

**CIS 3362 Test #2: Modern Symmetric Encryption Schemes (DES, AES)**  
**Date: 10/26/2016**

**Last Name:** \_\_\_\_\_, **First Name:** \_\_\_\_\_

1) (8 pts) Consider a 16 bit block cipher that uses a permutation matrix,  $P'$ , in the same format as IP in DES, given below. Let the 16 bit plaintext input to the matrix  $P'$  be 1001 0111 1011 0011. What is the output? (Express your answer as 16 bits.)

$$\begin{bmatrix} 14 & 10 & 3 & 7 \\ 9 & 12 & 13 & 15 \\ 6 & 11 & 8 & 4 \\ 16 & 2 & 5 & 1 \end{bmatrix}$$

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2) (12 pts) You are attempting to brute force a DES key. Luckily, you have obtained the following bit locations of the key (out of the locations  $k_1, k_2, \dots, k_{64}$  given in the official specification):

$k_1, k_5, k_8, k_{17}, k_{18}, k_{19}, k_{20}, k_{21}, k_{22}, k_{23}, k_{24}, k_{42}, k_{44}, k_{45}, k_{47}, k_{56}, k_{60},$  and  $k_{64}$

How many keys do you have to try to ensure that you find the appropriate key? (Assume that we have a matching plaintext and ciphertext block we can use to verify if a guess to the key is correct or not and the correct bits for the bit locations specified above in the key.) Please leave your answer as a power of 2.

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3) (16 pts) Consider a portion of a single DES round where the first 24 bits of input (expressed in HEX) to S boxes  $S_1, S_2, S_3, S_4$  is 3A7ED8. What are the 16 bits of output from those 4 S-boxes? Express your result in binary. (Note: Partial credit on this question will be limited for obvious reasons, so double check your answers.)

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4) (10 pts) In the DES key schedule, the algorithm keeps a buffer of bits whose left half is  $C_i$  and whose right half is  $D_i$ , for values of  $i$  from 0 to 16. Let  $C_5 = F560B94$ , represented in hex. Calculate  $C_6$  and give your result as 7 hex characters.

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5) (2 pts) Why doesn't the value 24 appear in the DES key schedule matrix PC-1?

6) (2 pts) Why are all of the values from 57 to 64 missing in the DES key schedule matrix PC-2?

7) (2 pts) Why is it possible for the value 24 to appear in the DES key schedule matrix PC-2? (It does appear, in the 4<sup>th</sup> position.)

8) (8 pts) Let the state matrix to AES right before the SubBytes step be the matrix shown below. Show the state of the matrix right AFTER the SubBytes step:

3D	FF	09	31
85	4B	75	E2
C6	BD	2E	18
5A	6C	A0	E4


9) (8 pts) Let the state matrix to AES right before the ShiftRows step be your answer from problem 8. Show the state of the matrix AFTER the ShiftRows step:


10) (12 pts) Consider the process of AES Key Expansion. Imagine that we have:

$w[16] = 54\ 9E\ B6\ 38$  (in hex)

$w[19] = 01\ F7\ AD\ C2$  (in hex)

Calculate  $w[20]$ , showing each of the following intermediate results: RotWord(temp), SubWord(RotWord(temp)), Rcon[i/4], and the result of the XOR with Rcon[i/4].

RotWord	SubWord	Rcon[i/4]	XOR	FinalResult

11) (18 pts) In class we discussed multiplication in the AES field  $GF(2^8)$  with the irreducible polynomial  $x^8 + x^4 + x^3 + x + 1$ . Based on this discussion, derive the answer for the calculation of  $07 \times E5$  in this field. Express your result as 8 bits.

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12) (2 pts) What does a football player playing the position of running back primarily do when holding a football?

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**Scratch Page - Please clearly mark any work on this page you would like graded.**