

So far: Shift, Affine

$$f(x) = 3x + 2$$

| x | f(x) |
|---|------|
| A | D    |
| B | E    |
| C | F    |
| ⋮ | ⋮    |

| x | f(x) |
|---|------|
| A | C    |
| B | F    |
| ⋮ | ⋮    |

|   |   |
|---|---|
| X | A |
| Y | B |
| Z | C |

Z | Z (fixed point)

Generalize this idea → any valid chart could be a key!

| x | f(x)   |
|---|--------|
| A | P 26   |
| B | A 25   |
| C | M 24   |
| D | X etc. |

(1) Pros

- lots of possible keys!!!  
 $26! \sim 10^{18}$  or more

(2) Con

harder to store key  
 (bigger)

But, since about the year 1000,  
substitution ciphers have been decrypted!

How?

al-Kindi - different letters appear diff # of  
times  
substitution - set of letter freq.  
stays the same!

Invariant in substitution cipher  $\Rightarrow$  LETTER FREQ!

$\Rightarrow$  GUESSING, PROCESS OF ELIMINATION

$\Rightarrow$  OTHER LANG FEATURES

frequencies won't be a perfect map!

in English 12.7%  $\rightarrow$  E  
9.1%  $\rightarrow$  T



In small samples "error bar" is large.

Some samples might be biased.

Usually most freq letter is either E, T, A, O, S, H, R

Common digraphs, trigraphs "ED", "ING", "AND", "EN"

(1) Make guesses, but

(2) Be willing to backtrack if you  
hit something impossible.

(3) KEEP TRACK OF WHAT YOU'VE TRIED!

Beginning rough! 2 hrs → 6 letters  
next 20 letters takes 10 min!

## Queen Mary Communication

- 1) Hide in beer barrels (steganography)
- 2) Code  
Substitution +
  - (1) 36 code words (the, for, it, etc.)
  - (2) 4 null characters
  - (3) doublet - next char doubled "rr"  
"doublet" [code]
- 3) Loyalists bribed a guard!  
- guard double paid by Queen!
- 4) Sir Francis Walsingham (Queen Eliz. cryptanalyst)  
also getting messages!

## Additional bellst whistles

delete char

100 cipher text (00 ... 99)

assign by let freq e → 12 diff codes

t → 9 code

a → 8 codes

each 100 codes

will appear roughly equally!

MOST OF THESE WERE EVENTUALLY BROKEN!