

Example. Convert a very small (in absolute value) decimal number to binary form.

Consider a small value $x = 0.67055225372314453125 \times 10^{-6} = 0.00000067055225372314453125$.

To convert x to binary form, multiply x by 2^{18} as a first try. (Note: Use the exponent 18 for base 2 because it is 3 times of the exponent from base 10, due to the estimate $2^{10} = 1024 \approx 10^3$, and the exponent ratio is $\frac{10}{3} \approx 3$):

$$(0.67055225372314453125 \times 10^{-6}) \cdot (2^{18}) = 0.17578125.$$

Try a few more until the result becomes > 1 :

$$(0.67055225372314453125 \times 10^{-6}) \cdot (2^{19}) = 0.3515625$$

$$(0.67055225372314453125 \times 10^{-6}) \cdot (2^{20}) = 0.703125$$

$$(0.67055225372314453125 \times 10^{-6}) \cdot (2^{21}) = \underline{1}.40625 = y.$$

↖ equals 2^{-21}

We then multiply the decimal portion of the value y by 2, then repeating the process:

$$0.40625 \times 2 = \underline{0}.8125$$

↖ equals 2^{-22}

$$0.8125 \times 2 = \underline{1}.625$$

↖ equals 2^{-23}

$$0.625 \times 2 = \underline{1}.25 \text{ (the "1" equals } 2^{-24}\text{)}$$

$$0.25 \times 2 = \underline{0}.5 \text{ (the "0" equals } 2^{-25}\text{)}$$

$$0.5 \times 2 = \underline{1}.0 \text{ (the "1" equals } 2^{-26}\text{)}$$

Therefore,

$$x = 0.67055225372314453125 \times 10^{-6} = 2^{-21} + 2^{-23} + 2^{-24} + 2^{-26} = 101101 \times 2^{-21}$$