

Last time memoization

This time Bottom-up

$$f(n) = f(n-1) + f(n-2) \quad \begin{matrix} f(0) = 0 \\ f(1) = 1 \end{matrix}$$

```
int f(i) {
    if (i == 1 || i == 0) return i;

```

```
    if (memo[i] != SENT) {
        return memo[i];
    }
    memo[i] = f(i-1) + f(i-2);
    return memo[i];

```

}

Brute Force

f(6)

f(5)

f(4)

f(3)

f(2)

f(1)

f(2)

f(1)

f(0)

f(2)

f(1)

f(0)

f(1)

f(0)

f(3)

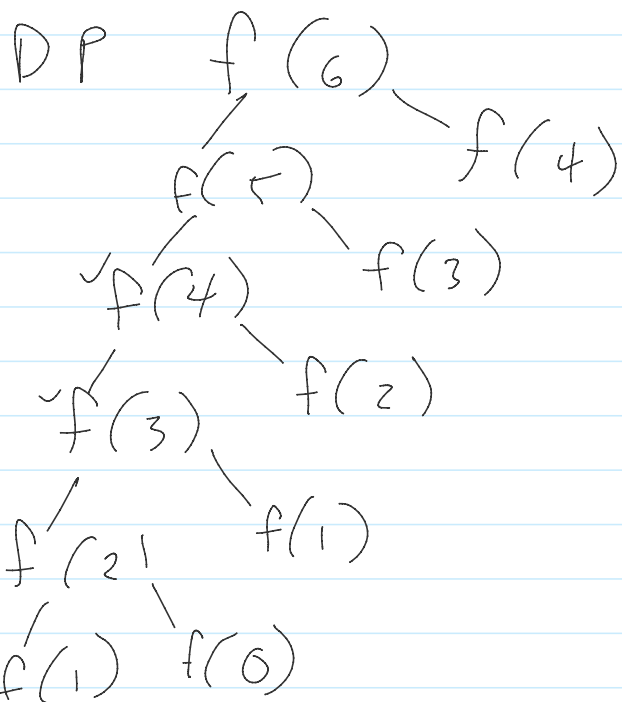
f(2)

f(1)

f(1)

f(0)

f(4)



DP Bottom up

DP Bottom up

compute $dp(i)$

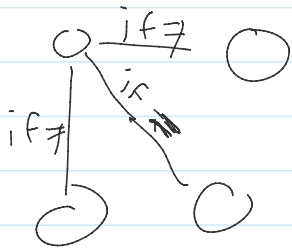
Build up the next

for $(i=2 \text{ to } n)$ $dp(i) = dp(i-1) + dp(i-2)$;

states for computation

store only necessary states
to save memory

LCS



second string

		G	C	A	T	A		" "
first string	0	G	3	-1	-1	-1	-1	0
	1	C	-1	2	-1	-1	-1	0
	2	G	-1	-1	1	1	1	0
	3	A	-1	-1	1	1	1	0
	4	" "	0	0	0	0	0	0

compute second

compute first in Bottom

i-th cell

last cell

will be the i-th to last cell visited in the recursive statement

for (int row = first string length to 1)

for (int col = second string length to 1)

compute state for row col

Shortest Path from a single source
to another (or all) other nodes

Effort

1 1 1 1

m

n

Effort

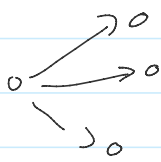
least

A* a little more efficient for single destination



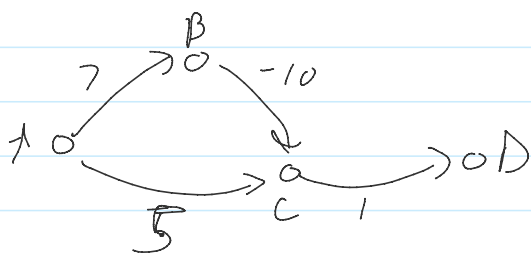
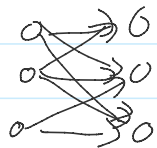
more

Dijkstra's



most

Floyd's



Adjacency Matrix

	to	A	B	C	D
From A	A	0	7	5	∞
B	A	∞	0	-10	∞
C	A	∞	∞	0	1
D	A	∞	∞	∞	0

Use A mid point

	A	B	C	D
A	0	7	5	∞
B	∞	0	-10	∞
C	∞	∞	0	1
D	∞	∞	∞	0

Use B

	A	B	C	D
A	0	7	-3	∞
B	∞	0	-10	∞
C	∞	∞	0	1
D	∞	∞	∞	0

Use C

	A	B	C	D
A	0	7	-3	-2
B	∞	0	-10	-9
C	∞	∞	0	1
D	∞	∞	∞	0

try all "mid points"

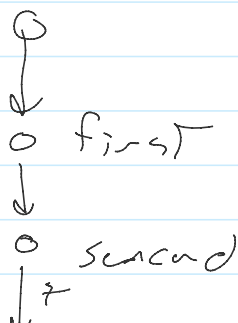
for mid point try all pairs of points

see if the pair is better off using the mid point

Class room

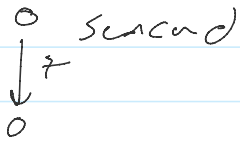
BA1 attriven

Outside



Outside

He C



Hypothetical Syllogism /

Transitivity

```
for (int i = 0; i < |V|; i++) {
  for (int f = 0; f < |V|; f++) {
    for (int s = 0; s < |V|; s++) {
      if (dist[f][s] > dist[f][i] + dist[i][s]) {
        dist[f][s] = dist[f][i] + dist[i][s];
        // build back
      }
    }
  }
}
```