

Assignment # 10.1 Key

1. Recast the decision problem for the Boolean expression $(a + b + \sim c)(\sim a + b + b)(a + \sim b + c)$ as a SubsetSum problem using the construction discussed in class. Indicate what rows would need to be chosen for a solution.

	<i>a</i>	<i>b</i>	<i>c</i>	<i>a + b + ~c</i>	<i>~a + b + b</i>	<i>a + ~b + c</i>
<i>a</i>	1	0	0	1	0	1
<i>~a</i>	1	0	0	0	1	0
<i>b</i>	0	1	0	1	2	0
<i>~b</i>	0	1	0	0	0	1
<i>c</i>	0	0	1	0	0	1
<i>~c</i>	0	0	1	1	0	0
<i>C1</i>	0	0	0	1	0	0
<i>C1'</i>	0	0	0	1	0	0
<i>C2</i>	0	0	0	0	1	0
<i>C2'</i>	0	0	0	0	1	0
<i>C3</i>	0	0	0	0	0	1
<i>C3'</i>	0	0	0	0	0	1
	1	1	1	3	3	3

Assignment # 10.2 Key

2. Recast the SubsetSum problem $\{15, 7, 12, 4, 11, 6, 4, 12, 3, 2\}$, $G=39$ as a Partition Problem using the construction discussed in class. Indicate what values would need to be chosen to equal 39. Indicate the partitions that evenly divide the Partition Problem you posed

$$\{15, 7, 12, 4, 11, 6, 4, 12, 3, 2\} \quad 15+7+12+3+2 = 39$$

$$\{15, 7, 12, 4, 11, 6, 4, 12, 3, 2, 113, 115\}$$

$$\text{Can partition as } \{15, 7, 12, 3, 2, 113\} = 152;$$
$$\{4, 11, 6, 4, 12, 115\} = 152$$

Assignment # 10.3 Key

3. Recast the decision problem for the Boolean expression $(a + b + \sim c + d)(\sim a + b + \sim d)(a + \sim b + c)$ as a 0,1-Integer Linear Programming problem using the construction discussed in class. Indicate what binary (0,1) values of a , b , c and d give rise to a solution to the Integer Linear Programming problem you posed.

$$0 \leq a \leq 1; 0 \leq b \leq 1; 0 \leq c \leq 1; 0 \leq d \leq 1$$

$$a + b + (1-c) + d \geq 1$$

$$(1-a) + b + (1-d) \geq 1$$

$$a + (1-b) + c \geq 1$$

Solution: $a = 1; b = 1; c = 1; d$ either 0 or 1 – Lots of other solutions