

AES #2

Friday, October 9, 2020 11:30 AM

1. Mix Cols Review
2. AES Key Schedule
3. Helper Mix Cols Program
4. Helper DES S-box Program
5. AES code

Mix Cols

02	03	01	01
01	02	03	01
01	01	02	03
03	01	01	02

x

63	7c	77	93
36	3f	cd	26
f1	1a	0c	13
16	4b	c6	d2

Note: first matrix is fixed for the algorithm.
Second matrix is the state matrix right before Mix Cols.

Entry in row 2, column1:

$$01 \times 63 + 02 \times 36 + 03 \times f1 + 01 \times 16$$
$$63 + 6c + 08 + 16$$

Rules for multiplication in the field:

1. mult 2 is a left shift
2. If there is an overflow bit, that bit is equivalent to xoring with 0001 1011, from the AES polynomial.
3. All other multiplications can be created as a combination of these rules and addition, which is XOR in the field.

02 x 36 = 0011 0110 left shifted by 1 bit
 0110 1100 = **6c**

03 x f1 = 02 x f1 +
 01 x f1

02 x f1 = 1111 0001 left shifted by 1
 = 1 1110 0010 (overflow)
 = 1110 0010
 + 1 1011

 1111 1001

03 x f1 = 1111 1001 (02 x f1)
 + 1111 0001 (01 x f1)

 0000 1000 = **08**

Final answer:

63 + **6c** + **08** + 16 use the XOR chart for HEX

6 + 6 + 0 + 1 = 1 (xor)
 3 + c + 8 + 6 = f + e = 1

Final Answer is **11**.

AES Key Schedule

bytes are 8 bits, words are 32 bits, so 4 bytes = word

KeyExpansion(byte key[16], word w[44]) {

word temp;

for (i=0; i<4; i++) w[i] = (key[4*i],key[4*i+1],key[4*i+2],key[4*i+3]);

for (i=4; i<44; i++) {

temp = w[i-1];

if (i%4 == 0) // Beginning of the new round key

temp = SubWord(RotWord(temp)) XOR Rcon[i/4]

```

    w[i] = w[i-4] XOR temp;
  }
}

```

Round 0 key is the original key.

For round 1 to round 10, the keys are $w[4] \dots w[7]$ R1

$w[8] \dots w[11]$ R2

$w[4i] \dots w[4i+3]$ Round i key

Unless it's the beginning of a new round key, all we do to generate the next 32 bits, is XOR the last 32 bits with the 32 bits from 4 times ago.

But, when we begin a new round, we want to mess stuff up...so here is what we do:

RotWord is a cyclic left rotation by one byte.

$i=36$ in this example..

Let's say that $w[35] = 7f8d292f$ (in hex)

$\text{RotWord}(w[35]) = 8d292f7f$

Next step is to do a SubBytes on the buffer:

$\text{SubBytes}(8d) = 5d$ (from S box)

$\text{SubBytes}(29) = a5$ (from S box)

$\text{SubBytes}(2f) = 15$ (from S box)

$\text{SubBytes}(7f) = d2$

So new buffer is 5da515d2, after subbytes.

XOR with $\text{Rcon}[36/4] = \text{Rcon}[9]$.

Here are the Rcon values in hex:

I	1	2	3	4	5	6	7	8	9	10
Rcon	01000	02000	04000	08000	10000	20000	40000	80000	1B000	36000
[i]	000	000	000	000	000	000	000	000	0000	000

Our example:

5da515d2 XOR 1b000000 (since round 9)

46a515d2, this is our new buffer (for temp)

Finally to get $w[i]$, we have to XOR it with $w[i-4]$, so I need to give you the value of $w[32]$.

For this example $w[32] = \text{ead27321}$

```
4 6 a 5 1 5 d 2
e a d 2 7 3 2 1
-----
a c 7 7 6 6 f 3
```

Sbox program verification

Input: f3e = 1111 0011 1110

$\text{Sbox1}(111100) = \text{row } 10 = 2, \text{col} = 1110 = 14$

For Quiz

Preprint all the necessary tables.

DES tables

AES tables

Bin->Hex chart