

COT 4210 Homework #6: Reducibility
Due Date: Tuesday November 9, 2010 (in class)

- 1) Find a match in the following instance of the PCP: $\left\{ \left[\frac{ab}{abab} \right], \left[\frac{b}{a} \right], \left[\frac{aba}{b} \right], \left[\frac{aa}{a} \right] \right\}$.
 - 2) Show that A_{TM} is not mapping reducible to E_{TM} .
 - 3) Let $S = \{ \langle M \rangle \mid M \text{ is a TM that accepts } w^R \text{ whenever it accepts } w \}$. Show that S is undecidable.
 - 4) Consider the problem of testing whether a Turing machine M on an input w ever attempts to move its head left at any point during its computation on w . Formulate this problem as a language and show that it's decidable.
 - 5) Show that the PCP is decidable over a unary alphabet, that is, over the alphabet $\Sigma = \{1\}$.
- Bonus Question) Show that the PCP is undecidable over a binary alphabet, that is, over the alphabet $\Sigma = \{0, 1\}$.