① Exam 2 + Next 2 Weeks

② Stacks

③ binary trees

Stacks - Abstract Data Type

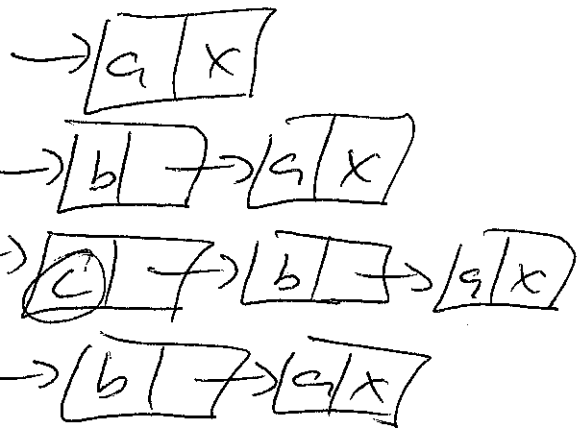
- Last In First Out
- push (puts item on top)
- pop (removes top item
- size
- top (returns top w/o removing)

d
a

① LL
② Stack

→ push - add to Front, pop - delete first front

push(a)
push(b)
push(c)
x = pop()

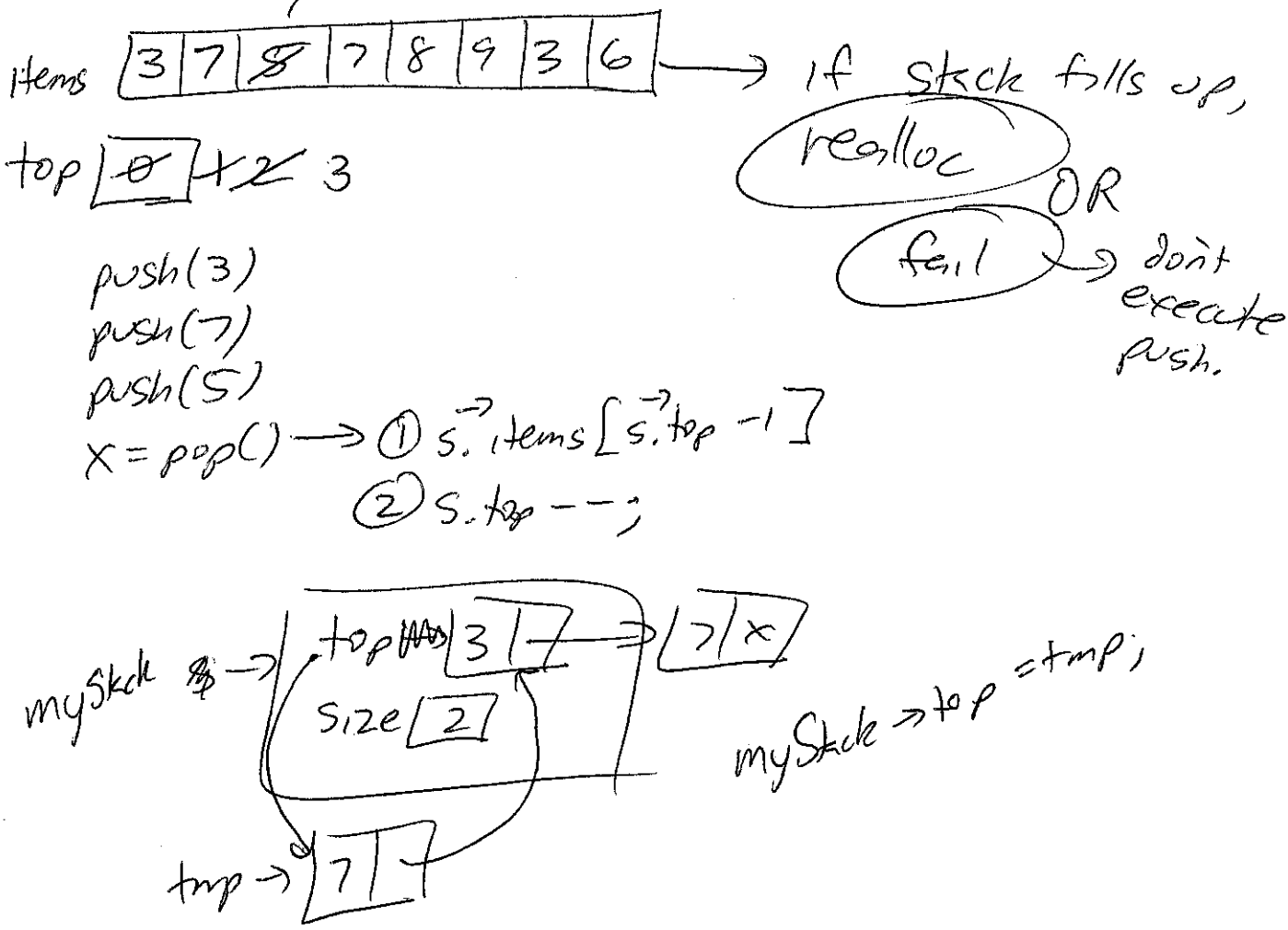



```
struct stack {
    struct node* front;
    int size;
};
```

① Call Stack

~~f(3) f(2)~~
~~f(4) f(3)~~
~~f(5)~~

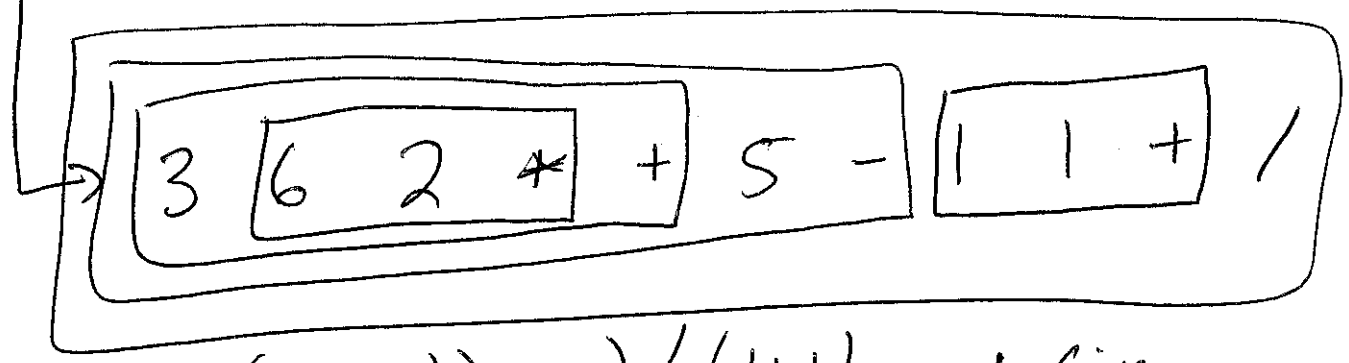
Array Implementation



Two Stack Algorithms

① Evaluating a postfix expression

② Converting infix to postfix



((3+(6*2))-5)/(1+1) Infix

(3+4)*5

Order of ops

Read expression L→R

Use a operand stack (starts empty)

① When you read an operand push it onto the stack

② When you read an operator (op), pop the last 2 items off the stack op2, followed by op1. Calculate op1 op op2. Push this value back onto the stack

⟹ If ~~your~~ ~~stack~~ you ever try to pop an empty stack, the expression is invalid. If you end up w/a stack size >1, it's also invalid.

Infix → Postfix

Stack → operator stack

$((3+6*2)-5)/(1+1)$

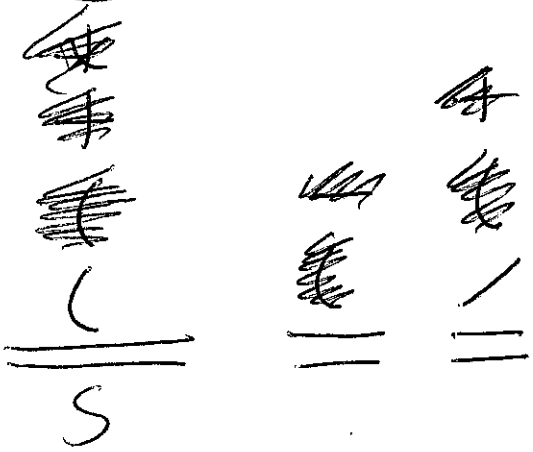
① Open paren → push onto stack

② Operand → Place into expression

③ Close paren → pop items off stack placing each in the expression until we hit the 1st open paren.

④ Operator → Pop off the stack each operator of equal OR higher precedence, placing each into the expression. Stop popping when you reach a operator of lower precedence OR a parenthesis OR the end of the stack. Push this operator onto the stack.

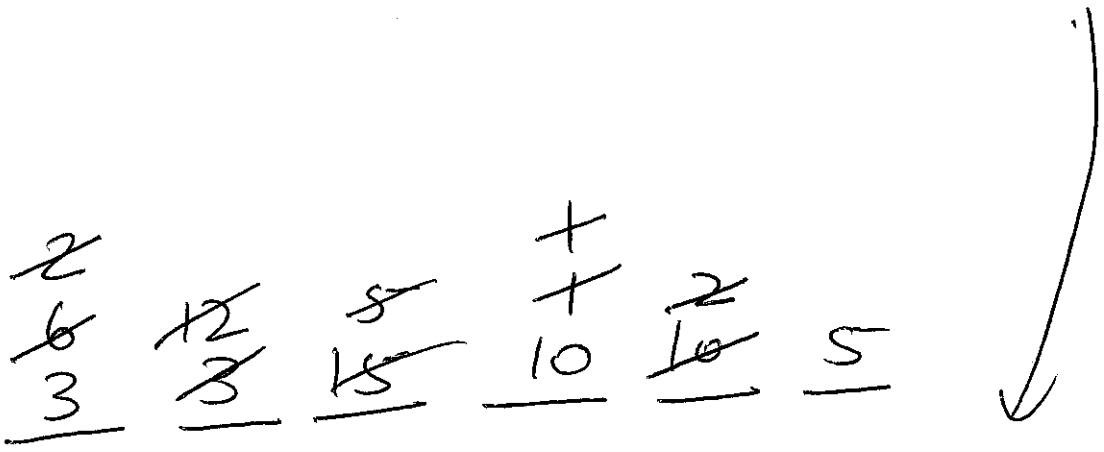
END Pop off remaining operators + place in expr.



Exp: 3 6 2 * + 5 − 1 1 + /

3/7/17 (5)

3 6 2 * + 5 - 1 1 + /



~~2~~			+		
~~6~~	~~12~~	~~5~~	+	~~2~~	
3	~~3~~	~~15~~	10	~~10~~	5

$6 * 2 = 12$

$3 + 12 = 15$

$15 - 5 = 10$

$1 + 1 = 2$

$10 / 2 = 5$

$((3+(6*2))-5)/(1+1)$

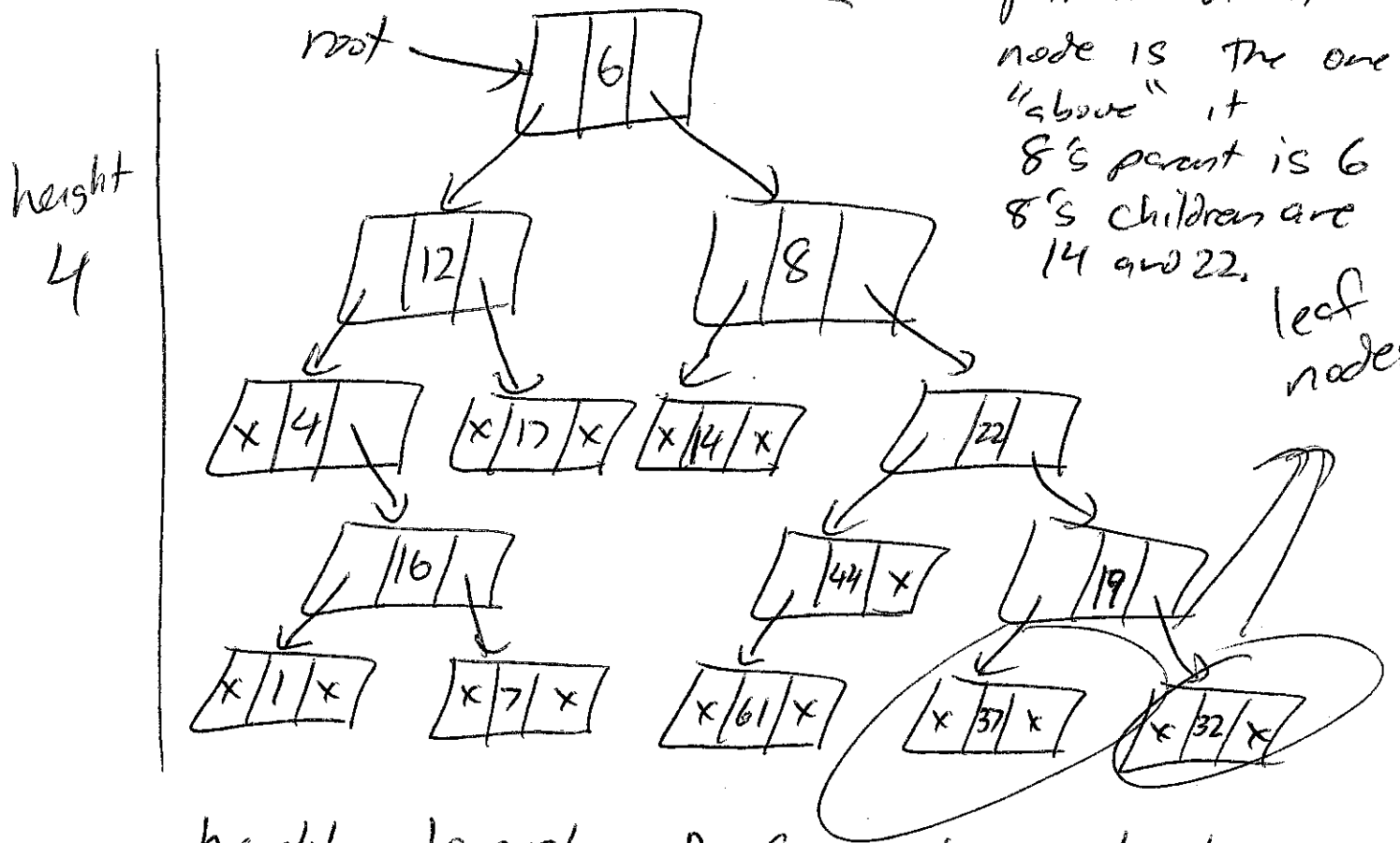
$((3+12)-5)/2$

$(15-5)/2$

$10/2$

5

Binary Trees

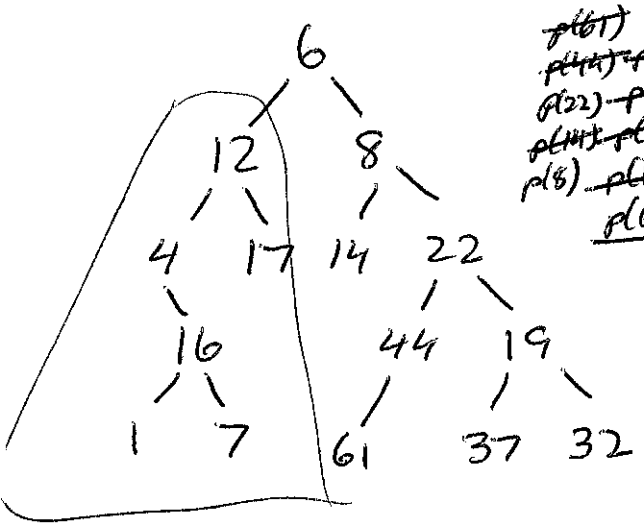


parent of a node is the one "above" it
8's parent is 6
8's children are 14 and 22.

height - longest path from the root to any leaf node

tree of 0 nodes has height -1
tree of 1 node has height 0
tree of 2 nodes has height 1

How do I traverse a tree?



~~p(6)~~
~~p(12)~~ ~~p(17)~~ ~~p(17)~~
~~p(22)~~ ~~p(16)~~
~~p(14)~~ ~~p(17)~~ ~~p(17)~~
~~p(8)~~ ~~p(12)~~
p(6)

```
typedef struct treenode {
    int data;
    struct treenode* left;
    struct treenode* right;
} treenode;
```

```
Void preorder(treenode* root) {
    if (root != NULL) {
        printf("%d ", root->data);      (1)
        preorder(root->left);           (2)
        preorder(root->right);          (3)
    }
}
```

6, 12, 4, 16, 1, 7, 17,
8, 14, 22, 44, 61, 19,
37, 32

```
void inorder(treenode* root) {
    if (root != NULL) {
        inorder(root->left);
        printf("%d ", root->data);
        inorder(root->right);
    }
}
```

4, 1, 16, 7, 12, 17, 6
14, 8, 61, 44, 22, 37, 19, 32

```
void postorder(treenode* root) {
    if (root != NULL) {
        postorder(root->left);
        postorder(root->right);
        printf("%d ", root->data);
    }
}
```

1, 7, 16, 4, 17, 12, 14
61, 44, 37, 32, 19, 22,
8, 6

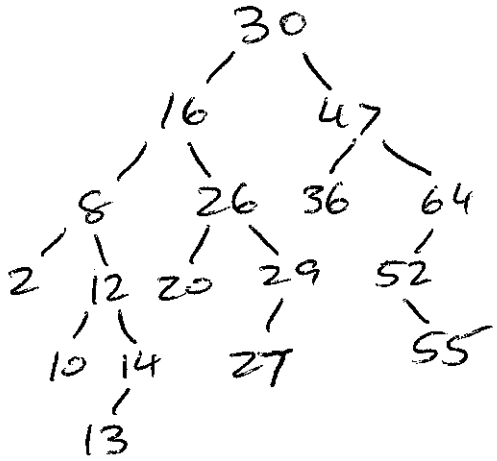
Couple Example Functions on binary trees

(1) Sum of all leaf nodes in a binary tree

```
int sumleaf(treenode* root) {
    if (root == NULL) return 0;
    if (root->left == NULL &&
        root->right == NULL) return root->data;
    return sumleaf(root->left) + sumleaf(root->right);
}
```

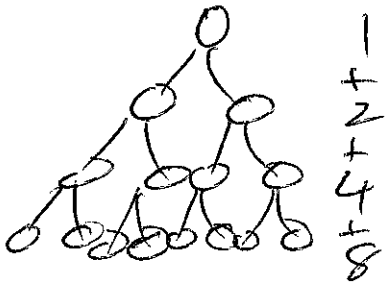
(2) height of a tree

```
int height(treenode* root) {
    if (root == NULL) return -1;
    int lheight = height(root->left);
    int rheight = height(root->right);
    if (lheight > rheight)
        return 1 + lheight;
    return 1 + rheight;
}
```



Binary Search Tree
→ BST property: for any node, all values in its left subtree are less than it, all values in the right are greater than it.

Runtimes of each traversal are $O(n)$ for a tree of n nodes.



A search in a Binary Search Tree takes $O(h)$ time, where h = height of the tree.
→ h is the worst case is $O(n)$.
→ h in the best case is $O(\lg n)$.
→ h is the avg case in $O(\lg n)$.

$1+2+4+8 \cdots +2^k = 2^{k+1} - 1$

let $n = 2^{k+1} - 1$

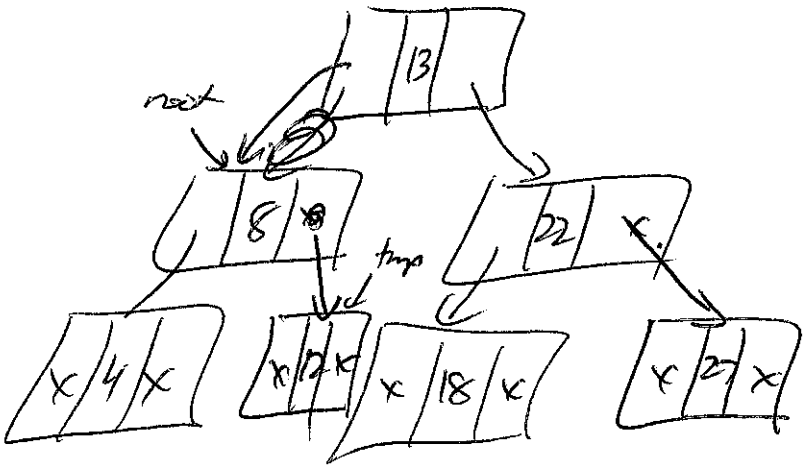
$n+1 = 2^{k+1}$

$\log_2(n+1) = k+1$

$k = \log_2(n+1) - 1 = O(\lg n)$

```
int search(treenode* root, int searchval) {
    if (root == NULL) return 0;
    if (searchval < root->data)
        return search(root->left, searchval);
    else if (searchval > root->data)
        return search(root->right, searchval);
    return 1;
}
```

Inserting into a BST




```
treenode* insertrec (treenode* root, int value) {
    if (root == NULL) {
        treenode* tmp = malloc(sizeof(treenode));
        tmp->data = value;
        tmp->left = NULL;
        tmp->right = NULL;
        return tmp;
    }
    if (value <= root->data)
        root->left = insertrec(root->left, value);
    else
        root->right = insertrec(root->right, value);
    return root;
}
```