

Assignment # 10.1 Key

- Recast the decision problem for the Boolean expression $(a + b)(a + \sim b + c)(\sim b)$ as a SubsetSum problem using the construction discussed in class.

| | a | b | c | $a + b + b$ | $a + \sim b + c$ | $\sim b + \sim b + \sim b$ |
|----------|-----|-----|-----|-------------|------------------|----------------------------|
| a | 1 | 0 | 0 | 1 | 1 | 0 |
| $\sim a$ | 1 | 0 | 0 | 0 | 0 | 0 |
| b | 0 | 1 | 0 | 2 | 0 | 0 |
| $\sim b$ | 0 | 1 | 0 | 0 | 1 | 3 |
| c | 0 | 0 | 1 | 0 | 1 | 0 |
| $\sim c$ | 0 | 0 | 1 | 0 | 0 | 0 |
| $C1$ | 0 | 0 | 0 | 1 | 0 | 0 |
| $C1'$ | 0 | 0 | 0 | 1 | 0 | 0 |
| $C2$ | 0 | 0 | 0 | 0 | 1 | 0 |
| $C2'$ | 0 | 0 | 0 | 0 | 1 | 0 |
| $C3$ | 0 | 0 | 0 | 0 | 0 | 1 |
| $C3'$ | 0 | 0 | 0 | 0 | 0 | 1 |
| | 1 | 1 | 1 | 3 | 3 | 3 |

Assignment # 10.2 Key

2. Recast the SubsetSum problem $(8, 7, 6, 4, 6, 8, 2, 7, 2)$, $G=19$ as a Partition Problem using the construction discussed in class.

$(8, 7, 6, 4, 6, 8, 2, 7, 2, 81, 69)$

Can partition as $(8, 7, 4, 81) = 100$; $(6, 6, 8, 2, 7, 2, 69) = 100$

Assignment # 10.3 Key

3. Recast the decision problem for the Boolean expression $(a + b) (a + \sim b + c) (\sim b)$ as an Integer Linear Programming problem using the construction discussed in class.

$$0 \leq a \leq 1; 0 \leq b \leq 1; 0 \leq c \leq 1;$$

$$a + b \geq 1$$

$$a + (1-b) + c \geq 1$$

$$(1-b) \geq 1$$

Solution: $a = 1; b = 0; c = 1$ (or 0)