

Laws of Logic

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| 1. | $\neg\neg p \leftrightarrow p$ | Law of Double Negation |
| 2. | $\neg(p \vee q) \leftrightarrow \neg p \wedge \neg q$
$\neg(p \wedge q) \leftrightarrow \neg p \vee \neg q$ | DeMorgan's Law |
| 3. | $p \vee q \leftrightarrow q \vee p$
$p \wedge q \leftrightarrow q \wedge p$ | Commutative Laws |
| 4. | $p \vee (q \vee r) \leftrightarrow (p \vee q) \vee r$
$p \wedge (q \wedge r) \leftrightarrow (p \wedge q) \wedge r$ | Associative Laws |
| 5. | $p \vee (q \wedge r) \leftrightarrow (p \vee q) \wedge (p \vee r)$
$p \wedge (q \vee r) \leftrightarrow (p \wedge q) \vee (p \wedge r)$ | Distributive Laws |
| 6. | $p \vee p \leftrightarrow p$
$p \wedge p \leftrightarrow p$ | Idempotent Laws |
| 7. | $p \vee F \leftrightarrow p$
$p \wedge T \leftrightarrow p$ | Identity Laws |
| 8. | $p \vee \neg p \leftrightarrow T$
$p \wedge \neg p \leftrightarrow F$ | Inverse Laws |
| 9. | $p \vee T \leftrightarrow T$
$p \wedge F \leftrightarrow F$ | Domination Laws |
| 10. | $p \vee (p \wedge q) \leftrightarrow p$
$p \wedge (p \vee q) \leftrightarrow p$ | Absorption Laws |
| 11. | $(p \rightarrow q) \leftrightarrow (\bar{p} \vee q)$ | Implication Identity |
| 12. | $(p \rightarrow q) \leftrightarrow (\bar{q} \rightarrow \bar{p})$ | Contrapositive |

Laws of Set Theory

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| 1. | $\bar{\bar{A}} = A$ | Law of Double Negation |
| 2. | $\overline{A \cup B} = \bar{A} \cap \bar{B}$
$\overline{A \cap B} = \bar{A} \cup \bar{B}$ | DeMorgan's Laws |
| 3. | $A \cup B = B \cup A$
$A \cap B = B \cap A$ | Commutative Laws |
| 4. | $A \cup (B \cup C) = (A \cup B) \cup C$
$A \cap (B \cap C) = (A \cap B) \cap C$ | Associative Laws |
| 5. | $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$
$A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$ | Distributive Laws |
| 6. | $A \cup A = A$
$A \cap A = A$ | Idempotent Laws |
| 7. | $A \cup \emptyset = A$
$A \cap \mathcal{U} = A$ | Identity Laws |
| 8. | $A \cup \bar{A} = \mathcal{U}$
$A \cap \bar{A} = \emptyset$ | Inverse Laws |
| 9. | $A \cup \mathcal{U} = \mathcal{U}$
$A \cap \emptyset = \emptyset$ | Domination Laws |
| 10. | $A \cup (A \cap B) = A$
$A \cap (A \cup B) = A$ | Absorption Laws |

Rules of Inference

1. $[p \wedge (p \rightarrow q)] \rightarrow q$ Rule of Detachment (Modus Ponens)
2. $[(p \rightarrow q) \wedge (q \rightarrow r)] \rightarrow (p \rightarrow r)$ Law of Syllogism
3. $[(p \rightarrow q) \wedge \neg q] \rightarrow \neg p$ Modus Tollens
4. $[(p) \wedge (q)] \rightarrow p \wedge q$ Rule of Conjunction
5. $[(p \vee q) \wedge \neg p] \rightarrow q$ Rule of Disjunctive Syllogism
6. $(\neg p \rightarrow F) \rightarrow p$ Rule of Contradiction
7. $(p \wedge q) \rightarrow p$ Rule of Conjunctive Simplification
8. $p \rightarrow (p \vee q)$ Rule of Disjunctive Amplification
9. $[(p \wedge q) \wedge [p \rightarrow (q \rightarrow r)]] \rightarrow r$ Rule of Conditional Proof
10. $[(p \rightarrow r) \wedge (q \rightarrow r)] \rightarrow [(p \vee q) \rightarrow r]$ Rule for Proof by Cases
11. $[(p \rightarrow q) \wedge (r \rightarrow s) \wedge (p \vee r)] \rightarrow (q \vee s)$ Rule of the Constructive Dilemma
12. $[(p \rightarrow q) \wedge (r \rightarrow s) \wedge (\neg q \vee \neg s)] \rightarrow (\neg p \vee \neg r)$ Rule of the Destructive Dilemma

Sequence and Series Terms and Sums

Arithmetic Sequences: $a_n = a_1 + (n - 1)d$, $a_j = a_i + (j - i)d$, $S_n = \frac{(a_1 + a_n)n}{2}$

Geometric Sequences: $a_n = a_1 r^{n-1}$, $a_j = a_i r^{j-i}$, $S_n = \frac{a_1(1-r^n)}{1-r}$, $r \neq 1$, $S_\infty = \frac{a_1}{1-r}$, $|r| < 1$

Sum Formulas: $\sum_{i=1}^n c = cn$, $\sum_{i=1}^n i = \frac{n(n+1)}{2}$, $\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$, $\sum_{i=1}^n i^3 = \frac{n^2(n+1)^2}{4}$