

1) Schedule



M - Labor Day  
 W - QUIZ  
 closed notes  
 formula sheet  
 11:5 → skt 11<sup>25</sup>  
 extend 12<sup>25</sup>  
 F - Do not come  
 to class  
 Watch Playfair  
 Video

2) Breaking Vigenere + MIC



Kasiski Test

l. of C.  
 → Find key word length

Ciphertext  $c_0 c_1 c_2 \dots c_{n-1}$  length  $n$   
 keyword length  $k$

BINS 0  $(c_0, c_k, c_{2k}, c_{3k}) \dots c_{\frac{n-k}{k}k}$

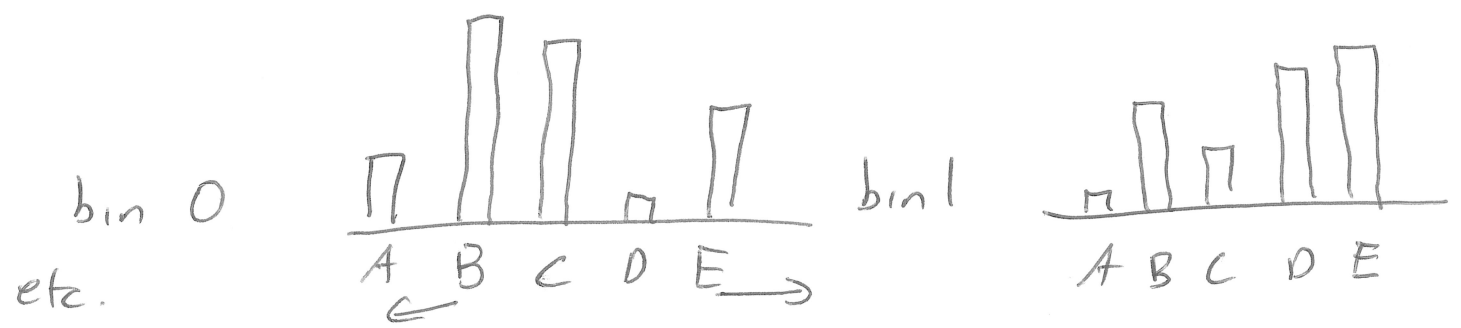
BIN 1  $(c_1, c_{k+1}, c_{2k+1}) \dots c_{n-k+1}$

⋮

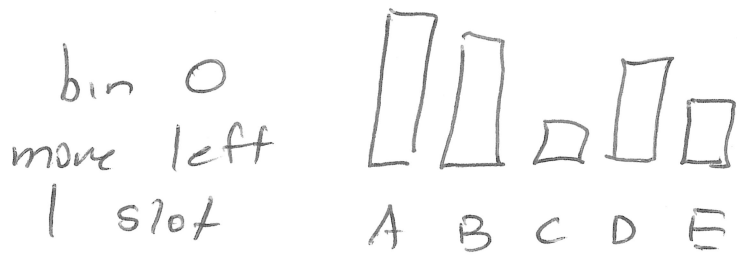
BIN  $k-1$   $(c_{k-1}, c_{2k-1}) \dots c_{n-1}$

all letters in bin 0 shifted by  $a_0$   
 = = = = | shifted by  $a_1$ , etc.

LETTERS A B C D E



Imagine bar graph conveyor belt (circular)



So if  $k_0 = 'B'$  then this would be plaintext letters.

VISUALLY  $\rightarrow$  try each cyclic shift of a bin and find the one that looks like English frequencies

How can we do this mathematically w/o drawing lots of graphs and eyeballing them?

### Mutual Index of Coincidence

Problem: Get 1 candy from each of 2 neighbors. What is the probability they are same?

	N1	N2
Snickers	10	<del>80</del> 30
Twix	20	5
Skittles	30	5
Mars	40	10

$$\begin{aligned}
 & \frac{10 \times 30 + 20 \times 5 + 30 \times 5 + 40 \times 10}{100 \times 50} \\
 & = \frac{300 + 100 + 150 + 400}{5000} \\
 & = \frac{950}{5000} = \frac{95}{1000} = \boxed{\frac{19}{200}}
 \end{aligned}$$

$$MIC(S_1, S_2) = \frac{\sum_{i=1}^k f_i \times g_i}{n \times m}$$

$$n = \sum_{i=1}^k f_i$$

$f_i$  is # of item  $i$  in  $S_1$

$g_i$  is # of item  $i$  in  $S_2$

$$m = \sum_{i=1}^k g_i$$

If your bin is real English this tends to maximize MIC calculation

Original bin 0 10, 50, 45, 5, 20

bin 1 8, 25, 15, 40, 45

Martin Language =  $.22, .1, .3, .34, .03$

$$\left( \begin{matrix} 10 & + & 50 & + & 45 & + & 5 & + & 20 \\ \times .22 & \times & .1 & \times & .3 & \times & .34 & \times & .03 \end{matrix} \right) / 130$$

$$= \frac{23.2}{130} = .178$$

Shift 1

50 45 5 20 10  
 $.22 \quad .1 \quad .3 \quad .34 \quad .04$

$$= \frac{24.2}{130} = .186$$

Shift 2

45 5 20 10 50  
 $.22 \quad .1 \quad .3 \quad .34 \quad .04$

$$= \frac{21.8}{130} = .168$$

Shift 3

5 20 10 50 45  
 $.22 \quad .1 \quad .3 \quad .34 \quad .04$

$$= \frac{24.9}{130} = .192$$

Shift 4

20 10 50 45 5  
 $.22 \quad .1 \quad .3 \quad .34 \quad .04$

$$= \frac{32.16}{130} = .247$$