

⑥ Oops - Computer @ Home → next ~~Wed~~ Fri
 (showing Cryptool.java)

all files in dir
 javac Cryptool.java
 java Cryptool

① Kasiski Test

② Index of Coincidence

③ Mutual Index of Coincidence

→ find keyword length

plaintext: $P_0 P_1 P_2 P_3 P_4$
 key: $K_0 K_1 K_2 K_0 K_1 K_2 \dots$

If we knew keyword length, we could create $|k|$ bins each which should mirror frequencies of Eng.

bin 0 K_0, C_3, C_6, \dots
 bin 1 C_1, C_4, C_7, \dots
 bin 2 C_2, C_5, C_8, \dots

} $|k| = 3$

Kasiski Test

Look for repeated "trigrams" or bigger.

$P_{47} P_{48} P_{49} P_{50}$
 $K_i K_{i+1} K_{i+2} K_{i+3}$
 G H Y X
 47

$K_i K_{i+1} K_{i+2} K_{i+3}$
 G H Y X
 167

length of keyword divides into $(167-47)$

$len(k) \mid 120.$

Find all repeats

$$w_1 : 47, 167, 267 \rightarrow 120, 100$$

$$w_2 : 85, 115 \rightarrow 30$$

$$w_3 : 122, 262, 402 \rightarrow 140, 160$$

$$\gcd(120, 100, 30, 140, 160) = 10$$

Index of Coincidence

Given a multiset of items

f_1 10 Skittles

f_2 5 Snickers

f_3 25 Mrms

f_4 $\frac{10}{50}$ gummy worms

k unique

Choose 2 items @ random.

What's the probability they are the same?

$$\text{Ans} = \text{locC}(\{10, 5, 25, 10\})$$

$$f_1 + f_2 + \dots + f_k = n$$

$$\begin{aligned} \text{locC} &= \frac{10}{50} \times \frac{9}{49} + \frac{5 \times 4}{50 \times 49} + \frac{25 \times 24}{50 \times 49} + \frac{10 \times 9}{50 \times 49} \\ &= \frac{90 + 20 + 600 + 90}{50 \times 49} = \frac{800}{50 \times 49} = \boxed{\frac{16}{49}} \end{aligned}$$

$$\text{locC} = \frac{\sum_{i=1}^k f_i(f_i - 1)}{n(n-1)}$$

random : 5 letters $\frac{1}{5}, \frac{1}{5}, \frac{1}{5}, \frac{1}{5}, \frac{1}{5}$ $\text{locC} \sim \frac{1}{5}$

$$\begin{aligned} &\frac{1}{2}, \frac{3}{8}, \frac{1}{24}, \frac{1}{24}, \frac{1}{24} \sim \frac{1}{2} \times \frac{1}{2} + \frac{3}{8} \times \frac{3}{8} \\ &= \frac{1}{4} + \frac{9}{64} = \frac{25}{64} \end{aligned}$$

random 26 letters $\text{lofC} \sim \frac{1}{26}$ ✓

English $\sim \underline{\underline{.0676}}$

lofC is independent of which letter has which freq.

① Guess keyword length ^{l_k=} 3, 4, 5, 6, ...

② for each guess partition the cipher text into the appropriate bins.

③ Calculate lofC of each bin

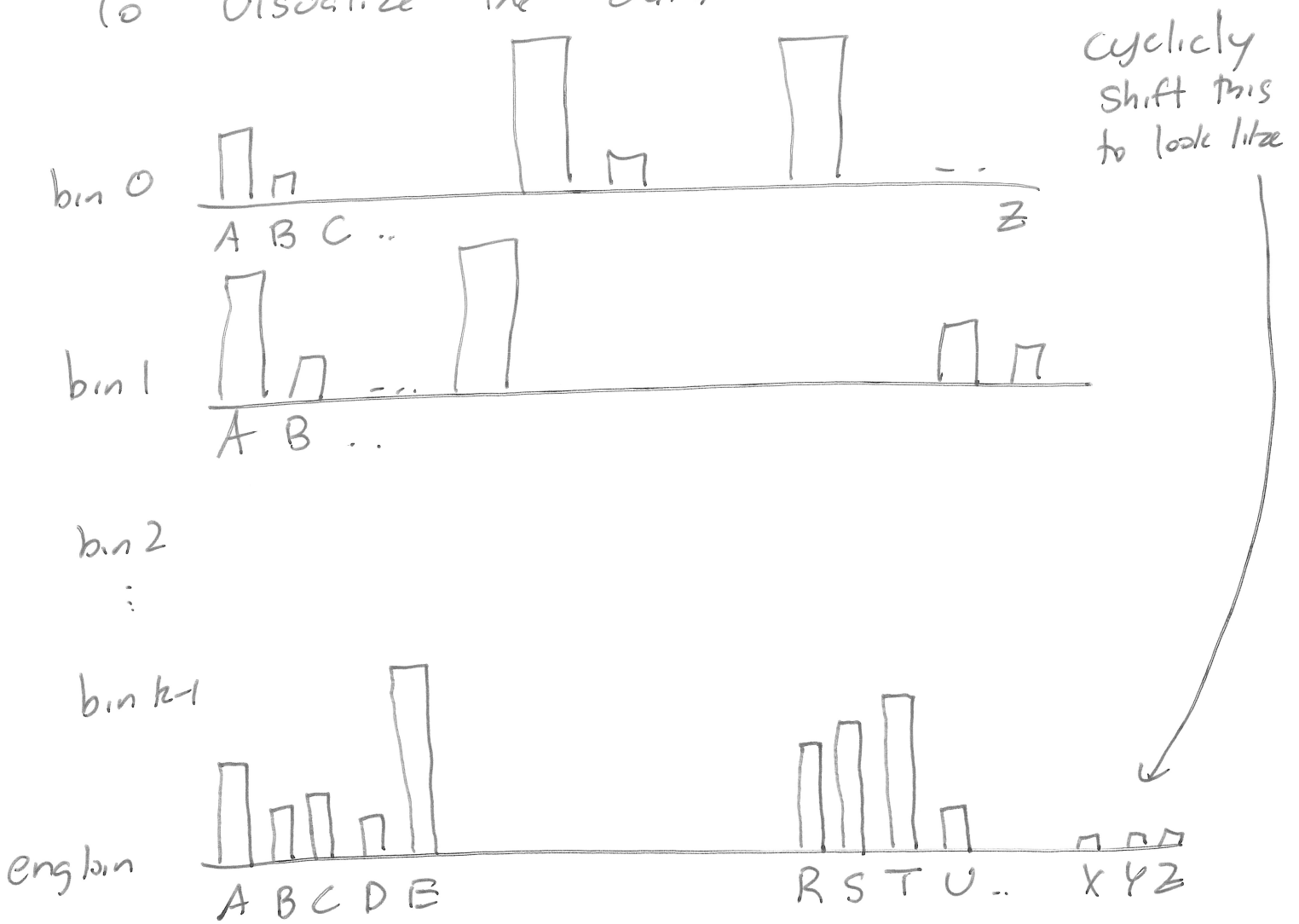
if each lofC is closer to .0676

than $\frac{1}{26} = .0378?$, then this is probably the keyword length (BREAK)

bins	0,	1,	2,	...	$k-1$ → keyword length
A	0	2	5		K arrays of size 26
B	3	0	0		
C	1	0	0		
D	6	0	0		
⋮	⋮	⋮	⋮		

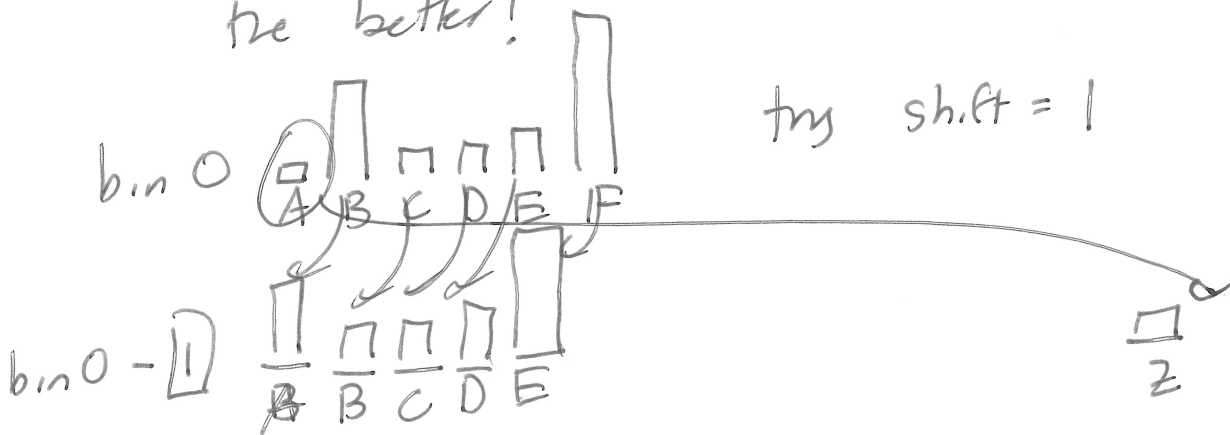
z

To visualize the data



Try 26 shifts.

For each shift, line up the bar graph for the bin w/ English. The "closer" they look the same the better!



Mutual Index of Coincidence

2 multisets

10 Sk
5 Gm
25 mmm
10 Sn

50

5 Sk
25 Gm
10 mmm
10 Sn

50

$$= \frac{10 \times 5 + 5 \times 25 + 25 \times 0 + 10 \times 0}{50 \times 50}$$

$$n = f_1 + f_2 + \dots + f_k \quad \text{Set 1}$$

$$m = g_1 + g_2 + \dots + g_k \quad \text{Set 2}$$

$$MIC = \frac{\sum_{i=1}^k f_i \cdot g_i}{n \cdot m}$$

Of the 26 possible shifts, whichever maximizes MIC is likely to be the shift of that bin, i.e. the letter for that keyword position!