1. A palindrome is nonempty string over some alphabet that reads the same forwards and backwards. Example palindromes include civic, racecar, aibohphobia (fear of palindromes). Give an efficient dynamic programming algorithm to find the longest palindrome that is a subsequence of a given input string. For example, given the input string character, your algorithm would return carac. Another example is the input string BBABCBCAB. Your algorithm would return BABCBA. (Hint: Use the approach taken to solve the longest common subsequence to help formulate your solution).

You should devise your solution into 5 parts.

a.) (5 pts) Characterize a longest palindrome subsequence
b.) (5 pts) Define a recursive solution
c.) (5 pts) Compute the length of a longest palindrome subsequence (Give pseudocode for a function called Longest-Palindrome.
d.) (5 pts) Construct a longest palindrome subsequence (Give pseudocode for a function called Generate-LPS)
e.) (5 pts) Give the running time for your algorithm.

2. (25 pts) Implement your solution to problem 1 in Java. You should provide a listing of your code as well as example inputs and outputs to show it is working. You should test your solution on at least 10 input strings that have and do not have palindromes. Here are some examples:

Madam
Repaper
Wow
Red rum, sir, is murder
No lemon, no melon
Kanakanak
Aibohphobia
Civic
Racecar
Character
Are we not pure? “No, sir!” Panama’s moody Noriega brags. “It is garbage!” Irony dooms a man—a prisoner up to new era.