

### LA Session - Induction Preparation

- 1) An arithmetic sequence  $a_1, a_2, a_3, \dots$  is such that  $a_{10} = 40$  and  $a_{25} = 10$ . Determine both  $a_1$  and the sum of the first 50 terms of the sequence.
- 2) An infinite geometric sequence  $a_1, a_2, a_3, \dots$  has a sum of 10. If the odd indexed terms ( $a_1, a_3, \dots$ ) have a sum of 7, what is the common ratio of the sequence? What is the first term of the sequence?
- 3) Determine the following summation in terms of  $n$ :  $\sum_{i=1}^{2n} (3i^2 - 4i)$ .
- 4) Determine the following infinite summation:  $\sum_{i=1}^{\infty} (2i - 1) \left(\frac{1}{2}\right)^i$ .
- 5) Determine the following matrix sum:  $\begin{bmatrix} 6 & 3 & -2 \\ 5 & -9 & 7 \end{bmatrix} + \begin{bmatrix} -2 & 12 & 3 \\ 6 & 4 & 8 \end{bmatrix}$ .
- 6) Determine the following matrix product,  $\begin{bmatrix} 2^n & 1 - 2^n \\ 3 & 2^{n-1} \end{bmatrix} \begin{bmatrix} 3 & 2 \\ 1 & -1 \end{bmatrix}$ , in terms of  $n$ .
- 7) Let the Fibonacci Sequence be defined as follows:  $F_0 = 0, F_1 = 1, F_n = F_{n-1} + F_{n-2}$ , for all integers  $n \geq 2$ . Determine and simplify the following matrix product, in terms of  $n$ :

$$\begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} F_n & F_{n-1} \\ F_{n-1} & F_{n-2} \end{bmatrix}$$