University of Central Florida

Department of Electrical Engineering and Computer Science COT 4500 Numerical Calculus Quiz 3 - Take home quiz (Due 3/25/2013)

For all exercises show all your work step by step.

1.- Find the invers of matrix A using determinant and cofactors.(20 points)

$$\mathbf{A} = \begin{bmatrix} 1 & 2 & 0 \\ 2 & 1 & -1 \\ 3 & 1 & -1 \end{bmatrix}$$

2.- Factor the following matrix into the LU decomposition using LU factorization.(20 points)

$$A = \begin{bmatrix} 2 & -1 & 1 \\ 3 & 3 & 9 \\ 3 & 3 & 5 \end{bmatrix}$$

3.- Solve the following linear system of equations, making use of the LU-factorization of the preceding coefficient matrix.(20 points)

$$2x_1 - x_2 + x_3 = -1 3x_1 + 3x_2 + 9x_3 = 0 3x_1 + 3x_2 + 5x_3 = 4$$

4.- Determine whether the matrix A is positive definite using Sylvester's criterion. (20 points)

$$\mathbf{A} = \begin{bmatrix} 1 & -1 & 0 \\ -1 & 4 & 2 \\ 0 & 2 & 2 \end{bmatrix}$$

5.- Use Cholesky's factorization to find a factorization of the form $A = LL^T$ for the following matrix: (20 points)

$$\mathbf{A} = \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$$

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