


Today: Quantum Cryptography
 Wed: Quiz Review
 Fri: Quiz

→ completely from Code Book

send photons →

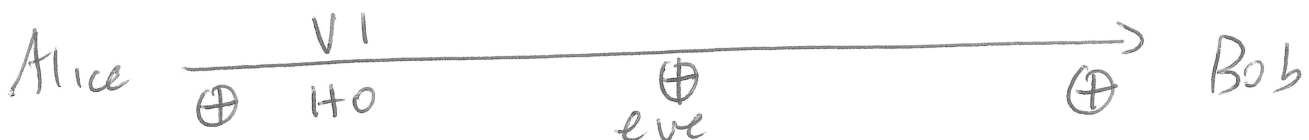
fiber optic cable
 each photon has an orientation , can spin anywhere 360°, / \ -

Reader for a photon  HV  FB

Send a photon through HV reader or V, then try to read it again on HV reader then it'll definitely be V.

Send a photon through FB reader as F the 2nd FB reader will also read F

Issue if you send a V photon using HV reader but try to read it later with FB reader, you'll get each result ~ 50% of the time.



Describe a key exchange method via quantum particles.

Alice choose random readers $\begin{matrix} \swarrow R1 HV \\ \searrow R2 PB \end{matrix}$

| | R1 | R1 | R1 | R2 | R2 | R1 | R2 | ... |
|-------------|----|----|----|----|----|----|----|-----|
| bits | + | + | + | X | X | + | X | ... |
| msg | - | 1 | | \ | / | - | / | |
| EVE | + | X | + | X | + | X | X | |
| Bob guess R | + | X | + | X | X | X | + | |
| | V | | V | V | V | | | |
| | 0 | 1 | 0 | 1 | 1 | 0 | 1 | |

GOAL
DETECT AN INTRUDER

eve guesses
eve wrong
bob RIGHT

100% correct

50% Bob correct
50% Bob incorrect

Possible Eve guesses wrong + Bob guesses right
 $\frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$

Probability Bob gets correct reading in this case $\frac{1}{2}$

$\frac{1}{8} = \frac{1}{4} \times \frac{1}{2} \rightarrow$ eve guesses wrong, bob guesses right, bob gets WRONG BIT!

Idea: send lots of bits say

$$2 \times \frac{1024}{\text{word}} + \frac{400}{\text{sample}} \approx 2500$$

50%
bob
misses

Choose 400 bits at
random to sample.
If eve was listening
w/ probability

~~$(\frac{7}{8})^{400}$ Bob
will read all bits
correctly!~~

to exchange
secret key

send $2X + S + \text{Buffer}$
bits.

Sample S bits.
For all that Bob
used for correct
reider, verify Bob
got ^{the} correct answer.

If he did, the
transmission was
clean and no one
was listening.

What will really happen \rightarrow
 ~ 200 get thrown out since
Bob guess wrong.

out of 200 left,
eve guesses correctly ~ 100 times
of the 100 that eve guessed
~~right~~ wrong + Bob got right
probability Bob gets all of
these correct is $(\frac{1}{2})^{100}$

\uparrow
probability
eve is
undetected

Figure out of the
 $2X$ bits which ones
Bob picked correct
reider + those bits are
the secret key.

prime $\sim \underline{\underline{2^{20}}}$ or 2^{24}

$\frac{\text{prime}}{2^{16}} \sim 15, 16, 17, 18 \dots$

max x is $\geq \frac{\text{limit} \times 2^{16}}{r}$

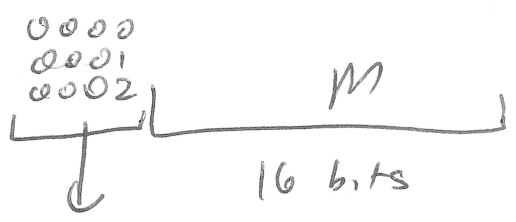
$0 \times 2^{16} + M$

$1 \times 2^{16} + M$

$2 \times 2^{16} + M$

⋮

$(\text{limit} - 1) \times 2^{16} + M \rightarrow < \text{limit} \times 2^{16}$



Value

$(i \ll \text{numbits}) + M$

\times Value

I am trying

$= (i \times 2^{\text{numbits}} + M)$

$\equiv M \pmod{2^{16}}$

med

$0 \times 2^{16} + 10825 \quad \times$

$1 \times 2^{16} + 10825 \quad \checkmark$

$\sim 70,000$