

COP 3502 - Computer Science I



#### Announcements

- Comment on Class Workload thus far:
  - # of hours expected of a full-time college student:
    - Just like a full-time job: around 40 or 50 or so hours/week
  - It is said that for every hour in class,
    - You can expect up to three hours of work outside class
  - Now do the math:
    - If you are registered for 12 credits
      - That adds up to 36 hours of outside-class work per week
      - For a total of 48 hours per week
  - Now ask yourself:
    - For this class, do you really put in 9 hours/week outside of the class?



#### Announcements

- Comment on Class Workload thus far:
  - Now ask yourself:
    - For this class, do you really put in 9 hours/week outside of the class?
    - Not even close!
    - If there's no program due, the average student puts in ZERO hours per week outside class
      - They don't even review notes for a MINUTE!
    - So how long then does a program take?
      - Let's even say 10 hours (which is high for most students)
      - Since they are due every two weeks (or so)
      - That adds up to 5 hours per week that you invest (at a max)
    - Leaving still 4 hours per week of study time!



- Program 3: Match-Making
  - Given a list of n men and n women
  - Also given the men's ratings of the women
  - And the women's ratings of the men
  - Find the best overall matching of men and women in the group
    - So you must find ALL possible matchings



Program 3: Match-Making

How many matchings will there be?

Example:

Following chart shows how the men rate the women:

	Diana	Ellen	Fran
Adam	4	8	7
Bob	6	7	5
Carl	5	9	6

Following chart shows how the women rate the men:

	Adam	Bob	Carl
Diana	7	6	8
Ellen	6	5	9
Fran	4	7	3



- Program 3: Match-Making
  - Example:
    - Here are the six (ALL) matchings:

<u>M1</u>	<u>S</u>	<u>M2</u>	<u>S</u>	<u>M3</u>	<u>S</u>
Adam+Diana	4	Adam+Diana	4	Adam+Ellen	6
Bob+Ellen	5	Bob+Fran	5	Bob+Diana	6
Carl+Fran	3	Carl+Ellen	9	Carl+Fran	3
<u>Total</u>	12		18		15

<u>M4</u>	<u>S</u>	<u>M5</u>	<u>S</u>	<u>M6</u>	<u>S</u>
Adam+Ellen	6	Adam+Fran	4	Adam+Fran	4
Bob+Fran	5	Bob+Diana	6	Bob+Ellen	5
Carl+Diana	5	Carl+Ellen	9	Carl+Diana	5
<u>Total</u>	16		19		14



- Program 3: Match-Making
  - Example:
    - Here are the six (ALL) matchings:

This is clearly the best match!

<u>M1</u>	<u>S</u>	<u>M2</u>	<u>S</u>	<u>M3</u>	<u>S</u>
Adam+Diana	4	Adam+Diana	4	Adam+Ellen	6
Bob+Ellen	5	Bob+Fran	5	Bob+Diana	6
Carl+Fran	3	Carl+Ellen	9	Carl+Fran	3
<b>Total</b>	12		18		15

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Adam+Ellen	6	Adam+Fran	4	Adam+Fran	4
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<u>Total</u>	16		19		14



- Program 3: Match-Making
  - Must use recursion
  - Must use permutations (this SAME algorithm)
  - Points to ponder:
    - The assignment says that you will try ALL possible matchings
    - So think about what it is that you need to permute
    - And once you finish any given permutation
      - k == # of people to permute
      - What do you do at this point?
        - Compute the likeability quotient
        - Is it better than previous best quotient?
        - Is it a tie? If so, what to do?



#### **Big-O Notation**

- What is Big O?
  - Big O comes from Big-O Notation
    - In C.S., we want to know how efficient an algorithm is...how "fast" it is
    - More specifically...we want to know <u>how the</u> <u>performance of an algorithm responds to changes</u> <u>in problem size</u>
    - The goal is to provide a *qualitative* insight on the # of operations for a problem size of n elements.
    - And this total # of operations can be described with a mathematical expression in terms of n.
      - This expression is known as Big-O



- Examples of Analyzing Code:
  - We now go over many examples of code fragments
  - Each of these functions will be analyzed for their runtime in terms of the variable n
  - Utilizing the idea of Big-O,
    - determine the Big-O running time of each



- Example 1:
  - Determine the Big O running time of the following code fragment:

```
for (k = 1; k <= n/2; k++) {
    sum = sum + 5;
}
for (j = 1; j <= n*n; j++) {
    delta = delta + 1;
}</pre>
```



#### Example 1:

- So look at what's going on in the code:
  - We care about the total number of REPETITIVE operations.
    - Remember, we said we care about the running time for LARGE values of n
    - So in a for loop with n as part of the comparison value determining when to stop  $for (k=1; k<=\underline{n}/2; k++)$
    - Whatever is INSIDE that loop will be executed a LOT of times
    - So we examine the code within this loop and see how many operations we find
      - When we say operations, we're referring to mathematical operations such as +, -, \*, /, etc.



#### Example 1:

- So look at what's going on in the code:
  - The number of operations executed by these loops is the sum of the individual loop operations.
  - We have 2 loops,
    - The first loop runs n/2 times
    - Each iteration of the <u>first loop</u> results in <u>one operation</u>
      - The + operation in: sum = sum + 5;
    - So there are n/2 operations in the first loop
    - The second loop runs n<sup>2</sup> times
    - Each iteration of the <u>second loop</u> results in <u>one operation</u>
      - The + operation in: delta = delta + 1;
    - So there are n<sup>2</sup> operations in the second loop.



#### Example 1:

- So look at what's going on in the code:
  - The number of operations executed by these loops is the sum of the individual loop operations.
  - The first loop has n/2 operations
  - The second loop has n<sup>2</sup> operations
  - They are NOT nested loops.
    - One loop executes AFTER the other completely finishes
  - So we simply ADD their operations
  - The total number of operations would be n/2 + n<sup>2</sup>
  - In Big-O terms, we can express the number of operations as O(n²)



- Example 2:
  - Determine the Big O running time of the following code fragment:

```
int func1(int n) {
    int i, j, x = 0;
    for (i = 1; i <= n; i++) {
        for (j = 1; j <= n; j++) {
            x++;
        }
    }
    return x;
}</pre>
```



#### Example 2:

- So look at what's going on in the code:
  - We care about the total number of REPETITIVE operations
  - We have two loops
    - AND they are NESTED loops
  - The outer loop runs n times
    - From i = 1 up through n
    - How many operations are performed at each iteration?
      - Answer is coming...
  - The inner loop runs n times
    - From j = 1 up through n
    - And only one operation (x++) is performed at each iteration



#### Example 2:

- So look at what's going on in the code:
  - Let's look at a couple of iterations of the OUTER loop:
    - When i = 1, what happens?
      - The inner loop runs n times
      - Resulting in n operations from the inner loop
    - Then, i gets incremented and it becomes equal to 2
    - When i = 2, what happens?
      - Again, the inner loop runs n times
      - Again resulting in n operations from the inner loop
  - We notice the following:
    - For EACH iteration of the OUTER loop,
    - The INNER loop runs n times
      - Resulting in n operations



#### Example 2:

- So look at what's going on in the code:
  - And how many times does the outer loop run?
    - n times
  - So the outer loop runs n times
  - And for each of those n times, the inner loop also runs n times
    - Resulting in n operations
  - So we have n operations per iteration of OUTER loop
  - And outer loop runs n times
  - Finally, we have n\*n as the number of operations
  - We approximate the running time as O(n²)



- Example 3:
  - Determine the Big O running time of the following code fragment:



#### Example 3:

- So look at what's going on in the code:
  - We care about the total number of REPETITIVE operations
  - We have two loops
    - They are NOT nested loops
  - The first loop runs n times
    - From i = 1 up through n
    - only one operation (x++) is performed at each iteration
  - How many times does the second loop run?
    - Notice that i is indeed reset to 1 at the beginning of the loop
    - Thus, the second loop runs n times, from i = 1 up through n
    - And only one operation (x++) is performed at each iteration



#### Example 3:

- So look at what's going on in the code:
  - Again, the loops are NOT nested
  - So they execute sequentially (one after the other)
- Therefore:
  - Our total runtime is on the order of n+n
  - Which of course equals 2n
- Now, in Big O notation
  - We approximate the running time as O(n)



- Example 4:
  - Determine the Big O running time of the following code fragment:



#### Example 4:

- So look at what's going on in the code:
  - We have one while loop
    - You can't just look at this loop and say it iterates n times or n/2 times
    - Rather, it continues to execute as long as n is greater than 0
    - The question is: <u>how many iterations will that be?</u>
  - Within the while loop
    - The last line of code divides the input, n, by 2
    - So n is halved at each iteration of the while loop
  - If you remember, we said this ends up running in log n time
  - Now let's look at how this works



#### Example 4:

- So look at what's going on in the code:
  - For the ease of the analysis, we make a new variable
    - originalN:
      - originalN refers to the value originally stored in the input, n
      - So if n started at 100, originalN will be equal to 100
  - The first time through the loop
    - n gets set to originalN/2
      - If the original n was 100, after one iteration n would be 100/2
  - The second time through the loop
    - n gets set to originalN/4
  - The third time through the loop
    - n gets set to originalN/8

#### **Notice:**

After **three** iterations, n gets set to originalN/2<sup>3</sup>



#### Example 4:

- So look at what's going on in the code:
  - In general, after k iterations
    - n gets set to originalN/2<sup>k</sup>
  - The algorithm ends when originalN/2<sup>k</sup> = 1, approximately
  - We now solve for k
  - Why?
    - Because we want to find the total # of iterations
  - Multiplying both sides by  $2^k$ , we get originalN =  $2^k$
  - Now, using the definition of logs, we solve for k
    - k = log originalN
  - So we approximate the running time as O(log n)



## Brief Interlude: Human Stupidity





- Example 5:
  - Determine the Big O running time of the following code fragment:



- Example 5:
  - So look at what's going on in the code:
    - At first glance, we see two NESTED loops
    - This can often indicate an O(n²) algorithm
      - But we need to look closer to confirm
    - Focus on what's going on with i and j



- Example 5:
  - So look at what's going on in the code:
    - Focus on what's going on with i and j
      - i and j clearly increase (from the j++ and i++)
      - BUT, they never decrease
      - AND, neither ever gets reset to 0



#### Example 5:

- So look at what's going on in the code:
  - And the OUTER while loop ends once i gets to n
  - So, what does this mean?
    - The statement i++ can never run more than n times
    - And the statement j++ can never run more than n times



#### Example 5:

- So look at what's going on in the code:
  - The MOST number of times these two statements can run (combined) is 2n times
  - So we approximate the running time as O(n)



- Example 6:
  - Determine the Big O running time of the following code fragment:
    - What's the one big difference here???



- Example 6:
  - So look at what's going on in the code:
    - The difference is that we RESET j to 0 a the beginning of the OUTER while loop



#### Example 6:

- So look at what's going on in the code:
  - The difference is that we RESET j to 0 a the beginning of the OUTER while loop
  - How does that change things?
    - Now j can iterate from 0 to n for EACH iteration of the OUTER while loop
      - For each value of i
    - This is similar to the 2<sup>nd</sup> example shown
  - So we approximate the running time as O(n²)



- Example 7:
  - Determine the Big O running time of the following code fragment:



#### Example 7:

- So look at what's going on in the code:
  - First notice that the runtime here is NOT in terms of n
  - It will be in terms of sizeA and sizeB
  - And this is also just like Example 2
  - The outer loop runs sizeA times
  - For EACH of those times,
    - The inner loop runs sizeB times
  - So this algorithm runs sizeA\*sizeB times
  - We approximate the running time as O(sizeA\*sizeB)



- Example 8:
  - Determine the Big O running time of the following code fragment:



#### Example 8:

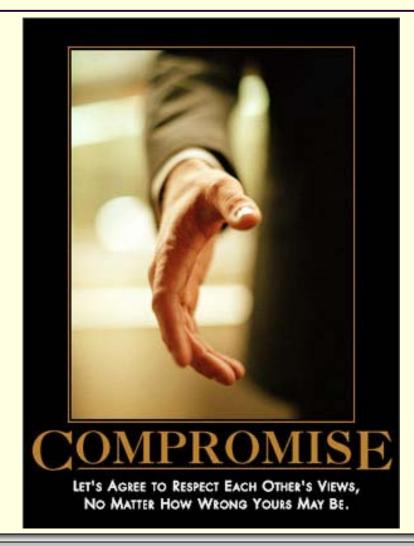
- So look at what's going on in the code:
  - Note: we see that we are calling the function binSearch
  - As discussed previously, a single binary search runs in O(log n) time
    - where n represents the number of items within which you are searching
- Examining the for loop:
  - The for loop will execute sizeA times
  - For EACH iteration of this loop
    - a binary search will be run
  - We approximate the running time as O(sizeA\*log(sizeB))

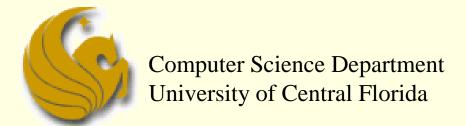


## **WASN'T** THAT SWEET!



## Daily Demotivator





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