

# Advanced Topics in Network Security

## Digital Signatures (Lecture #13)

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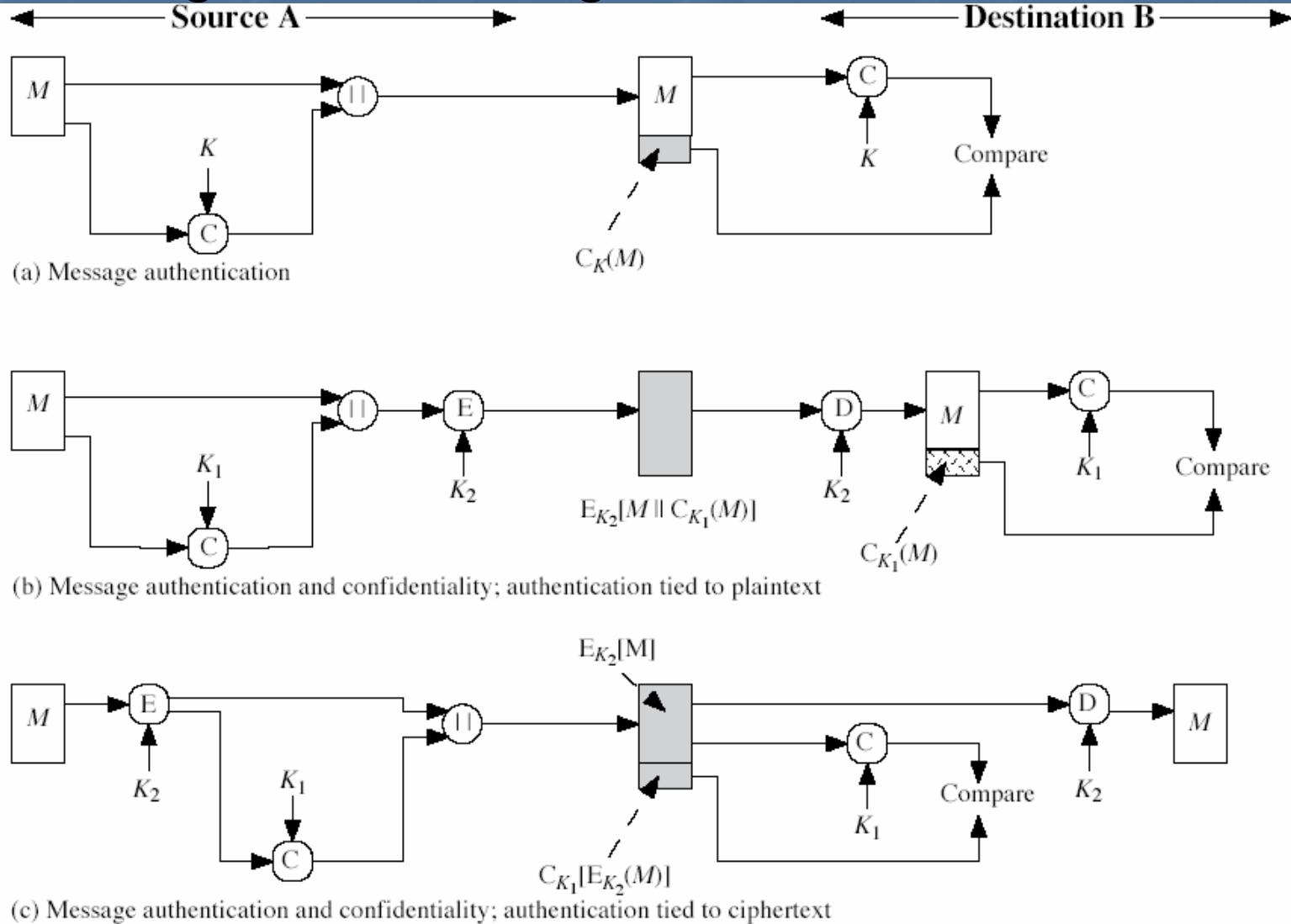


# Message Authentication

- Recall why we have used message authentication
  - Message authentication: a procedure to verify that received messages come from the alleged source and have not been altered.
  - Protects two parties who exchanges from any third party.
  - Trust between two communicating parties



# Message Authentication using MAC (Message Authentication Code)



# Why Digital Signature?

- What is the difference between message authentication and digital signature?
  - Message authentication does not protect two parties against each other.
  - What if there is no complete trust between sender and receiver?
- Examples (Bob sends an authenticated message to Alice)
  - Alice may forge a message and claim that it came from Bob by simply creating a message and append an authentication code using the key Bob and Alice share.
  - Bob can deny sending the message since it's possible for Alice to forge a message.



# Digital Signature

- Digital signatures provide the ability to:
  - verify author, date & time of signature
  - authenticate message contents
  - be verified by third parties to resolve disputes
- Hence, include authentication function with additional capabilities



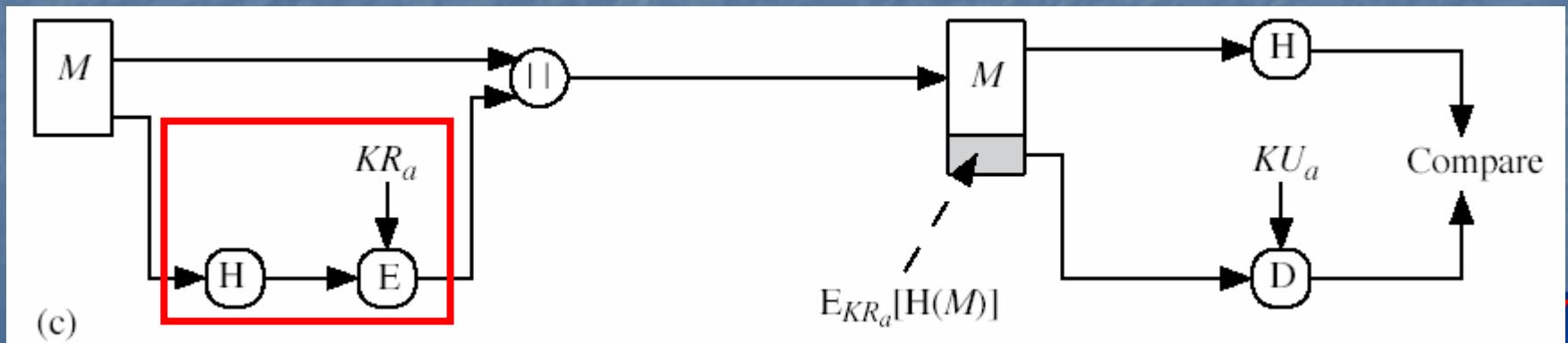
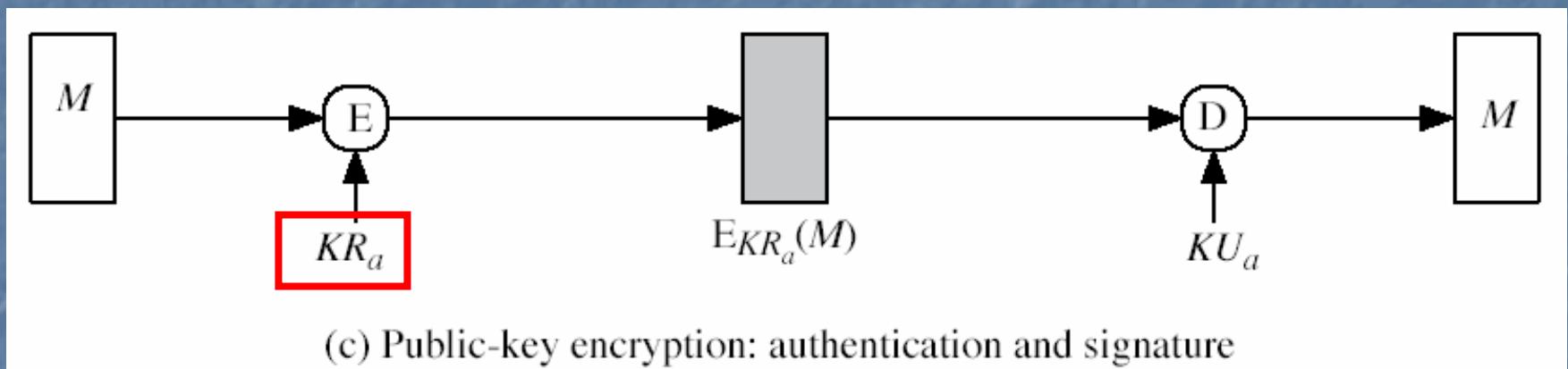
# Digital Signature Properties

- Must depend on the message signed
- Must use information unique to sender
  - To prevent both forgery and denial
- Must be relatively easy to produce
- Must be relatively easy to recognize & verify
- Be computationally infeasible to forge
  - With new message for existing digital signature
  - With fraudulent digital signature for given message
- Be practical save digital signature in storage
- Most of digital signature approaches can be classified into two categories
  - Direct vs. Arbitrated



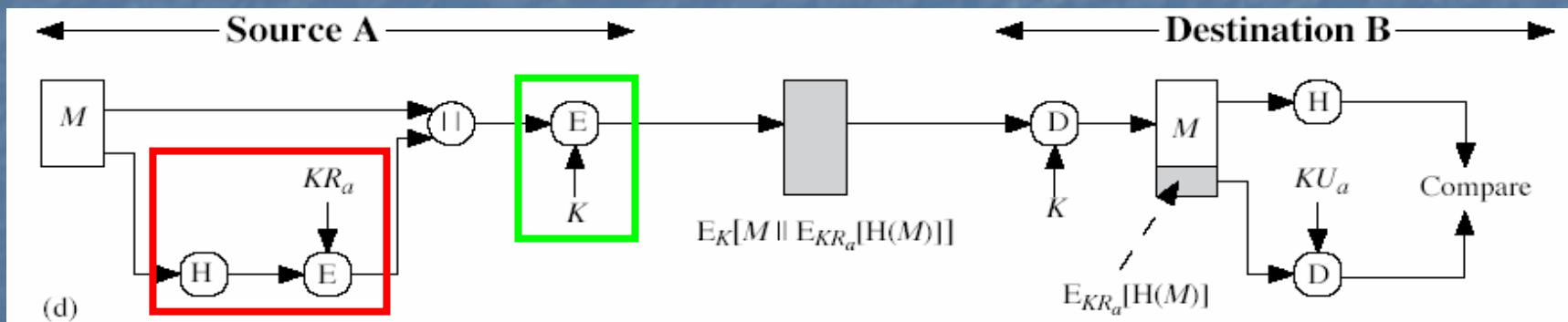
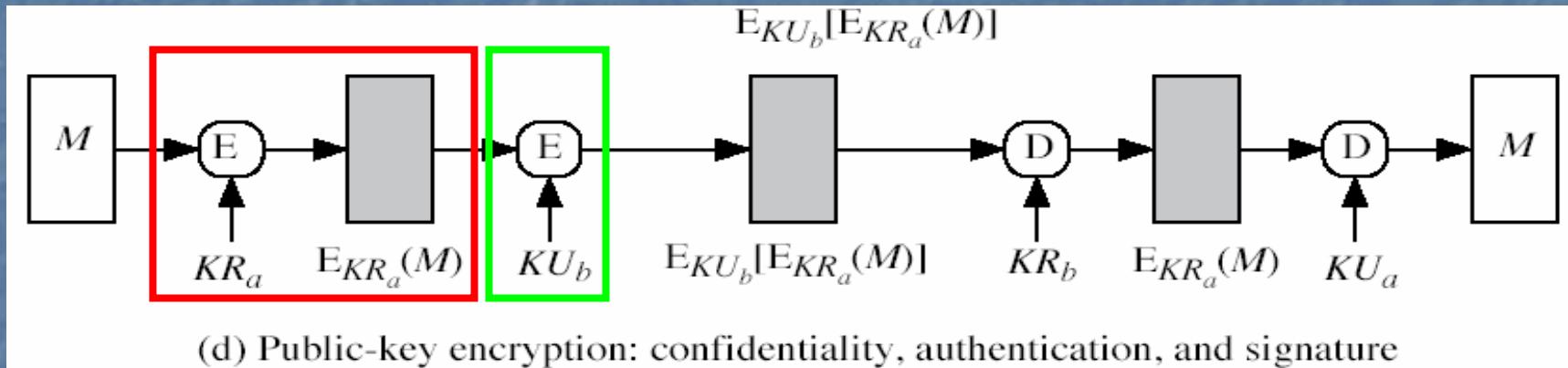
# Direct Digital Signatures

- Involve only sender & receiver
- Assumed receiver has sender's public-key
- Digital signature made by sender signing entire message or hash with private-key



# Direct Digital Signatures

- Confidentiality can be provided by further encrypting using receivers public-key or a shared secret key
- Important that sign first then encrypt message & signature



# Direct Digital Signatures

- Problems and weakness of direct digital signatures
  - Security depends on the sender's private key
    - could be lost and even the sender may deny sending the message claiming that the private key was stolen
  - Some private keys can be actually stolen and the opponent can replay the message at later time



# Arbitrated Digital Signatures

- Try to improve the weaknesses of direct digital signatures
- Involves use of an **arbiter A**
  - Every signed message from the sender first goes to the arbiter
  - The arbiter validates the signed message
  - Then, the arbiter dates and sends it to the recipient
- Requires suitable level of trust in arbiter
- Can be implemented with either private or public-key algorithms



# Arbitrated Digital Signatures

## (a) Conventional Encryption, Arbiter Sees Message

(1)  $X \rightarrow A: M \parallel E_{K_{xa}}[ID_X \parallel H(M)]$  signature

(2)  $A \rightarrow Y: E_{K_{ay}}[ID_X \parallel M \parallel E_{K_{xa}}[ID_X \parallel H(M)] \parallel T]$

- Arbiter sees the message
  - Any eavesdropper can see the message
- Y cannot directly check the signature of X
- In the future disputes between X and Y, Y can present the signature received from the arbiter
- X and Y trust A such that A never releases the secrecy of  $K_{xa}$  and  $K_{ay}$



# Arbitrated Digital Signatures

## (b) Conventional Encryption, Arbiter Does Not See Message

(1)  $X \rightarrow A: ID_X \parallel E_{K_{xy}}[M] \parallel E_{K_{xa}}[ID_X \parallel H(E_{K_{xy}}[M])]$  signature

(2)  $A \rightarrow Y: E_{K_{ay}}[ID_X \parallel E_{K_{xy}}[M] \parallel E_{K_{xa}}[ID_X \parallel H(E_{K_{xy}}[M])] \parallel T]$

- Arbiter cannot see the message
  - Provide confidentiality by using secret key  $K_{xy}$  between X and Y
- The rest is the same as the previous approach
- Problems
  - The arbiter could deny a signed message in alliance with the sender
  - The arbiter could forge the sender's signature in alliance with the receiver



# Arbitrated Digital Signatures

## (c) Public-Key Encryption, Arbiter Does Not See Message

(1)  $X \rightarrow A: ID_X \parallel E_{KR_x} [ID_X \parallel E_{KU_y} (E_{KR_x} [M])]$  signature

(2)  $A \rightarrow Y: E_{KR_a} [ID_X \parallel E_{KU_y} [E_{KR_x} [M]] \parallel T]$

- X double encrypts a message M with X's private key,  $KU_x$ , and Y's public key,  $KU_y$
- Could solve the previous problems



# Authentication Protocols

- Used to convince parties of each others identity and to exchange session keys
- May be one-way or mutual
- Key issues are
  - **Confidentiality** – to protect session keys and to prevent masquerade
  - **Timeliness** – to prevent replay attacks



# Types of Replay Attacks

- Where a valid signed message is copied and later resent
  - Simple replay
  - Repetition that can be logged
    - Replay a timestamped messages within the valid time window
  - Repetition that cannot be detected
    - The original message is suppressed and only the replay message arrives at the destination
  - Backward replay without modification
    - Reply back to the sender
    - Possible if symmetric encryption is used and the sender cannot easily recognize the difference between the sent message and the received message



# Counter Replay Attacks

- Countermeasures include
  - Use of sequence numbers
    - Keep track of the last sequence number
    - Associated overhead
    - Generally impractical
  - Timestamps
    - Needs synchronized clocks
    - Accept a message as fresh only if the message contains a timestamp that is close enough to A's knowledge of current time
  - Challenge/response
    - Using unique nonce (challenge)
    - Receiver first sends a nonce to the sender and requires the sender to use the correct nonce value (response)



# Using Symmetric Encryption

- As discussed previously can use a two-level hierarchy of keys
- Usually with a trusted Key Distribution Center (KDC)
  - Each party shares own master key with KDC
  - KDC generates session keys used for connections between parties
  - Master keys used to distribute these to them



# Needham-Schroeder Protocol

- Original third-party key distribution protocol
- For session between A B mediated by KDC
- protocol overview is:

1. A→KDC:  $ID_A \parallel ID_B \parallel N_1$
2. KDC→A:  $E_{Ka}[Ks] \parallel ID_B \parallel N_1 \parallel [E_{Kb}[Ks] \parallel ID_A]$
3. A→B:  $E_{Kb}[Ks] \parallel ID_A$
4. B→A:  $E_{Ks}[N_2]$
5. A→B:  $E_{Ks}[f(N_2)]$



# Needham-Schroeder Protocol

- Used to securely distribute a new session key for communications between A & B
- But is vulnerable to a **replay attack** if an old session key has been compromised
  - Then message 3 can be resent convincing B that is communicating with A
  - The opponent doesn't know  $K_a$  and  $K_b$  but simply replays it
- Modifications to address this require:
  - Timestamps (Denning 81)
  - Using an extra nonce (Neuman 93)



# Denning's Protocol

- Protocol overview is:

1. A→KDC:  $ID_A \parallel ID_B$
2. KDC→A:  $E_{Ka}[Ks \parallel ID_B \parallel T] \parallel E_{Kb}[Ks \parallel ID_A \parallel T]$
3. A→B:  $E_{Kb}[Ks \parallel ID_A \parallel T]$
4. B→A:  $E_{Ks}[N_1]$
5. A→B:  $E_{Ks}[f(N_1)]$

- A and B can verify timeliness by checking

$$|Clock - T| < \Delta t_1 + \Delta t_2$$

$\Delta t_1$  : estimated normal discrepancy between the KDC's clock and the local clocks

$\Delta t_2$  : expected network delay time

- Replying an old session can be verified at Step 3



# Denning's Protocol

- Suppressed replay attacks
  - Sabotage or faults in the clocks of the synchronization of the clocks
  - If the sender's clock is ahead of the intended recipient's clock, then the message can be intercepted and replayed later as if it's current
  - (Solution) Clocks need resynchronization regularly



# Improved Protocol

- Protocol overview is:

1. A→B:  $ID_A || N_a$
2. B→KDC:  $ID_B || N_b || E_{Kb}[ID_A || N_a || T_b]$
3. KDC→A:  $E_{Ka}[ID_B || N_a || K_s || T_b] || E_{Kb}[ID_A || K_s || T_b] || N_b$
4. A→B:  $E_{Kb}[ID_A || K_s || T_b] || E_{Ks}[N_b]$

- Handshaking protocol

- Alternative to avoid clock resynchronization for suppress-replay attack
- Use of nonces for handshaking
  - Nounce  $N_a$  is returned back to A
  - Nounce  $N_b$  is also returned back to B
  - Therefore, they don't need to synchronize the clock



# Using Public-Key Encryption

- Have a range of approaches based on the use of public-key encryption
- Need to ensure that both parties have the correct public keys for the other party
- Using a central Authentication Server (AS)
  - Provides public key certificates
- Various protocols exist using timestamps or nonces



# Denning AS Protocol

## ■ Assumption

- A and B don't have each other's public key
- AS has the public keys

## ■ Denning presented the following:

1. A→AS:  $ID_A \parallel ID_B$
2. AS→A:  $E_{KRas}[ID_A \parallel KU_a \parallel T] \parallel E_{KRas}[ID_B \parallel KU_b \parallel T]$
3. A→B:  $E_{KRas}[ID_A \parallel KU_a \parallel T] \parallel E_{KRas}[ID_B \parallel KU_b \parallel T] \parallel E_{KU_b}[E_{KRa}[K_s \parallel T]]$

- Note session key is chosen by A, hence AS need not be trusted to protect it
- **Timestamps** prevent replay but require synchronized clocks
  - Look at T in each step: to use the same T, A and B must have the **synchronized clock**



# One-Way Authentication

- The sender and the receiver need not be on-line at same time (eg. email)
- Have the E-mail header in clear so can be delivered by email system
- May want contents of body protected by encryption and sender authenticated



# One Way Authentication : Using Symmetric Encryption

- Can refine use of KDC but can't have final exchange of nonces: so that B doesn't have to be on-line
  1. A→KDC:  $ID_A \parallel ID_B \parallel N_1$
  2. KDC→A:  $E_{Ka}[Ks \parallel ID_B \parallel N_1 \parallel E_{Kb}[Ks] \parallel ID_A]$
  3. A→B:  $E_{Kb}[Ks] \parallel ID_A \parallel E_{Ks}[M]$
- Does not protect against replays
  - Could rely on timestamp in message, though email delays make this problematic



# One Way Authentication : Public-Key Approaches

- Have seen some public-key approaches
- If confidentiality is major concern, can use:  
$$A \rightarrow B: E_{KUb}[Ks] \parallel E_{Ks}[M]$$
  - Has encrypted session key, encrypted message
- If authentication needed use a digital signature with a digital certificate:  
$$A \rightarrow B: M \parallel E_{KRa}[H(M)] \parallel E_{KRas}[T \parallel ID_A \parallel KU_a]$$
  - with message, signature, certificate



# Digital Signature Standard (DSS)

- US Govt approved signature scheme FIPS 186
- Uses the **SHA** hash algorithm
- Designed by NIST & NSA in early 90's
- DSS is the standard, DSA is the algorithm
- Creates a 320 bit signature, but with 512-1024 bit security
- Security depends on difficulty of computing discrete logarithms



# Mathematical Background

## ■ A primitive prime root of a prime number

- $q$  : a prime number
- $a$  : a primitive prime root of  $q$
- $a \bmod q, a^2 \bmod q, a^3 \bmod q, \dots, a^{q-1} \bmod q$
- Successive powers of  $a$  can generate all the numbers between 1 and  $p-1$  such that  $a^i \bmod q$ , where  $1 \leq i \leq q-1$ , will be distinct and consists of the integers 1 to  $q-1$ .

## ■ Discrete logarithm

- For any integer  $b$  less than  $q$  and a prime root  $a$  of prime number  $q$ , we can find a unique exponent  $i$  such that  $b = a^i \bmod q$  where  $1 \leq i \leq q-1$   
exponent  $i$  is the **discrete logarithm** of  $b$  for the base  $a$  and  $\bmod q$



# DSA Key Generation

- Have shared global public key values (p,q,g):
  - a large prime  $2^{L-1} < p < 2^L$ 
    - where  $512 \leq L \leq 1024$  bits and is a multiple of 64
  - choose q, a 160 bit prime divisor of p-1
    - $2^{159} < q < 2^{160}$
  - choose  $g = h^{(p-1)/q} \pmod{p}$ 
    - where  $1 < h < p-1$ ,  $h^{(p-1)/q} \pmod{p} > 1$
- Users choose private & compute public key:
  - choose  $0 < x < q$
  - compute  $y = g^x \pmod{p}$
  - It is computationally infeasible to determine x, which is the discrete logarithm of y to the base g, mod p



# DSA Signature Creation

- To **sign** a message  $M$  the sender:
  - generates a random signature key  $k$ ,  $k < q$
  - nb.  $k$  must be random, be destroyed after use, and never be reused
- then computes signature pair:
$$r = (g^k \pmod p) \pmod q$$
$$s = (k^{-1} \cdot \text{SHA}(M) + x \cdot r) \pmod q$$
- sends signature  $(r, s)$  with message  $M$



# DSA Signature Verification

- Having received  $M$  & signature  $(r, s)$
- to **verify** a signature, recipient computes:

$$w = s^{-1} \pmod{q}$$

$$u_1 = (\text{SHA}(M) \cdot w) \pmod{q}$$

$$u_2 = (r \cdot w) \pmod{q}$$

$$v = (g^{u_1} \cdot y^{u_2} \pmod{p}) \pmod{q}$$

- if  $v=r$  then signature is verified
- see book web site for details of proof why



# Summary

- have considered:
  - digital signatures
  - authentication protocols (mutual & one-way)
  - digital signature standard

