

Data from an unknown function $y = f(x)$ is shown in the table below.

x	y
0	1
1	2
2	5
3	8

1. The equation $\hat{y} = 2x + 1$ is being used for interpolation of the function. The sum of the squares of the errors $e_i = y_i - \hat{y}_i$, $i = 1, 2, 3, 4$ is (3pts)

- a) 0 b) 2 c) 1.5 d) 4 e) 1.8 f) none of the above

$$\hat{y} = 1 \quad 3 \quad 5 \quad 7$$

$$e = 0 \quad -1 \quad 0 \quad 1$$

$$esq = 0 \quad 1 \quad 0 \quad 1$$

$$\text{sum_esq} = 2$$

2. The Least Squares line thru the data points is $\hat{y} = a_0 + a_1 x$ where (4 pts)

- a) $a_0 = 1, a_1 = 2$ b) $a_0 = 0.8, a_1 = 2.1$ c) $a_0 = 1.5, a_1 = 2.5$
d) $a_0 = 0.75, a_1 = 2.5$ e) $a_0 = 0.4, a_1 = 2.4$ f) none of the above

$$A =$$

$$\begin{matrix} 4 & 6 \\ 6 & 14 \end{matrix}$$

$$b = 16 \quad 36$$

$$a =$$

$$\begin{matrix} 0.4000 \\ 2.4000 \end{matrix}$$

3. SST and SSE for the Least Squares line are (3 pts)

- a) SST=30, SSE=1.2
- b) SST=18, SSE=2.4
- c) SST=24, SSE=1.5
- d) SST=36, SSE=3.0
- e) SST=10, SSE=1.1
- f) none of the above

$$\hat{y} = 0.4000 \quad 2.8000 \quad 5.2000 \quad 7.6000$$

$$e = 0.6000 \quad -0.8000 \quad -0.2000 \quad 0.4000$$

$$SSE = 1.2000$$

$$\bar{y} = 4$$

$$SST = 30$$

4. The correlation coefficient r is (2 pts)

- a) 0.9798
- b) 0.8667
- c) 0.9375
- d) 0.9167
- e) 0.8915
- f) 1
- g) none of the above

$$SSR = 28.8000$$

$$r = 0.9798$$

5. Using the Least Squares Line to predict the value of y when $x=1.5$ results in (3 pts)

- a) $y=3$
- b) $y=2.5$
- c) $y=4$
- d) $y=4.5$
- e) $y=3.5$
- f) none of the above

$$y = 4.0000$$