

Assignment # 10.1 Key

- Recast the decision problem for the Boolean expression $(a + b + \sim c)(\sim a + b + b)(a + \sim b + c)$ as a SubsetSum problem using the construction discussed in class. Indicate what rows would need to be chosen for a solution.

	a	b	c	$a + b + c$	$\sim a + \sim b + \sim c$	$a + \sim b + \sim c$
a	1	0	0	1	0	1
$\sim a$	1	0	0	0	1	0
b	0	1	0	1	0	0
$\sim b$	0	1	0	0	1	1
c	0	0	1	1	0	0
$\sim c$	0	0	1	0	1	1
$C1$	0	0	0	1	0	0
$C1'$	0	0	0	1	0	0
$C2$	0	0	0	0	1	0
$C2'$	0	0	0	0	1	0
$C3$	0	0	0	0	0	1
$C3'$	0	0	0	0	0	1
	1	1	1	3	3	3

Assignment # 10.2 Key

2. Recast the SubsetSum problem [(17, 27, 11, 2, 7, 3, 22), G=39] as a Partition Problem using the construction discussed in class. Indicate what values would need to be chosen to equal 39. Indicate the partitions that evenly divide the Partition Problem you posed

$\{17, 27, 11, 2, 7, 3, 22\}$ $17+22 = 39$

$\{17, 27, 11, 2, 7, 3, 22, 139, 128\}$

**Can partition as $\{17, 22, 139\} = 178$;
 $\{27, 11, 2, 7, 3, 128\} = 178$**

Assignment # 10.3 Key

3. Recast the decision problem for the Boolean expression $(a+b+c)(\sim a+\sim b+\sim c)(a+\sim b+\sim c)$ as a 0,1-Integer Linear Programming Problem using the construction discussed in class. Indicate what binary (0,1) values of a , b , c and d give rise to a solution to the Integer Linear Programming problem you posed.

$$0 \leq a \leq 1; 0 \leq b \leq 1; 0 \leq c \leq 1$$

$$a + b + c \geq 1$$

$$(1-a) + (1-b) + (1-c) \geq 1$$

$$a + (1-b) + (1-c) \geq 1$$

Solution: $a = 1; b = 0; c = 0$ – Lots of other solutions