

Assignment # 10.1 Key

1. Recast the decision problem for the Boolean expression $(a+d)(a+\sim b+c)(b+\sim d)$ as a SubsetSum problem using the construction discussed in class. Indicate what rows would need to be chosen for a solution.

	a	b	c	d	$a+d+d$	$a+\sim b+c$	$b+b+\sim d$
a	1	0	0	0	1	1	0
$\sim a$	1	0	0	0	0	0	0
b	0	1	0	0	0	0	2
$\sim b$	0	1	0	0	0	1	0
c	0	0	1	0	0	1	0
$\sim c$	0	0	1	0	0	0	0
d	0	0	1	1	2	0	0
$\sim d$	0	0	1	1	0	0	0
$C1$	0	0	0	1	1	0	1
$C1'$	0	0	0	0	1	0	0
$C2$	0	0	0	0	0	1	0
$C2'$	0	0	0	0	0	0	0
$C3$	0	0	0	0	0	0	1
$C3'$	0	0	0	0	0	0	1
	1	1	1	1	3	3	3

Assignment # 10.2 Key

2. Recast the SubsetSum problem $\{14, 7, 20, 11, 4, 13, 15, 18\}$, $G=43$ as a Partition Problem using the construction discussed in class. Indicate what values would need to be chosen to equal 43. Indicate the partitions that evenly divide the Partition Problem you posed

$\{14, 7, 20, 11, 4, 13, 15, 18\}$ $14+7+4+18 = 43$

$\{14, 7, 20, 11, 4, 13, 15, 18, 161, 145\}$

Can partition as $\{14, 7, 4, 18, 161\} = 204$;
 $\{20, 11, 13, 15, 145\} = 204$

Assignment # 10.3 Key

3. Recast the decision problem for the Boolean expression $(a+d)(a+\sim b+c+\sim d)(\sim b+\sim c+d)$ as a 0,1-Integer Linear Programming problem using the construction discussed in class. Indicate what binary (0,1) values of a , b , c and d give rise to a solution to the Integer Linear Programming problem you posed.

$$0 \leq a \leq 1; 0 \leq b \leq 1; 0 \leq c \leq 1; 0 \leq d \leq 1$$

$$a + d \geq 1$$

$$a + (1-b) + c + (1-d) \geq 1$$

$$(1-b) + (1-c) + d \geq 1$$

Solution: $a = 1; b = 1; c = 1; d = 1$ – Lots of other solutions