

# CIS 3362 - 10/8/21

- ① Finish Mix Cols
- ② Key Schedule
- ③ Quiz Notes

- No extra notes, no calculator
- 4 formula sheets given
- Topics: bitwise ops, DES, AES

$$\begin{pmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{pmatrix} \times \begin{pmatrix} a3 & 17 & b6 & 12 \\ b4 & e3 & 47 & 34 \\ 78 & 42 & 92 & 56 \\ 26 & 98 & ee & 78 \end{pmatrix}$$

Mix Col Mat
Stk Matrix

Row 4 Col 3?

$$03 \times b6 + 01 \times 47 + 01 \times 92 + 02 \times \cancel{cc}$$

$\downarrow$                        $\downarrow$   
 47                      92

$$\begin{aligned}
 & 3 \times b6 \\
 & = (x+1)(x^7 + x^5 + x^4 + x^2 + x) \\
 & \quad \begin{matrix} \uparrow & \uparrow & \uparrow & \uparrow & \uparrow \\ 0011 & 1011 & 0110 & & \end{matrix} \\
 & = (x^8 + x^6 + x^5 + x^3 + x^2) + (x^7 + x^5 + x^4 + x^2 + x) \\
 & = \underline{(x^4 + x^3 + x + 1)} + \underline{(x^6 + x^5 + x^3 + x^2)} + \underline{(x^7 + x^5 + x^4 + x^2 + x)} \\
 & = \boxed{x^7 + x^6 + 1}
 \end{aligned}$$

$x^8 \equiv x^4 + x^3 + x + 1$   
 $\text{mod } (x^8 + x^4 + x^3 + x + 1)$

$$3 \times 66 = 11 \times 10110110$$

$$\begin{array}{r}
 10110110 \quad (1 \times 66) \\
 + 01101100 \quad (2 \times 66) \\
 \hline
 11011 \quad (x^8 = x^4 + x^3 + x^2 + 1) \\
 \hline
 11000001 \quad (C1)
 \end{array}$$

$$C7 \times e3$$

$$\begin{array}{r}
 2 \times \overset{CC}{\cancel{CC}} = 11001100 \times 2 \\
 = \cancel{1}0011000 \\
 \quad 11011 \\
 \hline
 1000011 \quad (83)
 \end{array}$$

$$\begin{array}{r}
 \boxed{C1} + \boxed{47} + \boxed{92} + \boxed{83} \\
 \hline
 \boxed{86} + \boxed{11} \\
 \hline
 \boxed{97}
 \end{array}$$

Example w/o overflow

$$\begin{array}{r}
 02 \times 73 = 01110011 \times 2 \\
 = 11100110 \quad (e6)
 \end{array}$$

# AES Key Schedule

## Examples

$$w[17] = AB \ CD \ 79 \ 3E$$

$$w[20] = 34 \ 56 \ 78 \ A4$$

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$$w[21] = 9F \ 9B \ 01 \ 9A$$

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$$w[16] = 49 \ 6A \ CB \ 73$$

$$w[19] = 87 \ 65 \ 4E \ FD$$

$$w[20] =$$

$$\text{rot}(w[19]) = 65 \ 4E \ FD \ 87$$

$$\text{sub}(\text{rot}(w[19])) = 4D \ 2F \ 54 \ 17 \ (\text{from AES Sbox})$$

$$\oplus \text{roor}[5] = 10 \ 00 \ 00 \ 00$$

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$$\text{temp} = 5D \ 2F \ 54 \ 17$$

$$\oplus w[16] = 49 \ 6A \ CB \ 73$$

$$\rightarrow \boxed{i=20/4}$$

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$$\boxed{14 \ 45 \ 9F \ 64}$$

# QUIZ

4 SHEETS (I GAVE)

① Bitwise Ops (  $|$ ,  $\&$ ,  $\wedge$ ,  $\gg$ ,  $\ll$  )

② DES

Sboxes

IP

Key Schedule

③

AES

Sub bytes

Shift Rows

MixCols (1 entry)

Key Schedule