

# Matlab Tutorial.

## Session 2.

### SIFT



Gonzalo Vaca-Castano

# Sift purpose

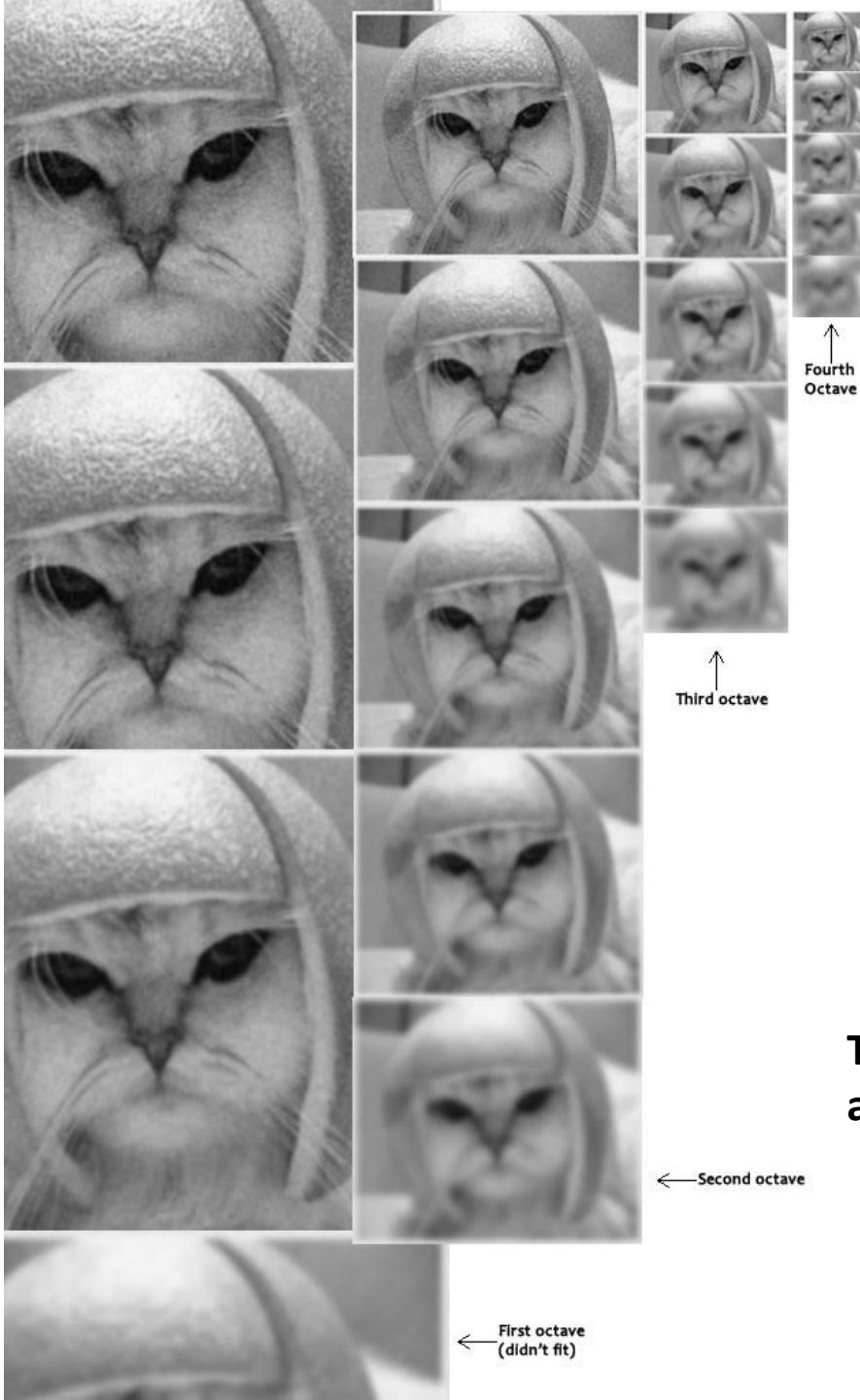
- Find and describe interest points invariants to:
  - Scale
  - Rotation
  - Illumination
  - Viewpoint

# Do it Yourself

- Constructing a scale space
- LoG Approximation
- Finding keypoints
- Get rid of bad key points (A technique similar to the Harris Corner Detector)
- Assigning an orientation to the keypoints
- Generate SIFT features

\*<http://www.aishack.in/2010/05/sift-scale-invariant-feature-transform/2/>

# Construction of a scale space



SIFT takes scale spaces to the next level. You take the original image, and generate progressively blurred out images. Then, you resize the original image to half size. And you generate blurred out images again. And you keep repeating.

**The creator of SIFT suggests that 4 octaves and 5 blur levels are ideal for the algorithm**

# Construction of a scale space (details)

- The first octave

- If the original image is doubled in size and antialiased a bit (by blurring it) then the algorithm produces more four times more keypoints. The more the keypoints, the better!

- Blurring

$$L(x, y, \sigma) = G(x, y, \sigma) * I(x, y)$$

$$G(x, y, \sigma) = \frac{1}{2\pi\sigma^2} e^{-(x^2+y^2)/2\sigma^2}$$

- Amount of Blurring

|        |          | scale →  |           |           |           |
|--------|----------|----------|-----------|-----------|-----------|
|        |          |          | 0.707107  | 1.414214  | 2.828427  |
| Octave | 0.707107 | 1.000000 | 1.414214  | 2.828427  | 5.656854  |
|        | 1.414214 | 2.000000 | 2.828427  | 4.000000  | 8.000000  |
|        | 2.828427 | 4.000000 | 5.656854  | 8.000000  | 11.313708 |
|        | 5.656854 | 8.000000 | 11.313708 | 16.000000 | 22.627417 |

# The Convolution of Two Gaussian Distributions

- <http://tina.wiau.man.ac.uk/docs/memos/2003-003.pdf>

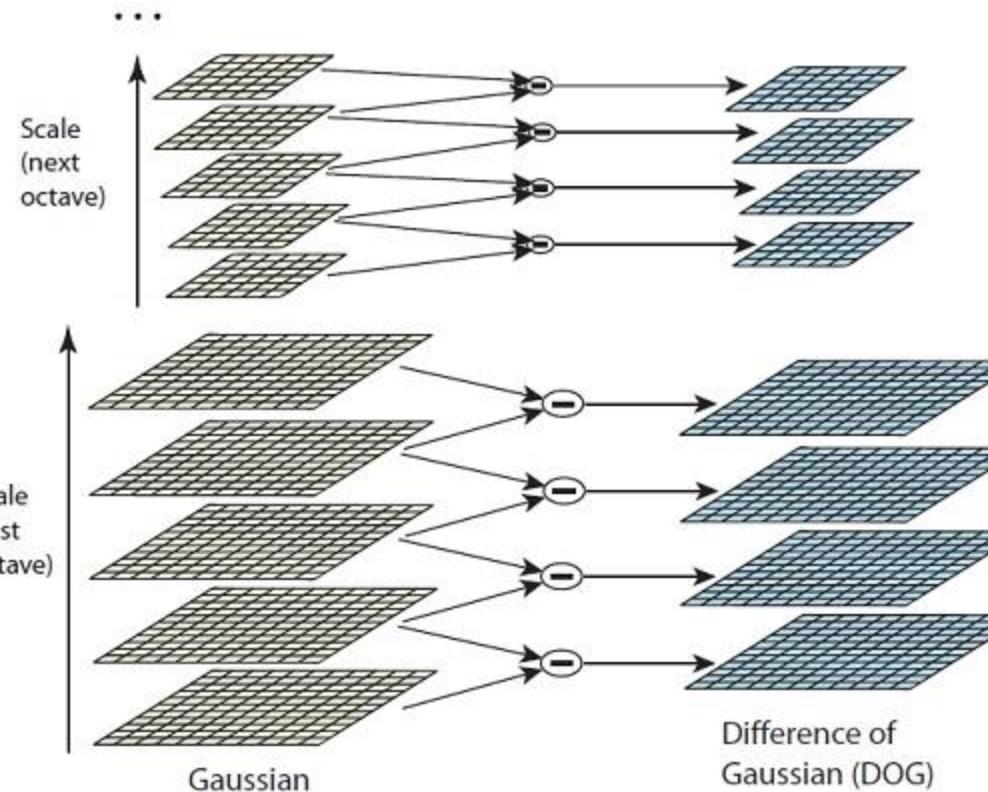
$$\mu_{f \otimes g} = \mu_f + \mu_g \quad \text{and} \quad \sigma_{f \otimes g} = \sqrt{\sigma_f^2 + \sigma_g^2}$$



0

Chose k=sqrt(2) means :  $\sigma_f = \sigma_g$

# LoG approximation

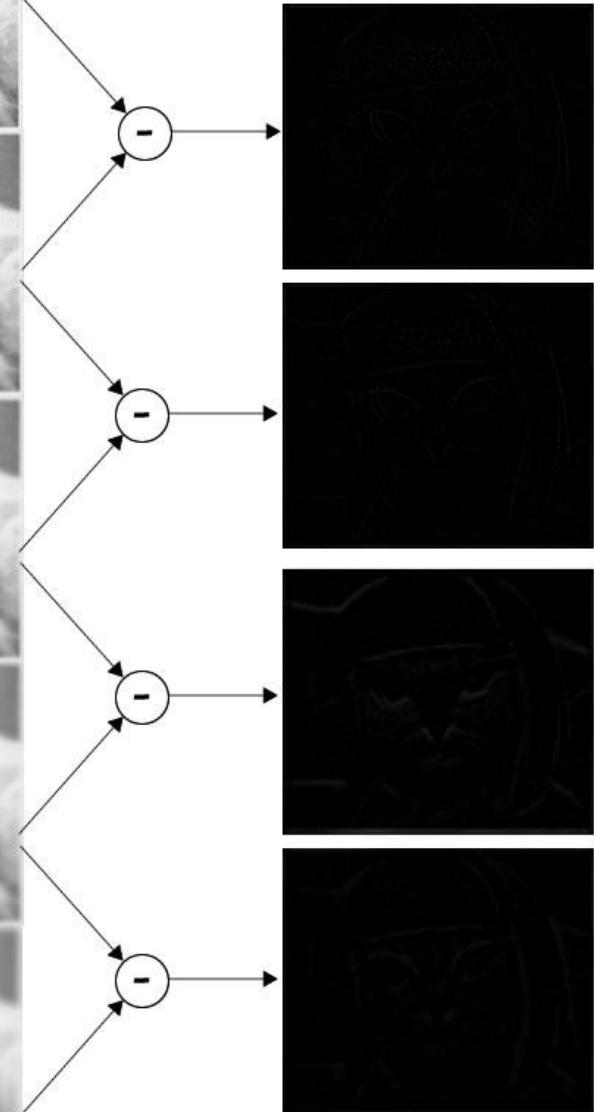


$$G(x, y, k\sigma) - G(x, y, \sigma) \approx (k - 1)\sigma^2 \nabla^2 G.$$

The Guassian blurred images



The Difference of Gaussian images



# Matlab Implementation !

```
% %%% Create first interval of the first octave %%%%
init_image=impyramid(gauss_filter(image1,antialiassigma,4*antialiassigma),'expand');
gaussians(1)={gauss_filter(init_image,sigmapvalue,4*sigmapvalue)};

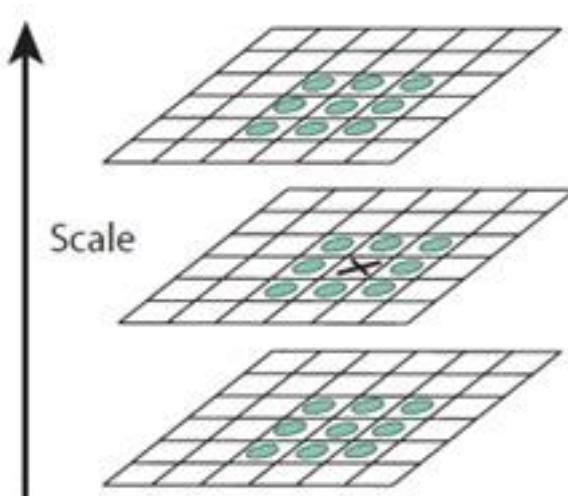
% %%% Generates all the blurred out images for each octave %%%%
% %%% and the DoG images %%%%
for i=1:num_octaves
    sigma=sigmapvalue; %reset the sigma value
    for j=1:(num_intervals+2)
        sigma=sigma*2^((j-1)/2); %Assign a sigma value according to the scale
        previmage=cell2mat(gaussians(j,i)); %Obtain the previous image
        newimage=gauss_filter(previmage,sigma,4*sigma); %apply a new smoothing
        dog=previmage-newimage; %calculate the difference of gaussians

        %save the results
        gaussians(j+1,i)={newimage};
        dogs(j,i)={dog};
    end

    %Build the init image in the next level
    if(i<num_octaves)
        lowscale=cell2mat(gaussians(num_intervals+1,i));
        upscale=impyramid(lowscale,'reduce');
        gaussians(1,i+1)={upscale};
    end
end
```

# Finding keypoints

- a) Locate maxima/minima in DoG images



# Matlab Implementation

```
for i=1:num_octaves
    for j=2:(num_intervals+1)
        % Obtain the matrices where to look for the extrema
        level=cell2mat(dogs(j,i));
        up=cell2mat(dogs(j+1,i));
        down=cell2mat(dogs(j-1,i));

        [sx,sy]=size(level);

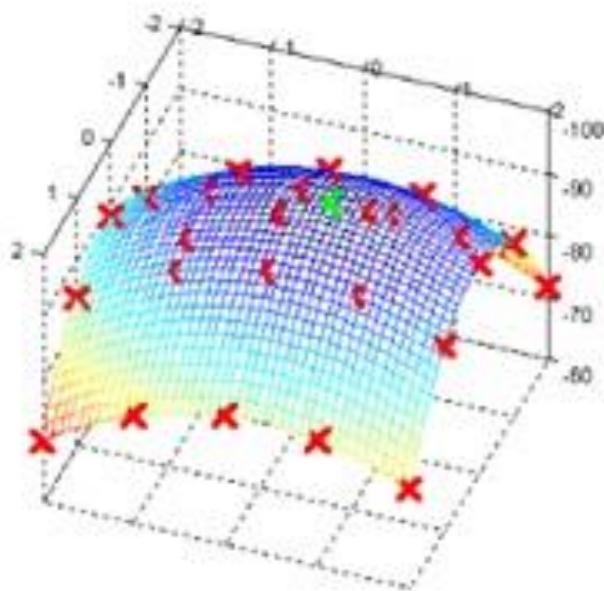
        %look for a local maxima
        local_maxima=(level(2:sx-1,2:sy-1)>level(1:sx-2,1:sy-2)) & ( level(2:sx-1,2:sy-1) > level(1:sx-2,2:sy-1) ) & (level(2:sx-1,2:sy-1)>level(1:sx-2,3:sy)) & (level(2:sx-1,2:sy-1)>level(2:sx-1,1:sy-2)) & (level(2:sx-1,2:sy-1)>level(2:sx-1,3:sy)) & (level(2:sx-1,2:sy-1)>level(3:sx,1:sy-2)) & (level(2:sx-1,2:sy-1)>level(3:sx,2:sy-1)) & (level(2:sx-1,2:sy-1)>level(3:sx,3:sy));
        local_maxima=local_maxima & (level(2:sx-1,2:sy-1)>up(1:sx-2,1:sy-2)) & ( level(2:sx-1,2:sy-1) > up(1:sx-2,2:sy-1) ) & (level(2:sx-1,2:sy-1)>up(1:sx-2,3:sy)) & (level(2:sx-1,2:sy-1)>up(2:sx-1,1:sy-2)) & (level(2:sx-1,2:sy-1)>up(2:sx-1,2:sy-1)) & (level(2:sx-1,2:sy-1)>up(2:sx-1,3:sy)) & (level(2:sx-1,2:sy-1)>up(3:sx,1:sy-2)) & (level(2:sx-1,2:sy-1)>up(3:sx,2:sy-1)) & (level(2:sx-1,2:sy-1)>up(3:sx,3:sy));
        local_maxima=local_maxima & (level(2:sx-1,2:sy-1)>down(1:sx-2,1:sy-2)) & ( level(2:sx-1,2:sy-1) > down(1:sx-2,2:sy-1) ) & (level(2:sx-1,2:sy-1)>down(1:sx-2,3:sy)) & (level(2:sx-1,2:sy-1)>down(2:sx-1,1:sy-2)) & (level(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)) & (level(2:sx-1,2:sy-1)>down(2:sx-1,3:sy)) & (level(2:sx-1,2:sy-1)>down(3:sx,1:sy-2)) & (level(2:sx-1,2:sy-1)>down(3:sx,2:sy-1)) & (level(2:sx-1,2:sy-1)>down(3:sx,3:sy));

        %look for a local minima
        local_minima=(level(2:sx-1,2:sy-1)>level(1:sx-2,1:sy-2)) & ( level(2:sx-1,2:sy-1) > level(1:sx-2,2:sy-1) ) & (level(2:sx-1,2:sy-1)>level(1:sx-2,3:sy)) & (level(2:sx-1,2:sy-1)>level(2:sx-1,1:sy-2)) & (level(2:sx-1,2:sy-1)>level(2:sx-1,3:sy)) & (level(2:sx-1,2:sy-1)>level(3:sx,1:sy-2)) & (level(2:sx-1,2:sy-1)>level(3:sx,2:sy-1)) & (level(2:sx-1,2:sy-1)>level(3:sx,3:sy));
        local_minima=local_minima & (level(2:sx-1,2:sy-1)>up(1:sx-2,1:sy-2)) & ( level(2:sx-1,2:sy-1) > up(1:sx-2,2:sy-1) ) & (level(2:sx-1,2:sy-1)>up(1:sx-2,3:sy)) & (level(2:sx-1,2:sy-1)>up(2:sx-1,1:sy-2)) & (level(2:sx-1,2:sy-1)>up(2:sx-1,2:sy-1)) & (level(2:sx-1,2:sy-1)>up(2:sx-1,3:sy)) & (level(2:sx-1,2:sy-1)>up(3:sx,1:sy-2)) & (level(2:sx-1,2:sy-1)>up(3:sx,2:sy-1)) & (level(2:sx-1,2:sy-1)>up(3:sx,3:sy));
        local_minima=local_minima & (level(2:sx-1,2:sy-1)>down(1:sx-2,1:sy-2)) & ( level(2:sx-1,2:sy-1) > down(1:sx-2,2:sy-1) ) & (level(2:sx-1,2:sy-1)>down(1:sx-2,3:sy)) & (level(2:sx-1,2:sy-1)>down(2:sx-1,1:sy-2)) & (level(2:sx-1,2:sy-1)>down(2:sx-1,2:sy-1)) & (level(2:sx-1,2:sy-1)>down(2:sx-1,3:sy)) & (level(2:sx-1,2:sy-1)>down(3:sx,1:sy-2)) & (level(2:sx-1,2:sy-1)>down(3:sx,2:sy-1)) & (level(2:sx-1,2:sy-1)>down(3:sx,3:sy));

        extrema=local_maxima | local_minima;
    end
end
```

# Finding keypoints

- b) Find subpixel maxima/minima



$$D(\mathbf{x}) = D + \frac{\partial D^T}{\partial \mathbf{x}} \mathbf{x} + \frac{1}{2} \mathbf{x}^T \frac{\partial^2 D}{\partial \mathbf{x}^2} \mathbf{x}$$

# Get rid of bad key points

- **Removing low contrast features**

If the magnitude of the intensity (i.e., without sign) at the current pixel in the DoG image (that is being checked for minima/maxima) is less than a certain value, it is rejected

- **Removing edges**

$$\text{Tr}(\mathbf{H}) = D_{xx} + D_{yy}$$

$$\text{Det}(\mathbf{H}) = D_{xx}D_{yy} - (D_{xy})^2$$

$$R = \frac{\text{Tr}(\mathbf{H})^2}{\text{Det}(\mathbf{H})}$$

- ◎ If the value of R is greater for a candidate keypoint, then that keypoint is poorly localized and hence rejected.

$$H = \begin{bmatrix} D_{xx} & D_{xy} \\ D_{xy} & D_{yy} \end{bmatrix}$$

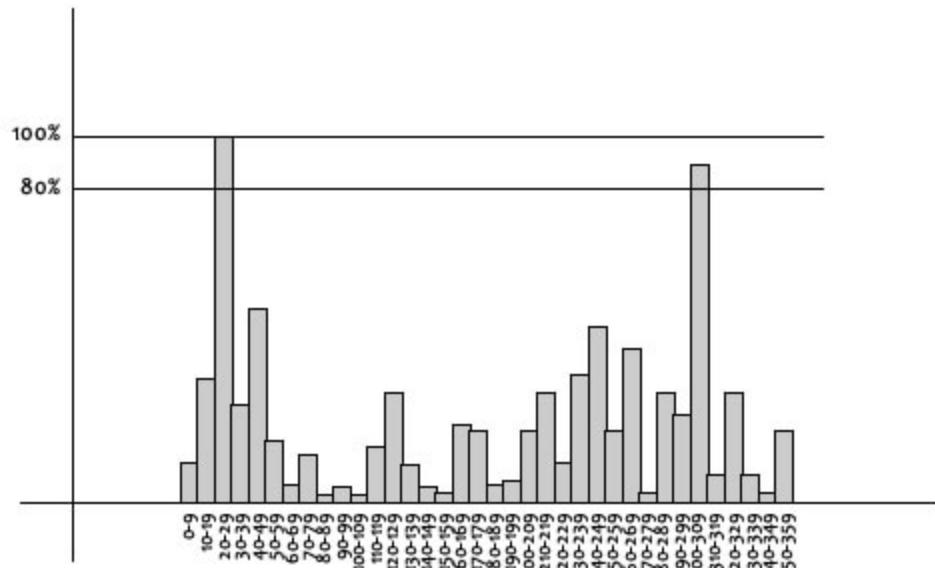
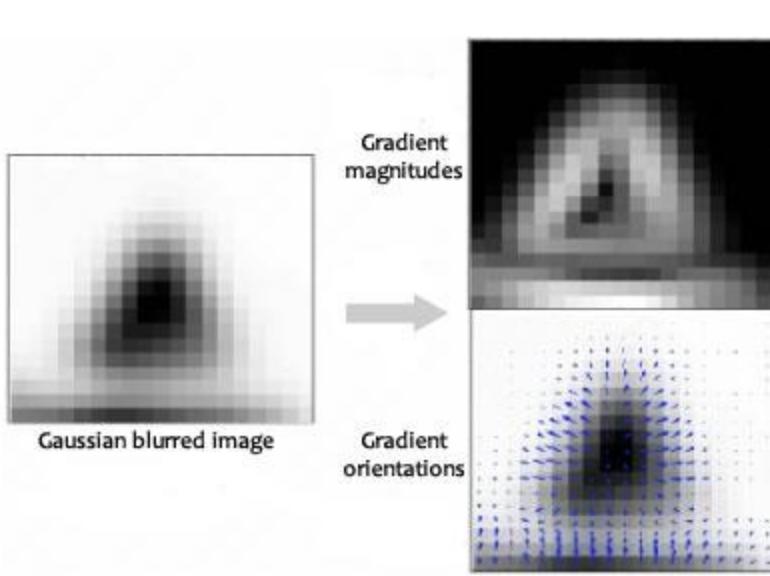
$$\frac{D_{xx} + D_{yy}}{D_{xx}D_{yy} - (D_{xy})^2} < \frac{(r+1)^2}{r}$$

# Matlab Implementation

```
%indices of the extrema points
[x,y]=find(extrema);
numtimes=size(find(extrema));

for k=1:numtimes
    x1=x(k);
    y1=y(k);
    if(abs(level(x1+1,y1+1))<contrast_threshold) %low contrast point are discarded
        extrema(x1,y1)=0;
    else %keep being extrema, check for edge
        rx=x1+1;
        ry=y1+1;
        fxx= level(rx-1,ry)+level(rx+1,ry)-2*level(rx,ry); % double derivate in x direction
        fyy= level(rx,ry-1)+level(rx,ry+1)-2*level(rx,ry); % double derivate in y direction
        fxy= level(rx-1,ry-1)+level(rx+1,ry+1)-level(rx-1,ry+1)-level(rx+1,ry-1); %derivate inx and y direction
        trace=fxx+fyy;
        deter=fxx*fyy-fxy*fxy;
        curvature=trace*trace/deter;
        curv_threshold= ((r_curvature+1)^2)/r_curvature;
        if(deter<0 || curvature>curv_threshold) %Reject edge points
            extrema(x1,y1)=0;
        end
    end
end
```

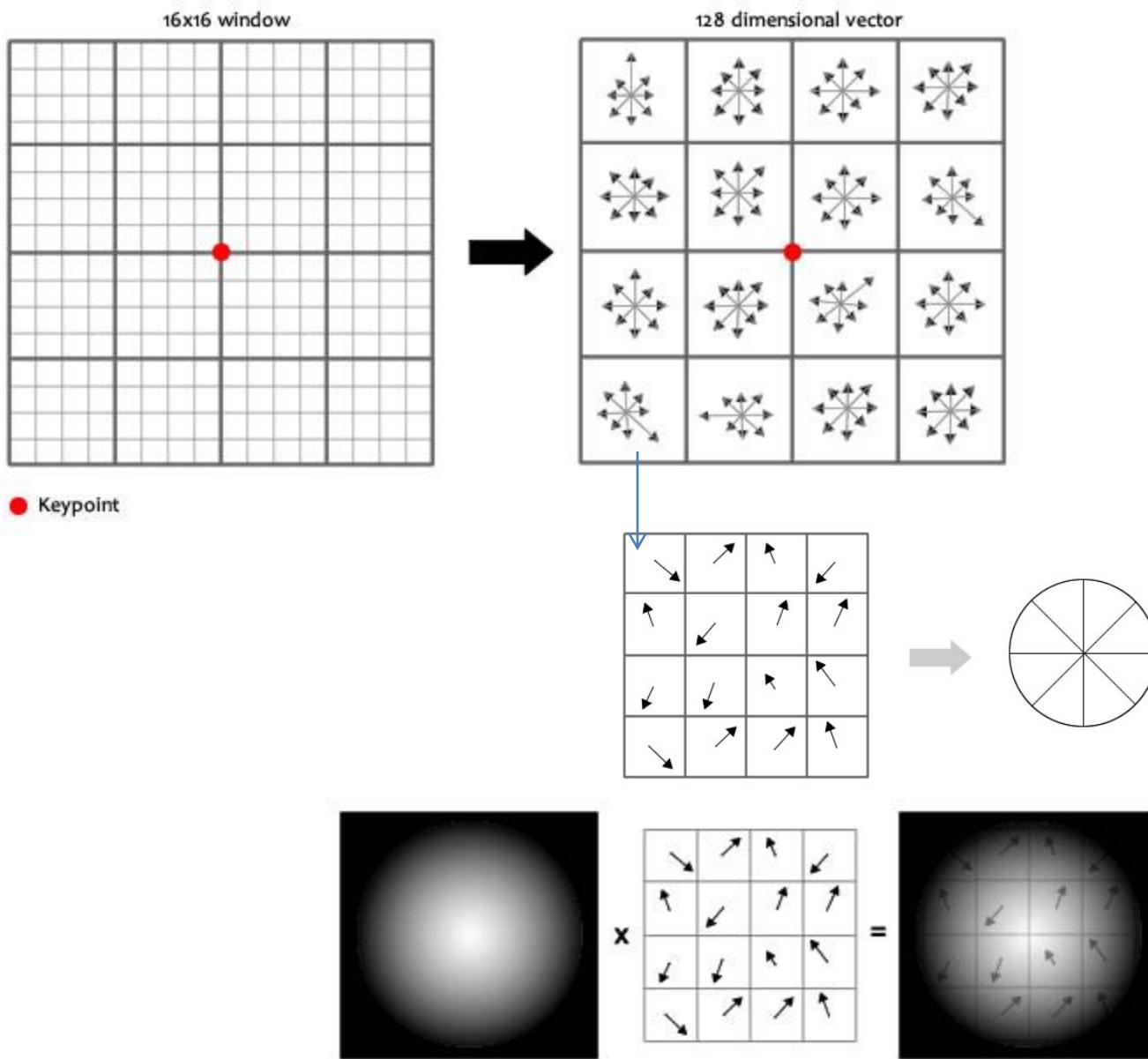
# Assigning an orientation to the keypoints



$$m(x, y) = \sqrt{(L(x+1, y) - L(x-1, y))^2 + (L(x, y+1) - L(x, y-1))^2}$$

$$\theta(x, y) = \tan^{-1}((L(x, y+1) - L(x, y-1)) / (L(x+1, y) - L(x-1, y)))$$

# Generate SIFT features



# Generate SIFT features

- You take a  $16 \times 16$  window of “in-between” pixels around the keypoint. You split that window into sixteen  $4 \times 4$  windows. From each  $4 \times 4$  window you generate a histogram of 8 bins. Each bin corresponding to 0-44 degrees, 45-89 degrees, etc. Gradient orientations from the  $4 \times 4$  are put into these bins. This is done for all  $4 \times 4$  blocks. Finally, you normalize the 128 values you get.
- To solve a few problems, you subtract the keypoint’s orientation and also threshold the value of each element of the feature vector to 0.2 (larger than 0.2 becomes 0.2) (and normalize again).

# Testing the detector

- `i=imread('groceries_gray.jpg');`
- `sift(i,3,5,1.1)`

# VL\_feat

- The VLFeat open source library implements popular computer vision algorithms including SIFT, MSER, k-means, hierarchical k-means, agglomerative information bottleneck, and quick shift. It is written in C for efficiency and compatibility, with interfaces in MATLAB for ease of use, and detailed documentation throughout. It supports Windows, Mac OS X, and Linux

# VL\_feat

- Download vl\_feat from <http://www.vlfeat.org/>
- `run('VLFEATROOT/toolbox/vl_setup')`
- Permanent setup
  - To permanently add VLFeat to your MATLAB environment, add this line to your startup.m file:
  - `run('VLFEATROOT/toolbox/vl_setup')`

# Extracting frames and descriptors

```
pfx = fullfile(vl_root,'data', 'roofs1.jpg') ;
I = imread(pfx) ;
image(I) ;
I = single(rgb2gray(I)) ;
[f,d] = vl_sift(I) ;
perm = randperm(size(f,2)) ;
sel = perm(1:50) ;
h1 = vl_plotframe(f(:,sel)) ;
h2 = vl_plotframe(f(:,sel)) ;
set(h1,'color','k','linewidth',3) ;
set(h2,'color','y','linewidth',2) ;
h3 = vl_plotsiftdescriptor(d(:,sel),f(:,sel)) ;
set(h3,'color','g')
```

# Basic Matching

```
pxf = fullfile(vl_root,'data', 'roofs1.jpg') ;  
I = imread(pfx) ;  
figure; image(I) ;  
la = single(rgb2gray(I)) ;
```

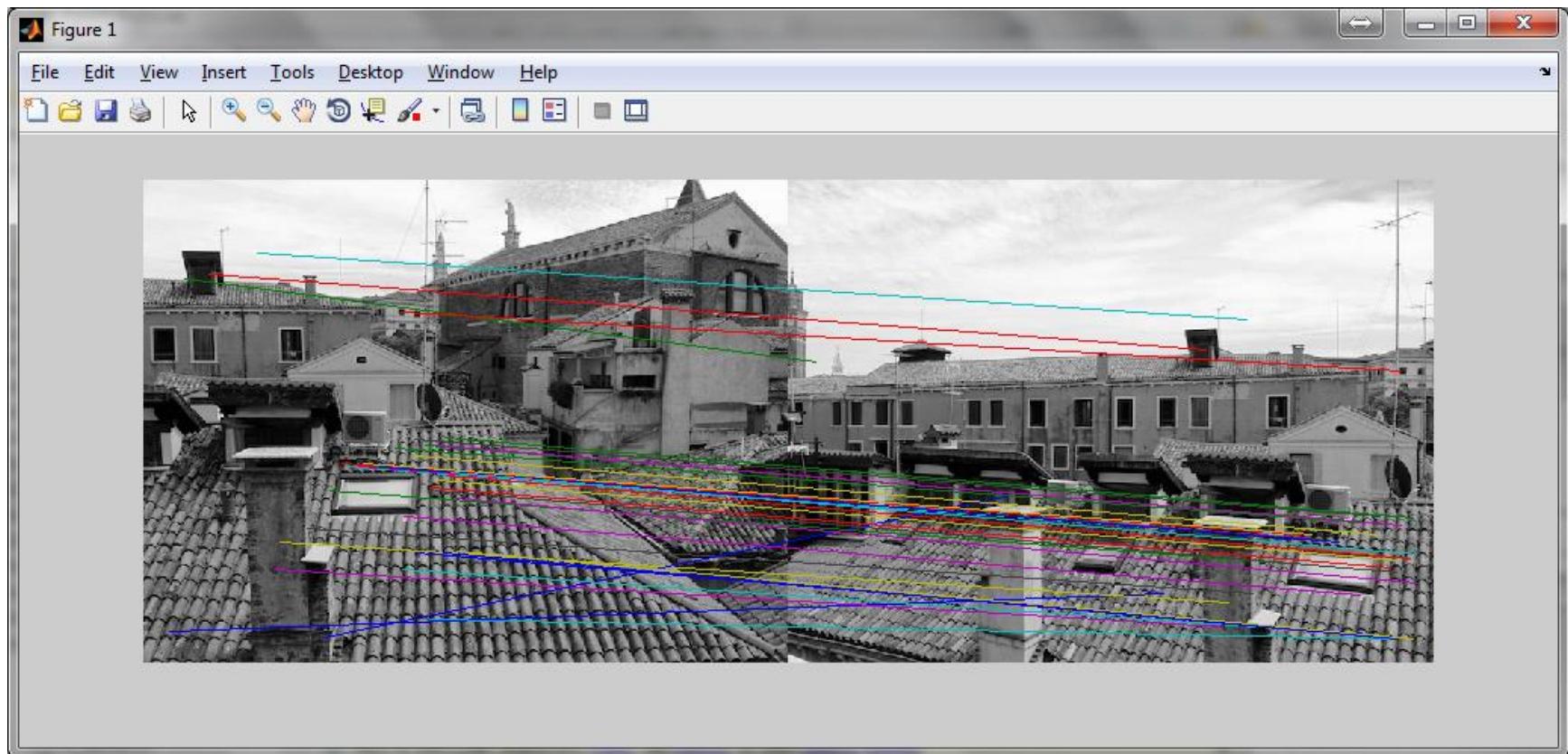
```
pxf = fullfile(vl_root,'data', 'roofs2.jpg') ;  
I = imread(pfx) ;  
figure, image(I) ;  
lb = single(rgb2gray(I)) ;
```

```
[fa, da] = vl_sift(la) ;  
[fb, db] = vl_sift(lb) ;  
[matches, scores] = vl_ubcmatch(da, db) ;
```

# Visualization

```
m1= fa(1:2,matches(1,:));
m2=fb(1:2,matches(2,:));
m2(1,:)= m2(1,:)+size(la,2)*ones(1,size(m2,2));
X=[m1(1,:);m2(1,:)];
Y=[m1(2,:);m2(2,:)];
c=[la lb];
imshow(c,[]);
hold on;
line(X(:,1:3:100),Y(:,1:3:100))
```

# Visualization



# Custom frames

- The MATLAB command `vl_sift` (and the command line utility) can bypass the detector and compute the descriptor on custom frames using the `Frames` option.
- For instance, we can compute the descriptor of a SIFT frame centered at position (100,100), of scale 10 and orientation -pi/8 by
- `fc = [100;100;10;-pi/8] ;`
- `[f,d] = vl_sift(l,'frames',fc) ;`
- `fc = [100;100;10;0] ;`
- `[f,d] = vl_sift(l,'frames',fc,'orientations') ;`