

1) Grade Calculation - Will post how to calc our grade by tomorrow.

2) Homework 6 will be made up soon - look for it! (might have prize!)

### 3) Public Key Cryptography

Private Key / Symmetric 2 people must ~~to~~ meet in a secure location and exchange a shared secret key.

Is it possible for 2 people to have a conversation with others listening, but at the end of it, exchange some secret info that the others can't ~~deduce~~ deduce or figure out?

Goal #1: Exchange a secret key (bitstring)  
Public Key Exchange

Goal #2: Straight up exchange messages of our choosing  
Public Key Cryptography

Both Solved in the 1970s.

- Publicly known / ~~post~~ published solution  $\rightarrow$  1976 Key  $\rightarrow$  1977 Crypto
- Secret Solution (person didn't get credit for a long time)  $\rightarrow$  1972/3 (both) Clifford Cocks

Whitfield Diffie

Today's Lec: Diffie-Hellman Key Exchange

Look at Discrete Log Problem

$$c = b^e \pmod p \quad \left. \vphantom{c = b^e \pmod p} \right\} \text{easy calc forward}$$

but given  $c, e$  and  $p$  hard figure out  $b$ .

Public Components

$p =$  large prime (many digits)

$g =$  generator of prime

Private Keys

$a =$  Alice's secret key

$b =$  Bob's secret key

$$1 < a, b < p-1$$

Alice

$$C_1 = g^a \pmod p$$

receives  $C_2$

$$K = C_2^a \pmod p$$

$\rightarrow$  shared key

$$C_2^a = (g^b)^a \pmod p = g^{ab} \pmod p$$

sends to Bob  $\rightarrow$

sends to Alice  $\leftarrow$

PUBLIC

$C_1$

$C_2$

$p$

$g$

Bob

receives  $C_1$

$$C_2 = g^b \pmod p$$

$$K = C_1^b \pmod p$$

$\rightarrow$  shared key

$$C_1^b = (g^a)^b \pmod p$$

$$= g^{ab} \pmod p$$

As a hystander you know:

$p$  - prime

$g$  - gen

$$g^a = c_1$$

$$g^b = c_2$$

$$c_1 \times c_2 = g^{a+b} \quad X$$

$$c_1^b = (g^a)^b = g^{ab} \quad X$$

→ knowledge of  $c_1, g$  and  $p$  doesn't compromise knowledge of  $a$  (Discrete Log Problem)