

COT 3100 Recitation: Log Problems

Set #1

- 1) What is the value of $(81^{\log_3 1234})^{0.25}$?
- 2) Determine the ordered pair, (a, b), that satisfies the following pair of equations:

$$\log_{16} a^2 + \log_8 b^3 = 11$$

$$\log_8 a^6 + \log_{16} b^{10} = 32$$

Note: You may express a and b as a some base raised to an exponent instead of a single value, if you wish.

- 3) What is the value of a for which $\sum_{i=2}^{10} \frac{1}{\log_i a} = 1$?
- 4) The sequence $\log_{12} 162, \log_{12} x, \log_{12} y, \log_{12} z, \log_{12} 1250$ is an arithmetic progression. What is x?

Set #2

- 1) Solve for x in the following equation: $\log_2 x^3 + \log_4 (8x^2) = -\frac{5}{2}$
- 2) If $3^{\log_9 x} = 9^{\log_3 27}$, what is the prime factorization of x?
- 3) What is the value of the following summation?

$$\sum_{i=1}^n \log_{n!} i$$

- 4) Define a function f as follows: $f(1) = 2$. For all integers $n > 1$, $f(n) = (f(n-1))^{2^n}$.

What is the value of $\log_{65536}(\log_{65536}(f(4)))$?

Express your answer in the form $2^a + 2^b$, where both a and b are integers. Note that $65536 = 2^{16}$.