

How to convert a decimal value into the binary format using the IEEE floating point arithmetic standard:

Example. Convert the number 27.56640625 into the binary floating point format.

(Step 1) Convert the integer portion (i.e. 27) into binary.

$$\begin{array}{r}
 2 \overline{) 27} \\
 \underline{2 \cdot 13} \\
 27 - 26 = 1 \quad (\text{i.e. } 27 = 2 \cdot 13 + 1) \\
 \underline{2 \cdot 6} \\
 12 - 12 = 0 \quad (\text{etc.}) \\
 \underline{2 \cdot 3} \\
 6 - 6 = 0 \\
 \underline{1} \\
 1 - 1 = 0
 \end{array}$$

Thus, $27 = 1 + 2^1 + 2^2 + 2^4 = 11011$

(Step 2) Convert the decimal portion (i.e. 0.56640625) into binary

$$\begin{array}{r}
 0.56640625 \\
 \times 2 \\
 \hline
 \textcircled{1} .13281250 \\
 \times 2 \\
 \hline
 0.2656250 \\
 \times 2 \\
 \hline
 0.531250 \\
 \times 2 \\
 \hline
 \textcircled{1} .06250 \\
 \times 2 \\
 \hline
 0.1250 \\
 \times 2 \\
 \hline
 0.250 \\
 \times 2 \\
 \hline
 0.50 \\
 \times 2 \\
 \hline
 \textcircled{1} 0
 \end{array}$$

(Step 3) Combine integer & decimal portions of steps 1 and 2.

Therefore,

$$\begin{aligned}
 27.56640625 &= 11011.10010001 \text{ (base 2)} \\
 &= 1.101110010001 \times 2^4 \text{ (normalize)}
 \end{aligned}$$

(Step 4) Apply the formula $(-1)^s 2^{c-1023} (1+f)$

$$\begin{aligned}
 s &= 0, \quad c = 1023 + 4 = 1027 = 1000000011 \text{ (base 2)} \\
 f &= 101110010001
 \end{aligned}$$

Thus, $0.56640625 = 1 \cdot \left(\frac{1}{2}\right) + 0 \cdot \left(\frac{1}{2}\right)^2 + 0 \cdot \left(\frac{1}{2}\right)^3 + 1 \cdot \left(\frac{1}{2}\right)^4 + 0 \cdot \left(\frac{1}{2}\right)^5 + 0 \cdot \left(\frac{1}{2}\right)^6 + 0 \cdot \left(\frac{1}{2}\right)^7 + 1 \cdot \left(\frac{1}{2}\right)^8 = 0.10010001 \text{ (base-2)}$

Answer: 0 1000000011 101110010001 (40 zeros followed)