

Public Key Cryptography

Everything before this required 2 people to meet in a secure location to exchange a private key.

Is it possible for 2 people (Alice, Bob) to communicate on an insecure line so everyone can see what they're saying to each other, but at the end of the conversation they've exchanged a secret key that no one else can decipher?

Whitfield Diffie - gave talks about the possibility of a public key exchange protocol.

Martin Hellman - was interested in what Diffie had to say + decided he wanted to work with him on it.

1972-34?

took about a year!

Diffie-Hellman Key Exchange

Security is based on the difficulty of the Discrete Log Problem.

Alice

Public keys

$p = \text{large prime}$

$g = \text{generator}$

Bob

Alice picks
secret value
 $a, 1 < a < p-1$

Alice computes

$$B^a \pmod p$$

$$(g^b)^a \pmod p$$

$$\equiv g^{ab} \pmod p$$

sends $A = g^a \pmod p$

sends $B = g^b \pmod p$

Observer sees

g^a, g^b , but doesn't

see a or b .

Shared key

$$(g^a)(g^b) = g^{a+b} \text{ not helpful}$$

$$(g^a)^{g^b} = g^{ag^b} \equiv \text{not helpful}$$

Bob picks
secret value
 $b, 1 < b < p-1$

Bob
computes

$$A^b \pmod p$$

$$(g^a)^b \pmod p$$

$$\equiv g^{ab} \pmod p$$