99	77	65	77	100	99	93	107	111	149]
	[166	143	131	101	70	133	90	65	92	130	72	102	133	143	170]
	[165	143	143	140	68	64	64	63	64	65	71	143	143	143	170]
	[177	158	139	71	77	71	200	254	194	71	78	72	141	158	180]
	[235	229	174	64	71	64	199	255	193	64	71	65	180	229	236]
	[255	176	109	91	101	186	238	255	236	184	101	91	110	182	255]
	[169	114	93	92	103	227	255	255	255	223	103	92	93	116	172]
	[186	168	168	169	172	239	255	255	255	236	172	168	169	168	189]
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- 2. If we filter using a 3x3 kernel and do not perform padding on the borders (convolution in the regions where filter and image are fully intersected), what will be the dimension of the previous image after filtering? [10%]
- 3. What will be the output dimension if the kernel is 5x5 (convolution in the regions where filter and image are fully intersected)? [10%]
- 4. Assuming the dimensions of the image are M x N . can you come out with a general formula that tells you the dimension of the image after filtering if only consider 'valid' regions (where filter and image fully intersect)? [10%]
- 5. Compute the output of applying the filter  $\begin{pmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \end{pmatrix}$  on the first 5 valid columns of row 2 of  $\begin{pmatrix} -1 & -2 & -1 \\ \end{pmatrix}$  "mario" (row 2 is the one that start with values 255 255 210 ..). Show your computations and write the obtained output. [10%]

## Kernel estimation

$$G(x)=\frac{1}{\sqrt{2\pi}\sigma}e^{-\frac{x^2}{2\sigma^2}}$$
 to find coefficients of a kernel of size 7 when  $\sigma$ =1.4. Hint: x is evaluated in interval [ -3 -2 -1 0 1 2 3] [10%]

- 7. The size of a gaussian kernel is usually chosen to have values in the order of 2 or 3 sigmas, since after that the values of the function are almost zero. In the extreme parts of this kernel (when x is either -3 or 3) how many sigmas it corresponds to? Is the chosen size of 7 a good value? [10%]
- 8. Approximate the obtained kernel as a fraction of integer numbers. Hint: use 64 as the denominator. [10%]
- 9. Compute a 7x7 Gaussian kernel using the 1D estimated kernel you estimated in the previous exercise. Remember, this is a separable filter and can be obtained using matrix multiplication. [10%]

$$G = K_{7x1} * K_{1x7}$$

10. In class we build a sharpen filter as the sum of original filter + detail. The detail part was built with the original function and a box filter. Create a new kernel for sharpening but this time uses a gaussian filter. [10%]