

① Breaking Vigenere

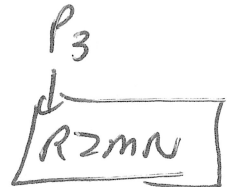
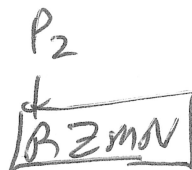
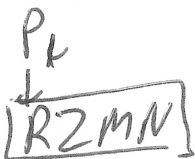
- Kasiski Test

- Index of Coincidence

- Mutual Index of Coincidence

② Cryptool

③ Quiz Wed



repeated n-grams

ciphertext

length keyword = $\text{gcd}(P_2 - P_1, P_3 - P_2, P_5 - P_4)$

QZRB

QZRB

P_4

P_5

Index of Coincidence is defined on a set of multi objects

10 Twix

8 Snickers

22 Skittles

25 Mars

randomly select 2 items out of the whole.

What is probability they are the same type?

$$f_1, f_2, \dots, f_k \quad f_1 + f_2 + f_3 + \dots + f_k = n$$

$$10, + 8, + 22, + 25 = 65 (n)$$

$$\frac{10}{65} \times \frac{9}{64} + \frac{8 \times 7}{65 \times 64} + \frac{22 \times 21}{65 \times 64} + \frac{25 \times 24}{65 \times 64}$$

↑
1st
twix

$$= \frac{90 + 56 + 462 + 600}{65 \times 64}$$

$$= \frac{1208}{65 \times 64} = \frac{302}{65 \times 16} = \frac{151}{65 \times 8} = \boxed{\frac{151}{520}}$$

$$\begin{array}{r} 65 \\ \times 8 \\ \hline 520 \\ \end{array}$$

$$\begin{array}{r} 22 \\ \times 21 \\ \hline 462 \\ \end{array}$$

$$\begin{array}{r} 600 \\ 462 \\ \hline 1062 \\ \end{array}$$

$$\begin{array}{r} 10 \\ \times 146 \\ \hline 1460 \\ \end{array}$$

$$\begin{array}{r} 22 \\ \times 21 \\ \hline 462 \\ \end{array}$$

$$\begin{array}{r} 600 \\ 462 \\ \hline 1062 \\ \end{array}$$

$$\begin{array}{r} 10 \\ \times 146 \\ \hline 1460 \\ \end{array}$$

$$\begin{array}{r} 208 \\ \end{array}$$

$$IC = \frac{\sum_{i=1}^k f_i \times (f_i - 1)}{n(n-1)}$$

We use this with frequency of letters

Cipher : c_0, c_1, c_2, \dots

Guess keyword length is 5

Shifted to bin 0 : c_0, c_5, c_{10}, c_{15} frequencies should be ~~to~~ plaintext freq.

Shifted to bin 1 : $c_1, c_6, c_{11}, c_{16}, \dots$

Shifted to bin 2 : $c_2, c_7, c_{12}, c_{17}, \dots$

Shifted to bin 3 : $c_3, c_8, c_{13}, c_{18}, \dots$

Shifted to bin 4 : $c_4, c_9, c_{14}, c_{19}, \dots$

If a distribution is equally random
 $\frac{1}{26}$ letters is A, B, etc.

$$IC(\text{set}) \approx \frac{1}{26} = .0378 \text{ ish}$$

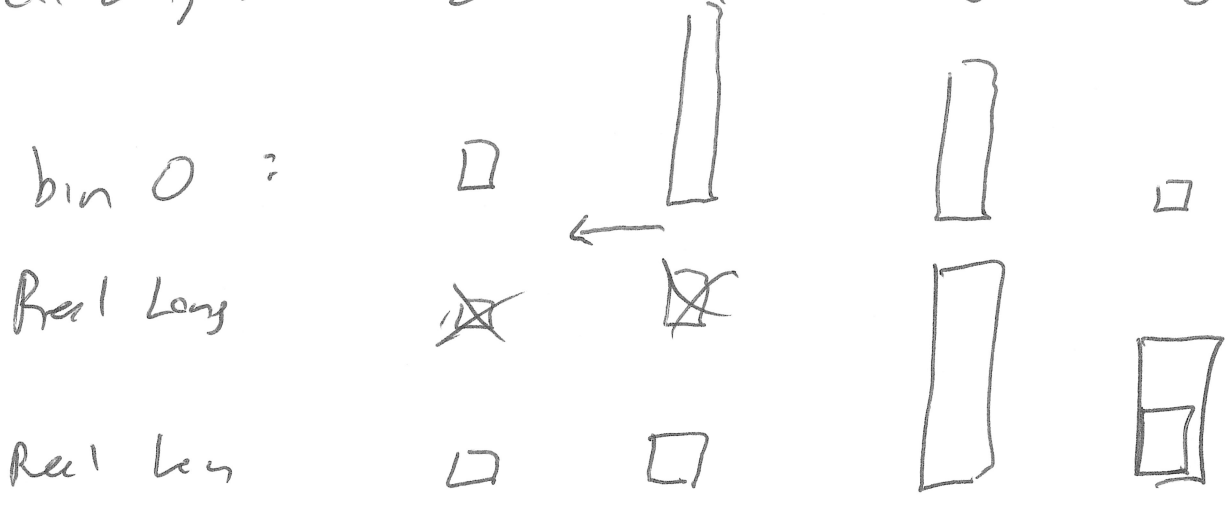
$$IC(\text{English}) \approx .0676$$

The more "off balanced" a distribution is
the higher the Index of Coincidence!

If we guessed correctly, the IC of
ALL the bins should be "high"
near 0.07. If we guessed wrong, some
bins will be lower.

Once we know the length of the
keyword, what do we do?

Cipher	A	B	C	D
Bin 0:	3	18	10	1
Real Leng:	2%	4%	60%	34%



Left Shift 0	3	18	10	1
Left Shift 1	18	10	1	3
Left Shift 2	10	1	3	18
Left Shift 3	1	3	18	10

Intuitively, try all left shifts (decrypt) on a bin, and pick the one that makes the adjusted bar graph look most like the English!

	bin graph	↓				
b.g. 1	3	18	10	1	Set 1	
	X	X	X	X		
b.g. 2	2	4	60	34	Set 2	

What's the probability if I grab 1 item from set 1 and 1 item from set 2, that they are the same?

Mutual Index of Coincidence $= \frac{3}{32} \times \frac{2}{100} + \frac{18}{32} \times \frac{4}{100} + \frac{10}{32} \times \frac{60}{100} + \frac{1}{32} \times \frac{34}{100}$

$$f_1 + f_2 + \dots + f_k = n$$

$$g_1 + g_2 + \dots + g_k = m$$

$$\text{MIC}(F, G) = \frac{\sum_{i=1}^k f_i \times g_i}{n \times m}$$

LS 0

$$\begin{array}{r} 3, 18, 10, 1 \\ \times 2 \quad 4 \quad 60 \quad 34 \\ \hline 6 + 72 + 600 + 34 \end{array}$$

LS 1

$$\begin{array}{r} 18, 10, 1, 3 \\ 2 \quad 4 \quad 60 \quad 34 \\ \hline 36 + 40 + 60 + 102 \end{array}$$

$$\begin{array}{r} 34 \\ 18 \\ \hline 272 \\ 34 \end{array}$$

LS 2

$$\begin{array}{r} 10, 1, 3, 18 \\ 2 \quad 4 \quad 60 \quad 34 \\ \hline 20 + 4 + 180 + 612 \end{array}$$

LS 3

$$\begin{array}{r} 1, 3, 18, 10 \\ 2, 4, 60, 34 \\ \hline 2 + 12 + 1080 + 340 \end{array}$$