

Honors Seminar Mathematical Modeling
Homework #4
Assigned: 2/11/14 (Tuesday)
Due: 2/18/14 (Tuesday) – in class, written

1) Find a closed form solution to the following recurrence relation using the first method (characteristic equation) shown in class:

$$\begin{aligned}T(1) &= -2, T(2) = 2 \\T(n) &= 5T(n-1) - 6T(n-2), \text{ for all } n > 2\end{aligned}$$

2) Find a closed form solution to the following recurrence relation using the first method (characteristic equation) shown in class:

$$\begin{aligned}T(0) &= 5, T(1) = 21 \\T(n) &= 6T(n-1) - 9T(n-2), \text{ for all } n > 1\end{aligned}$$

3) Find a closed form solution to the following recurrence relation using the first method (characteristic equation) shown in class:

$$\begin{aligned}T(0) &= 5, T(1) = 7 \\T(n) &= -2T(n-1) - 4T(n-2), \text{ for all } n > 1\end{aligned}$$

4) Find a closed form solution to the following recurrence relation using the generating functions method shown in class:

$$\begin{aligned}T(0) &= 7, T(1) = 14 \\T(n) &= T(n-1) + 12T(n-2)\end{aligned}$$

5) Determine the number of solutions to the following equation:

$$a + b + c + d + e + f = 20$$

for integers a, b, c, d, e and f that satisfy the following restrictions:

$$a < 5, 2 < b < 10, \text{ and } d > 3.$$

6) Write out a generating function using the information in question 5 so that its coefficient for the term x^{20} equals the answer to question 5. When possible, simplify the generating function to a closed form with relatively few terms.