

Introduction to Computing and Algorithms

Basic Data, Operations and Decisions

Chapter 3

Basic Tools for Building Algorithms

- Atomic Data
 - Numbers
 - Characters
 - Booleans
 - Pointers
- Operators
 - Assignment
 - Arithmetic
 - Input / Output
 - Relational
 - Boolean

Data

Data Structures are containers for data.

The simplest of them are called “**atomic**” because they hold only a single value; the data they hold cannot be subdivided into lower-level components.

“**Complex**” data structures may hold multiple pieces of data, are constructed from atomic types.

Four atomic types:

- Character
- Number
- Boolean
- Pointer

One built-in complex type:

- String

Built-in Data Types

Variables are data structures whose value *may be changed* by the algorithm.

- Each variable must be *declared* to
 - have an *identifier* (i.e., a *name*)
 - be of some *data type*:

For example: to declare a variable named “some number” that can hold a numeric value:

```
some_number isoftype Num
```

- Each variable must be *assigned* a value of the appropriate type:

For example: to assign the value 4 to the variable *some_number*:

```
some_number <- 4
```

Built-in Data Types

- ***Numbers***, declared as:

```
my_age isoftype Num
```

my_age can now store one number
of any magnitude

For example:

```
my_age <- 1      // this is OK
my_age <- 65     // so is this
my_age <- 14.5   // and so is this

my_age <- "old"  // an ERROR
```

Built-in Data Types (cont.)

- ***Characters***, declared as:

```
your_grade isoftype Char
```

your_grade can now store any
one alphanumeric character
single-quote marks are used to
distinguish Char values from
identifiers.

For example:

```
your_grade <- 'A'    // this is OK  
your_grade <- 'B'    // so is this
```

```
your_grade <- 'A-'    // an ERROR
```

```
your_grade <- '9'     // this is OK  
your_grade <- 9        // an ERROR  
your_grade <- '10'    // an ERROR
```

Built-in Data Types (cont.)

- ***Booleans***, declared as:

```
this_test isoftype Boolean
```

this_test can now hold one
boolean (*TRUE* or *FALSE*) value

For example:

```
this_test <- TRUE           // this is OK
```

```
this_test <- FALSE          // so is this
```

```
this_test <- "true"         // an ERROR
```

Built-in Data Types (cont.)

- ***Pointers***, declared as:

```
this_num_ptr isoftype ptr toa Num
```

this_num_ptr can now “know”
where a *Num* variable “lives” in
memory

(will discuss pointers later)

Built-in Data Types (cont.)

- ***String*** is a *built-in complex* (non-atomic) type which can hold a collection of characters.

A string is declared as:

```
this_string isoftype String
```

this_string can now hold a “string” of any number of alphanumeric characters

For example:

```
this_string <- “a group of Chars” // this is OK  
this_string <- a group of Chars   // an ERROR
```

```
this_string <- “45”                // this is OK  
this_string <- 45                  // an ERROR
```

The Assignment Operator

The Assignment Operator stores a particular value in a variable.

```
my_age <- 43
```

(any integer or real number)

```
your_grade <- 'A'
```

(quote marks needed to distinguish Chars from variable names)

```
this_test <- TRUE
```

(*TRUE* and *FALSE* are each *single* boolean values)

Assignment Operator (cont.)

For pointers, assignment means one of three things, depending on how used ...

1. Creating a new variable. Given:

```
this_ptr isoftype ptr toa Num,  
that_ptr isoftype ptr toa Num ,  
other_ptr isoftype ptr toa Num
```

then:

```
this_ptr <- new(Num)  
that_ptr <- new(Num)
```

creates a *new* Number variable for each pointer and makes the specified *pointer variable* refer to it, e.g.:

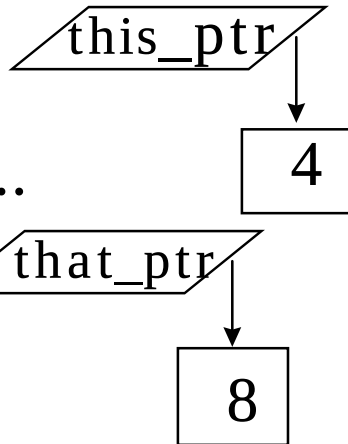


Assignment Operator (cont.)

2. Assigning a value to a variable to which a ptr points..

Given previous, then:

```
this_ptr^ <- 4  
that_ptr^ <- 8
```

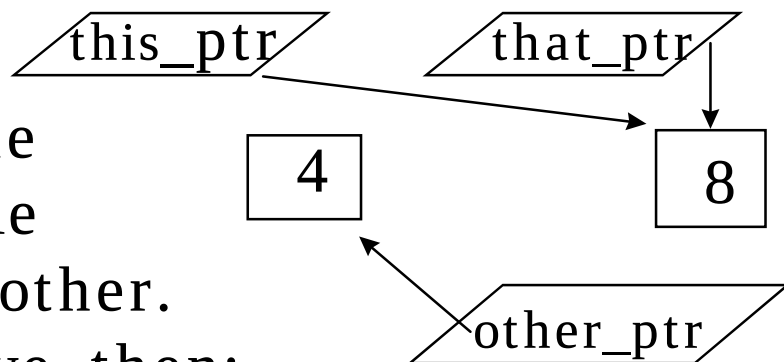


assigns those values to the Num var to which the pointer var refers.

3. Making one ptr variable refer to another.

Given above, then:

```
other_ptr <- this_ptr  
this_ptr <- that_ptr
```



assigns/reassigns pointers variables to reference other variables

Arithmetic Operators

Arithmetic Operators allow us to express mathematical operations:

- Addition $+$
- Subtraction $-$
- Multiplication $*$
- Division $/$

Using the Arithmetic Operators

- To add the values found in variables *num_one* and *num_two*, and store the result in variable *num_three*:

```
num_three <- num_one + num_two
```

Use parentheses to alter the standard order of operations:

- To add the values found in *num_one* and *num_two*, multiply the result by two, and store that result in variable *num_three*:

```
num_three <- (num_one + num_two) * 2
```

Input and Output Operators

I/O Operators:

allow us to communicate with the “outside world,” i.e, the real world beyond the algorithm

read - obtains an input value

each *read* operation does 2 things:

1. obtains next value from “outside”
2. stores it in the specified variable

```
// get next value, store it in var num_one  
read (num_one)
```

print - sends out an output value

```
// output the current value of  
// variable num_two  
print (num_two)
```

```
// output a literal text message  
print (“Hello, World!”)
```

Input and Output Operators

read and *print* may take *any number* of arguments of type Num, Boolean, Char, or String.

For example,

```
read(this_var)
read(that_var)
```

is equivalent to:

```
read (this_var, that_var)
```

- Don't worry about the exact details of the format of input or about how to format output for printing.
- We intentionally leave that vague for now. Assume that it works by magic.
- Such things are unimportant details covered in later programming courses.

A Simple Example

```
algorithm Simple_Example
```

```
    // declare the variables  
    num_one,  
    num_two,  
    num_three isoftype Num
```

```
    // get the numbers from “outside”  
    read (num_one, num_two)
```

```
    // perform addition and show result  
    num_three <- num_one + num_two  
    print(“The addition result is: ”, num_three)
```

```
    //perform multiplication and show result  
    num_three <- num_one * num_two  
    print(“This multiplication results is: ”, num_three)
```

```
endalgorithm // Simple_Example
```

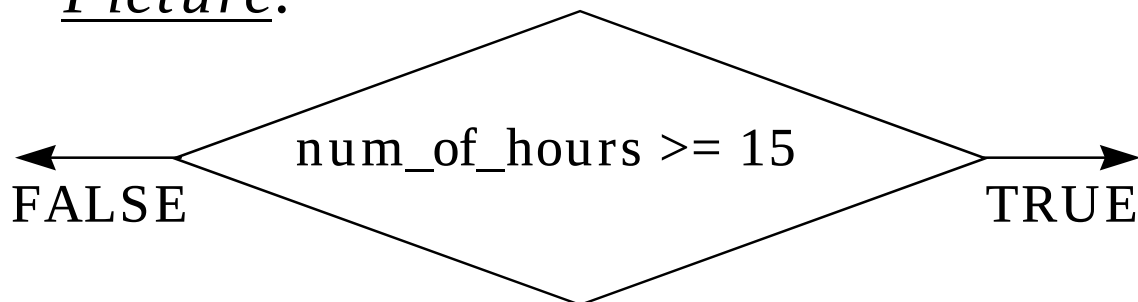
Decisions Statements (Conditionals)

Conditionals allow us to make decisions about data. Results of conditionals are always *TRUE* or *FALSE*, i.e., *boolean values*.

Natural Language:

“Is it true that the number of hours is greater than or equal to 15 ?”

Picture:



Code:

```
if (num_of_hours >= 15) then...
```

Decisions Statements (Conditionals)

Conditionals can have three parts:

- *A conditional expression*
- *A then clause*
- *An (optional) else clause*

For example:

```
if (num_one < num_two) then
    highest <- num_two
else
    highest <- num_one
endif
```

The “else” clause is optional:

```
if ( salary > MONEY_NEEDED ) then
    save some of it
    give some to charity
endif
```

Relational Operators

Conditionals produce boolean (*TRUE* / *FALSE*) results based on comparisons specified by the *relational operators*:

- Greater than >
- Greater or equal >=
- Equal to =
- Less than or equal <=
- Less than <
- Not equal to < >

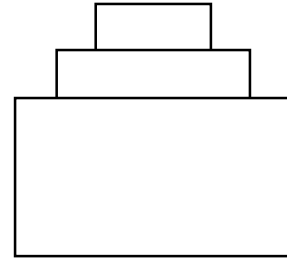
Decisions Statements (Conditionals)

- These simple *if-then-else* constructs enable computers to do complex things.
- The difference between a *calculator* and a *computer* is “the ability to make decisions and act on them”
- *All decisions* made by *any* computer is governed by the simple mechanism of:
 - compare two values according to the specified relational operator
 - if the answer is TRUE take one course of action, else take another course of action.
- Computer-made decisions that appear to be complex are all constructed from simple *if-then-else* logic . . .

Nested Conditionals

Plain English

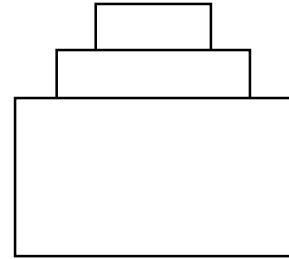
Conditionals can
reside *inside* other
conditionals:



```
check if Today is Sunday
if it is Sunday,
    if it's not Raining go to
    the park, otherwise
    stay home
if its NOT Sunday,
    go to work
```

Nested Conditionals Pseudocode

Conditionals can
reside inside other
conditionals:



```
if (Today = Sunday) then
    if (NOT Raining) then
        go to the park
    else
        stay home
    endif
else
    go to work
endif
```

- Note use indentation and *endifs* to make nesting clear, unambiguous

Boolean Operators

Decisions may have multiple parts:

if the class is not full AND
it does not conflict with a
currently scheduled class. . .

Boolean operators allow us to
express compound conditionals:

- AND

// both conditions must be true
((5 > 4) AND (4 > 7)) is FALSE

- OR

// at least one condition must be true
((5 > 4) OR (4 > 7)) is TRUE

- NOT

// reverses the boolean value
NOT (4 > 7) is TRUE

Using the Boolean Operators

```
if (NOT (it is raining))
then
    go to the park
else
    play video games
endif
```

- Boolean operators can be combined:

```
if ((location = Atlanta) AND
    (house_cost < 150,000) OR
    won_lottery) then
    buy_the_house
else
    keep_looking
endif
```

- What does the complex condition above really do?

Documenting Algorithms

FICTION: “the main audience for an algorithm is a computer.”

FACTS: only 10-20% of \$\$ cost is *writing* algorithm;

80-90% is subsequent repair, extension, reuse by *people*.

TRUTH: writing algorithms for the human audience is ***critical*** and ***essential***

DOCUMENTATION: refers to brief, explanatory comments that are written into the algorithm for the purpose of making it easy for people to understand

Documenting Algorithms

- To signify documentation, use *double slash marks*.
- Whatever follows is documentation, i.e., notes to the reader, not instructions to the computer,

```
// this is a documentation comment
```

- Document:
 - purpose of algorithm and modules;
 - the role of data structures;
 - key decision points;
 - complex calculations;
 - changes in flow of control.
- Don't document the trite & trivial, e.g.,

```
// Assign the value 4 to variable a_value  
a_value <- 4
```

Self-Documenting Algorithms

Whereever possible, make the algorithm *self-documenting* by:

- Using *descriptive identifiers*. Choose variable names that describe the data they will hold.

For example,

If declaring variables to hold values for the *radius and area of a circle . . .*

Good:

```
radius isotype Num  
area isotype Num
```

Bad:

```
x isotype Num // used to store radius  
y isotype Num // used to store area
```

- Use *constants* instead of *literals* . . .

Literals

Literals are data values that are “hardwired” into the algorithm:

algorithm Literals

```
num_one isotype Num  
num_one <- 1
```

```
your_grade isotype Char  
your_grade <- “A”
```

```
your_score isotype Num  
your_score <- 42
```

```
print(“Each assignment statement here  
      contains a literal value”)
```

endalgorithm // Literals

Constants

A better way ...

- To use non-variable values in your algorithm, use **constants**, not *literals*:
- A constant allows us to give a name (identifier) to a fixed value, making it easier to read and understand.

For example:

PI is 3.1415926

TAX_RATE is .28

Then, instead of:

area = 3.1415926 * radius * radius

we have:

area = PI * radius * radius

And instead of

tax_due <- taxable_gain * .28

we have

tax_due <- taxable_gain * TAX_RATE

Another Simple Example

```
algorithm Circle_Facts
// declare constants and variables
PI is 3.1415926
radius,
diameter,
circumference,
area isotype Num

// get data
print("Enter the radius")
read(radius)

// perform calculations
diameter <- radius * 2
circumference<- 2 * PI * radius
area <- PI * radius * radius

// display the results
print("Diameter is: ", diameter)
print("Circumference is: ", circumference)
ptint ("Area is: ", area)

endalgorithm // Circle_Facts
```

Tracking Stooge Boinks

```
algorithm Stooge_Boinks
// calculates the average number of boinks
// performed per Stooge in a given episode

NUM_STOOGES is 3
larry isotype Num
moe isotype Num
curley isotype Num

// obtain data from user
print("Enter number of boinks by Larry,
      Moe and Curley, respectively")
read (larry, moe, curley)

// perform calculation
average isotype Num
average <- (larry + moe + curley)
          / NUM_STOOGES

// generate output
print ("The average number of boinks
      per stooge is ", average)

endalgorithm // Stooge_Boinks
```

Simple Finances

algorithm Net_Interest_Earned

```
// Computes simple interest earned in one year
// and associated flat-rate tax, based on data
// obtained from user.
```

```
money_invested isoftype Num
read(money_invested)
```

```
interest_rate isoftype Num
read(interest_rate)
```

```
interest_earned isoftype Num
interest_earned <- money_invested *
                    (INTEREST_RATE)
```

```
TAX_RATE is .34 // 34% (28 fed+6 state)
taxes_incurred isoftype Num
taxes_incurred <- interest_earned * TAX_RATE
```

```
print ("In one year at " + interest_rate + " interest, ")
print (money_invested, " earns " + interest_earned)
print (taxes_incurred, " is owed in taxes, for a net.")
print ("gain of " + (interest_earned - taxes_incurred))
```

endalgorithm // Net_Interest_Earned