# Computer Science Foundation Exam 

January 16, 2021<br>Section I A<br>\section*{DATA STRUCTURES}

## ONLINE EXAM

Directions: You may either directly edit this document, or write out your answers in a .txt file, or scan your answers to .pdf and submit them in the COT 3960 Webcourses for the Assignment "Section I A". Please put your name, UCFID and NID on the top left hand corner of each document you submit. Please aim to submit 1 document, but if it's necessary, you may submit 2. Clearly mark for which question your work is associated with. If you choose to edit this document, please remove this cover page from the file you submit and make sure your name, UCFID and NID are on the top left hand corner of the next page (first page of your submission).

| Question \# | Max Pts | Category | Score |
| :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | $\mathbf{5}$ | DSN |  |
| 2 | $\mathbf{1 0}$ | DSN |  |
| $\mathbf{3}$ | $\mathbf{1 0}$ | ALG |  |
| TOTAL | $\mathbf{2 5}$ |  |  |

You must do all 3 problems in this section of the exam.
Problems will be graded based on the completeness of the solution steps and not graded based on the answer alone. Credit cannot be given unless all work is shown and is readable. Be complete, yet concise, and above all be neat. For each coding question, assume that all of the necessary includes (stdlib, stdio, math, string) for that particular question have been made.

Name: $\qquad$
UCFID: $\qquad$
NID: $\qquad$

1) ( 5 pts ) DSN (Dynamic Memory Management in C )

Suppose we have a function that is designed to take in a large string and trim it down to only the needed size. The function is called trim_buffer. It takes in 1 parameter: the buffer, which is a string with a max size of 1024 characters. It returns a string that is only the size needed to represent the valid characters in the buffer. The function is implemented below.

Identify all of the errors (there are multiple errors) with the following trim_buffer function.

```
#define BUFFERSIZE 1024
```

```
// Pre-condition: buffer has a '\0' character at or before index
// BUFFERSIZE-1.
// Post-condition: returns a pointer to a dynamically allocated
// string that is a copy of the contents of buffer,
// dynamically resized to the appropriate size.
char * trim_buffer(char * buffer) {
    char *string;
    int length;
    while (length < BUFFERSIZE && buffer[length] != '\0')
                length++;
    string = malloc(sizeof(char) * (length));
    length = 0;
    while ((string[length] = buffer[length]) != '\0')
                        length++;
    return;
}
```

2) (10 pts) DSN (Linked Lists)

Suppose we have a singly linked list implemented with the structure below. Write a recursive function that takes in the list and returns 1 if the list is non-empty AND all of the numbers in the list are even, and returns 0 if the list is empty OR contains at least one odd integer. (For example, the function should return 0 for an empty list, 1 for a list that contains 2 only, and 0 for a list that contains 3 only.)

```
struct node {
    int data;
    struct node* next;
};
int check_all_even(struct node *head) {
```

3) (10 pts) ALG (Queues)

Consider the circular array implementation of a queue named Q , implemented with the structure shown below.

```
struct queue {
    int *array;
    int num_elements;
    int front;
    int capacity;
};
```

Suppose the queue is created with a capacity of 5 and front and num_elements are initialzed to 0 . Trace the status of the queue by showing the valid elements in the queue and the position of front after each of the operations shown below. Indicate front by making bold the element at the front of the queue.

1. enqueue $(\mathrm{Q}, 50)$;
2. enqueue( $\mathrm{Q}, 34$ );
3. enqueue ( $\mathrm{Q}, 91$ );
4. $\mathrm{x}=\operatorname{dequeue}(\mathrm{Q})$;
5. enqueue $(\mathrm{Q}, 23)$;
6. $\mathrm{y}=$ dequeue $(\mathrm{Q})$;
7. enqueue( $\mathrm{Q}, \mathrm{y}$ );
8. enqueue( $\mathrm{Q}, 15$ );
9. enqueue $(\mathrm{Q}, \mathrm{x})$;
10. $\mathrm{x}=\operatorname{dequeue}(\mathrm{Q})$;

## After stmt \#1:



## After stmt \#3:



## After stmt \#5:



## After stmt \#7:

|  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |

## After stmt \#9:

|  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |

After stmt \#2:


## After stmt \#4:



## After stmt \#6:



## After stmt \#8:



## After stmt \#10:

|  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |

# Computer Science Foundation Exam 

January 16, 2021

Section I B

## DATA STRUCTURES

## ONLINE EXAM

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| Question \# | Max Pts | Category | Score |
| :--- | :---: | :---: | :---: |
| $\mathbf{1}$ | $\mathbf{1 0}$ | DSN |  |
| $\mathbf{2}$ | $\mathbf{5}$ | ALG |  |
| $\mathbf{3}$ | $\mathbf{1 0}$ | DSN |  |
| TOTAL | $\mathbf{2 5}$ |  |  |

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Name:
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NID: $\qquad$

1) (10 pts) DSN (Binary Trees)

Write a function named find_below() that takes a pointer to the root of a binary tree (root) and an integer value ( val ) and returns the greatest value in the tree that is strictly less than val. If no such value exists, simply return val itself. Note that the tree passed to your function will not necessarily be a binary search tree; it's just a regular binary tree.

For example:


```
find_below(root, 196) would return 22
find below(root, 1) would return 1
find below(root, 4) would return 1
find_below(root, 22) would return 18
find_below(root, 20) would return 18
find 'below(root, 8) would return 7
find'below(root, -23) would return -23
```

You must write your solution in a single function. You cannot write any helper functions.
The function signature and node struct are given below.

```
typedef struct node
{
    int data;
    struct node *left;
    struct node *right;
} node;
int find_below(node *root, int val)
{
```


## 2) ( 5 pts ) ALG (Heaps)

Show the state of the following minheap after performing the deleteMin operation. (Instead of writing this with a pen or pencil, typing the result in text similarly to how the drawing of the heap below was constructed will suffice.)

| 14 |  |  |  |
| :---: | :---: | :---: | :---: |
|  | / | $\backslash$ |  |
|  | 22 |  | 72 |
| / | 1 | / | $\backslash$ |
| 38 | 40 | 80 | 90 |

## 3) (10 pts) DSN (Tries)

Write a function that takes the root of a trie (root) and returns the number of strings in that trie that end with the letter $q$. The count member of the node struct indicates how many occurrences of a particular string have been inserted into the trie. So, a string can be represented in the trie multiple times. If a string ending in $q$ occurs multiple times in the trie, all occurrences of that string should be included in the value returned by this function.

The node struct and function signature are given below. You must write your solution in a single function. You cannot write any helper functions.

```
typedef struct TrieNode
{
    // Pointers to the child nodes (26 total).
    struct TrieNode *children[26];
    // Indicates how many occurrences of a particular string are contained
    // in this trie. If none, this is set to zero (0).
    int count;
} TrieNode;
int ends_with_q_count(TrieNode *root)
{
```

\}

# Computer Science Foundation Exam 

January 16, 2021

## Section II A

## ALGORITHMS AND ANALYSIS TOOLS

## ONLINE EXAM

Directions: You may either directly edit this document, or write out your answers in a .txt file, or scan your answers to .pdf and submit them in the COT 3960 Webcourses for the Assignment "Section II A". Please put your name, UCFID and NID on the top left hand corner of each document you submit. Please aim to submit 1 document, but if it's necessary, you may submit 2. Clearly mark for which question your work is associated with. If you choose to edit this document, please remove this cover page from the file you submit and make sure your name, UCFID and NID are on the top left hand corner of the next page (first page of your submission).

| Question \# | Max Pts | Category | Score |
| :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | $\mathbf{1 0}$ | ANL |  |
| $\mathbf{2}$ | $\mathbf{5}$ | ANL |  |
| $\mathbf{3}$ | $\mathbf{1 0}$ | ANL |  |
| TOTAL | $\mathbf{2 5}$ |  |  |

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Name: $\qquad$
UCFID: $\qquad$
NID: $\qquad$

1) (10 pts) ANL (Algorithm Analysis)

What is the run-time of the function hash_func shown below, in terms of $n$, the length of its input string? Please provide sufficient proof of your answer. ( 9 out of the 10 points are awarded for the proof. 1 point is awarded for the answer.)

```
#include <stdio.h>
#include <string.h>
#define MOD 1072373
#define BASE 256
int hash_func(char* str);
int hash_func_rec(char* str, int k);
int hash_func(char* str) {
    return hash_func_rec(str, strlen(str));
}
int hash_func_rec(char* str, int k) {
    if (\overline{k}== -
    int sum = 0;
    for (int i=k-1; i>=0; i--)
            sum = (BASE*sum + str[i])%MOD;
        return (sum + hash_func_rec(str, k-1))%MOD;
}
```

2) (5 pts) ANL (Algorithm Analysis)

A sorting algorithm takes $\mathrm{O}(n \sqrt{n})$ time to sort $n$ values. The algorithm took .2 milliseconds to sort an array of 1000 values. How many seconds would it take to sort an array of size 900,000 ?
3) (10 pts) ANL (Recurrence Relations)

What is the closed form solution to the following recurrence relation? Please use the iteration technique, show all of your work and provide your final answer in Big-Oh notation.
$\mathrm{T}(1)=1$
$\mathrm{T}(\mathrm{n})=2 \mathrm{~T}(\mathrm{n} / 4)+1$

# Computer Science Foundation Exam 

January 16, 2021

## Section II B

## ALGORITHMS AND ANALYSIS TOOLS

## ONLINE EXAM

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| :--- | :---: | :---: | :---: |
| $\mathbf{1}$ | $\mathbf{1 0}$ | DSN |  |
| $\mathbf{2}$ | $\mathbf{5}$ | ALG |  |
| $\mathbf{3}$ | $\mathbf{1 0}$ | DSN |  |
| TOTAL | 25 |  |  |

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Name:
UCFID: $\qquad$
NID: $\qquad$

## 1) (10 pts) DSN (Recursive Coding)

Imagine a Towers of Hanoi puzzle with 4 towers, labeled A, B, C and D, with a tower of $n$ disks, starting on tower A , to be moved to tower B , using the usual rules of the puzzle. One strategy to solve the puzzle would be to move the k smallest disks recursively to tower D , where all 4 towers are used. Then, with the remaining $\mathrm{n}-\mathrm{k}$ disks, use the usual strategy (since tower $D$ is unavailable), which will take exactly $2^{n-k}-1$ moves, to transfer the bottom $\mathrm{n}-\mathrm{k}$ disks to tower B. Finally, now that you can use all 4 towers again, recursively transfer the k smallest disks on tower D to tower B , completing the puzzle. Sonia has decided that she wants the value of k to be set at (3n)/4, using integer division. For this question, write a recursive function that takes in $n$, the number of disks in the game, and returns the number of moves that it will take to solve the game using Sonia's strategy. A function prototype with pre and post conditions is provided below. (Note: In order to get full credit you MUST NOT USE the pow function in math.h because it returns a double which has inherent floating point error. Please manually use integers to calculate an exponent or bitwise operators.)

```
// Pre-condition: 1 <= n <= 115 (ensures no overflow)
// Post-condition: Returns the number of moves Sonia's strategy
// will take to solve a Towers of Hanoi with n
// disks with 4 towers.
int fourTowersNumMoves(int n) {
```

\}
2) ( 5 pts ) ALG (Sorting)

The code below is a buggy implementation Selection Sort.

```
void buggySelectionSort(int array[], int n) {
    for (int i=n-1; i>=0; i--) {
        int best = array[0];
        for (int j=1; j<=i; j++) {
            if (array[j] > best)
                best = array[j];
            }
        array[i] = best;
    }
}
```

(a) Conceptually, the variable best is storing the wrong thing. What should it store instead?
(b) If we fix the code so that best stores what it ought to, conceptually, we will have to change both the if statement inside of the j for loop as well as the assignment statement inside of the if. (With these two changes, best will store what it is supposed to store.) Once we make those changes, we can finish fixing the sort completely by replacing the line

```
array[i] = best;
```

with three lines of code (where one more variable is declared). Show the three line fix, assuming that best stored the conceptually correct value.

## 3) (10 pts) DSN (Bitwise Operators)

In the game of NIM, there are several piles with stones and two players alternate taking 1 or more stones from a single pile, until there are no more stones left. The person who takes the last stone wins. It turns out that if it's someone's turn, if they play optimally, they can win as long as the bitwise XOR of all of the number of stones in each pile is not equal to 0 . Write a function that takes in an array of values representing the number of stones in the piles of NIM and the length of that array, and returns 1, if the current player can win, and 0 otherwise, assuming both players play optimally.
int canWinNIM(int piles[], int numPiles) \{
\}

