Assignment # 7.1 Sample

1. For the following languges, either provide a grammar to show it is a CFL or employ the Pumping Lemma to show it is not
   a.) **$L = \{ a^i b^j \mid j > 2*I \}$**

   b.) **$L = \{ a^n b^{n!} \mid n>0 \}$**

Assignment # 7.2 Sample

2. Consider the context-free grammar **G = ({ S } , { a , b } , S , P),** where **P** is:

   S $\rightarrow$ **S a S b S | S b S a S | S a S a S | a |** λ

   Provide the first part of the proof that

   L (G) = L = { w | w has at least as many **a's** as **b's }**

   That is, show that **L (G)** $\subseteq$ **L**

   To attack this problem we can first introduce the notation that, for a syntactic form α, α_a = the number of **a's** in α, and α_b = the number of **b's** in α. Using this, we show that if **S** $\Rightarrow* \alpha$, then $\alpha_b \leq \alpha_a$ and hence that **L (G)** $\subseteq$ **L:**

   A straightforward approach is to show, inductively on the number of steps, **i**, in a derivation, that, if **S** $\Rightarrow^{i} \alpha$, then $\alpha_b \leq \alpha_a$.