1. (25 pts) Modify Dijkstra’s algorithm so that it checks if a given directed graph $G = (V,E)$ has a cycle. Give the pseudocode and analyze the performance.

2. (25 pts) Assume that for a given weighted directed graph $G = (V,E)$, the shortest path from $s$ to any other vertex contains at most $m$ edges. Show how to modify the Bellman-Ford algorithm to take advantage of this information. Give the pseudocode.

Extra Credit (10 pts)

How can we use the output of the Floyd-Warshall algorithm to detect the presence of a negative weight cycle?