

**COT 3100 Fall 2017 Homework #4**  
**Please Consult WebCourses for the due date/time**

1) Find the greatest common divisor of each of the following pairs of integers using the Euclidean Algorithm:

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|----------------|-----------------|-----------------|
| a) 123 and 63  | c) 131 and 108  | e) 1111 and 111 |
| b) 979 and 782 | d) 923 and 7238 | f) 555 and 330  |

2) Determine  $108^{-1} \pmod{131}$ . (Note: You can use your work from question 1c if you'd like.)

3) Without the use of a calculator determine the remainder when  $47^{37}$  is divided by 51. Please show all of your steps by hand and utilize one of the two methods shown in class.

4) Prove or disprove: if  $p$  and  $q$  are prime numbers then  $pq - 2$  is also a prime number.

5) Find the least common multiple of each pair of numbers from question 1. Use your results from question 1.

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|----------------|-----------------|-----------------|
| a) 123 and 63  | c) 131 and 108  | e) 1111 and 111 |
| b) 979 and 782 | d) 923 and 7238 | f) 555 and 330  |

6) Determine the number of divisors that each of the following integers have:

- |        |        |           |
|--------|--------|-----------|
| a) 96  | c) 267 | e) 625040 |
| b) 108 | d) 289 | f) 698112 |

7) Give a summary of the life and mathematical contributions of Sophie Germain. Please aim for a length of roughly 200 - 400 words. **Your summary must be typed.** Please state the sources you used in writing your summary.