

CIS 3362

Goal: Past H2 before I leave
Code Breaking - Substitution, Vigenere

Today: Vigenere Cipher

Under substitution transformation the set of letter frequencies is UNCHANGED (invariant).

Plain text: T O D A Y I S W E D N E S D A Y

19, 14, 3, 0, 24, 8, 18, 22, 4, 3, 13, 4, 18, 3, 0, 24

KEY:

K N I G H T S K N I G H T S K N

+ 10, 13, 8, 6, 7, 19, 18, 10, 13, 8, 6, 7, 19, 18, 10, 13

29, 27, 11, 6, 31, 27, 36, 32, 17, 11, 19, 11, 37, 21, 10, 37

↓ ↓ ↓ ↓ ↓ ↓
3 1 5 1 10 6

↓ ↓
11 11

Cipher

D B L G F B K G R L T L L V K L

Remained unbroken 1500s - early 1800s

This breaks the fundamental assumption that

(1) the same letter Plain maps same letter
cipher

(2) 2 ciphered letters are same \Rightarrow same plain text letters
LL

TO DO

① Live Code to fill some missing pieces on my sample programs.

② Vigenere Cryptanalysis

→ frequencies messed up

What about repeated n-grams?

P_1, P_2, P_3, P_4, P_5
 K_3, K_4, K_5, K_6, K_7

67, 68, 69, 70, 71

L_1, L_2, L_3, L_4, L_5

P_1, P_2, P_3, P_4, P_5
 K_3, K_4, K_5, K_6, K_7

122, 123, 124, 125, 126

L_1, L_2, L_3, L_4, L_5

Scenario 1
same plain
same cycle
of key

P_1, P_2, P_3, P_4, P_5
 K_1, K_2, K_3, K_4, K_5

L_1, L_2, L_3, L_4, L_5

$P_6, P_7, P_8, P_9, P_{10}$
 K_4, K_5, K_6, K_7, K_8

L_1, L_2, L_3, L_4, L_5 } Coincidence

Scenario 2

→ Probability low → longer the repeated string, lower probability...

→ repeated likely keyword lines up

$$\begin{array}{r} 122 \\ - 67 \\ \hline 55 \end{array}$$

→ keyword length likely divides into this evenly
5, 11

Kasiski Test: Look for all repeated
n-grams $n \geq 3$. Note their starting index

Indices: 67, 122, 207



55 85 num divides into 55
AND 85

take gcd of each of these gaps
and that's likely the keyword length.