## Homework \#1

Problems 1.1, 1.2, 1.6, 1.7, 1.8

## 1.1

a) For the graph the x and y values can be found easily by using the value of 20 for Speedup ${ }_{\text {enhanced }}$ and the values 10,20 , and 30 for the percentage of vectorization or
Fraction ${ }_{\text {enhanced }}$.
Plugging these values into
Net Speedup $=1 /\left(\left(1-\right.\right.$ Fraction $\left._{\text {enhanced }}\right)+\left(\right.$ Fraction $_{\left.\left.\text {enhanced } / \text { Speedup }_{\text {enhanced }}\right)\right)}$
Gives

| X | Y |
| :--- | :--- |
| 10 | 1.105 |
| 20 | 1.235 |
| 30 | 1.399 |


b) Using Amdahl's Law the following equation can be used:

Speedup $_{\text {overall }}=1 /\left(\left(1-\right.\right.$ Fraction $\left._{\text {enhanced }}\right)+\left(\right.$ Fraction $_{\text {enhanced }} /$ Speedup $\left._{\text {enhanced }}\right)=2$
Rearranging this to solve for Fraction $_{\text {enhanced }}$ gives the equation:
Fraction $_{\text {enhanced }}=$ speedup $_{\text {overall }} *$ speedup $_{\text {enhanced }}-$ speedup $_{\text {enhanced }} /$ speedup $_{\text {overall }} *$ speedup $_{\text {enhanced }}$ - speedup ${ }_{\text {overall }}$

So,
Fraction $_{\text {enhanced }}=(2 * 20-20) /(2 * 20-2)=.526$
Therefore, the percentage vectorization needed to gain a speedup of 2 is $52.6 \%$
c)

Since the maximum speedup attainable would be 20 , one-half of this value would be a Fraction $_{\text {enhanced }}=10$.
So,
Speedup $_{\text {overall }}=1 /\left(\left(1-\right.\right.$ Fraction $\left._{\text {enhanced }}\right)+\left(\right.$ Fraction $_{\text {enhanced }} /$ Speedup $\left._{\text {enhanced }}\right)=10$

Rearranging this to solve for Fraction $_{\text {enhanced }}$ gives the equation:
Fraction $_{\text {enhanced }}=$ speedup $_{\text {overall }} *$ speedup $_{\text {enhanced }}-$ speedup $_{\text {enhanced }} /$ speedup $_{\text {overall }} *$ speedup $_{\text {enhanced }}-$ speedup $_{\text {overall }}$

As above,
Fraction $_{\text {enhanced }}=(10 * 20-20) /(10 * 20-10)=.95$
Therefore, the percentage vectorization needed to gain one-half of the maximum speedup attainable is $95 \%$.
d)

Using the hardware doubling the following equation can be generated:
Speedup ${ }_{\text {overall }}=1 /((1-.7)+(.7 / 40)$
Solving the above equation gives a Speedup ${ }_{\text {overall }}$ of 3.149

To find what percentage of vectorization would need to be achieved to match the hardware doubling method simply solve for Fraction enhanced as follows:
 speedup $_{\text {overall }}$

So,
Fraction $_{\text {enhanced }}=(3.14 * 20-20) /(3.14 * 20-3.14)=.718$
Therefore, a percentage vectorization of around $1 \%$ would match the hardware doubling technique. I would recommend using the compiler to crew to gain the extra $1 \%$ vectorization.

## 1.2

a) Speedup $=$ Time $_{\text {original }} /$ Time $_{\text {enhanced }}$

Since the speedup value is 10 :
.5 Time $_{\text {enhanced }}=\left(\right.$ Fraction $_{\text {enhanced }} *$ Time $\left._{\text {orginal }}\right) / 10$
Solving for Percentage ${ }_{\text {original }}$ :
Fraction $_{\text {enhanced }}=10 *$ Time $_{\text {enhanced }} / 2 *$ Time $_{\text {original }} \quad($ Equation 1)
Since $50 \%$ of enhanced execution time is spent is used on the enhancement, the following can also be found:
.5 Time $_{\text {enhanced }}=\left(1-\right.$ Fraction $\left._{\text {enhanced }}\right) *$ Time $_{\text {original }}$
Plugging Fraction enhanced found in Equation 1 into the previous equation and solving for Time $_{\text {original }}$ Time $_{\text {enhanced }}$ yields:

$$
\text { Speedup }_{\text {overall }}=5.5
$$

b) To solve the speedup found in 1.2a must be used with the equation:

Speedup $_{\text {overall }}=1 /\left(\left(1-\right.\right.$ Fraction $\left._{\text {enhanced }}\right)+\left(\right.$ Fraction $_{\text {enhanced }} /$ Speedup $\left._{\text {enhanced }}\right)$
Since the speedup ${ }_{\text {overall }}$ is 5.5 and the speedup ${ }_{\text {enhanced }}=10$ there is only one variable left to solve. The following equation can be used:
$5.5=1 /\left(\left(1-\right.\right.$ Fraction $\left._{\text {enhanced }}\right)+\left(\right.$ Fraction $\left._{\text {enhanced }} / 10\right)$
Solving for Fraction enhanced the percentage can then be found.
Percentage of original execution time: $91 \%$

## 1.6

Execution time is the primary concern so the following equation should be used when making the decision:
CPU Time $=\mathrm{IC} *$ CPI $*$ Clock Cycle Time
Starting with the un-optimized version we know that CPI is 1 so:
CPU Time ${ }_{\text {un }}=\mathrm{IC} * 1 *$ Clock Cycle Time (Equation 1)
We also know that the clock rate of the un-optimized machine is $5 \%$ higher than the optimized machine so: $(100 \%-5 \%)$ Clock Cycle Time ${ }_{\text {op }}=$ Clock Cycle Time ${ }_{\text {un }}$ (Equation 2)

The optimized machine does not execute $1 / 3$ of the load and store instructions that the un-optimized machine does, and load and store instructions make up $30 \%$ of the total instructions so: $\mathrm{IC}_{\mathrm{op}}=.9 \mathrm{IC}_{\mathrm{un}}$ (Equation 3)

Using the equations above as well as information stated in the exercise the following equation can be constructed:
$\mathrm{CPU}_{\mathrm{op}}=.9 \mathrm{IC}_{\mathrm{un}} * 1 * 1.05$ Clock Cycle Time ${ }_{\mathrm{un}}$
Now performance of the optimization can be compared with the un-optimized version by using the speedup equation of:

Speedup $_{\text {overall }}=\left(\mathrm{IC}_{\mathrm{un}} *\right.$ Clock Cycle Time $\left.{ }_{\mathrm{un}}\right) /\left(.9 \mathrm{IC}_{\mathrm{un}} * 1.05\right.$ Clock Cycle Time $\left.{ }_{\mathrm{un}}\right)$
Solving the previous equation gives a Speedup ${ }_{\text {overall }}$ of 1.06. Therefore, by using the optimization technique a $6 \%$ increase in performance is realized.

## 1.7

a) $\operatorname{MIPS}=\operatorname{Clock} \operatorname{Rate} /\left(\mathrm{CPI} * 10^{6}\right)$
$\operatorname{MIPS}_{\text {software }}=\left(16.67 * 10^{6}\right) /\left(6 * 10^{6}\right)=2.8$
$\operatorname{MIPS}_{\text {coprocessor }}=\left(16.67 * 10^{6}\right) /\left(10 * 10^{6}\right)=1.7$
b) Instruction Count $=$ Execution Time * $\left(\right.$ MIPS $\left.* 10^{6}\right)$

Instruction Count software $=13.6 *\left(2.8 * 10^{6}\right)=3.8 * 10^{7}$
Instruction Count ${ }_{\text {coprocessor }}=1.08 *\left(1.7 * 10^{6}\right)=1.8 * 10^{6}$
c) Using the coprocessor because each floating point operation definitely corresponds to one instruction find the non floating point instructions:

NFP $=($ Instruction Count coprocessor ) - Total Instructions (From Exercise)
So,
NFP $=\left(1.08 * 10^{6}\right)-195,578=1.6 * 10^{6}$
Floating Point Instructions $=$ Total Instructions - NFP
So,
$\operatorname{FPI}=\left(3.8 * 10^{7}\right)-\left(1.6 * 10^{6}\right)=3.6 * 10^{7}$
Instructions per floating point operation $=$ Floating Point Instructions/ Floating Point Operations
So,
Instructions per floating point operation $=3.6 * 10^{7} / 195,578=185$
Therefore, on average, in software 185 integer instructions are required to perform a floating-point operation.
d) MFLOPS $=$ Number of floating point operations in program/(Execution Time $* 10^{6}$ )

So,
MFLOPS $=195,578 /\left(1.08 * 10^{6}\right)=0.18$

## 1.8

a) To find the number of good dies per wafer use:

Good Dies per Wafer $=$ Dies per Wafer * Die Yield $($ Equation 1)
Where
Dies per Wafer $=\left(\left(\pi^{*}(\text { Wafer Diameter } / 2)^{2)} / \text { Die area }\right)-\pi^{*} \text { Wafer Diameter/(2* Die Area) }\right)^{1 / 2}$
And
Die Yield $=$ Wafer yield $*(1+(\text { Defects per unit area } * \text { Die area }) / \alpha)^{-\alpha}$

Using a 20 cm wafer, a defect density of $1 \mathrm{~cm}^{2}, \alpha$ of 3 , and a wafer yield of $95 \%$ the following table can be created by substituting these values into Equation 1 above.

| Microprocessor | Dies per Wafer | Die Yield | Good Chips |
| :--- | :--- | :--- | :--- |
| MIPS 4600 | 357 | .48 | 171 |
| PowerPC 603 | 321 | .45 | 144 |
| HP 71x0 | 128 | .21 | 26 |
| Digital 21064 A | 154 | .26 | 40 |
| SuperSPARC/60 | 94 | .15 | 14 |

b) Using the good chip total found in 1.8 a the die cost would be found by dividing the wafer cost by the total number of good dies per wafer. Doing this yields the die cost as illustrated below.

| Microprocessor | Good Chips | Wafer Cost | Die Cost |
| :--- | :--- | :--- | :--- |
| MIPS 4600 | 171 | $\$ 3200$ | $\$ 18.7$ |
| PowerPC 603 | 144 | $\$ 3400$ | $\$ 23.6$ |
| HP 71x0 | 26 | $\$ 2800$ | $\$ 107.7$ |
| Digital 21064 A | 40 | $\$ 4000$ | $\$ 100$ |
| SuperSPARC/60 | 14 | $\$ 4000$ | $\$ 285.7$ |

c)

To find the cost for each good, tested, and packaged good use the values found above in part a and b.

| Microprocessor | Die Cost | Testing | Packaging | Total Cost |
| :--- | :--- | :--- | :--- | :--- |
| MIPS 4600 | $\$ 18.7$ | $\$ 1.7$ | $\$ 12$ | $\$ 32.4$ |
| PowerPC 603 | $\$ 23.6$ | $\$ 2$ | $\$ 20$ | $\$ 45.6$ |
| HP 71x0 | $\$ 107.7$ | $\$ 7.9$ | $\$ 70$ | $\$ 185.6$ |
| Digital 21064 A | $\$ 100$ | $\$ 5.1$ | $\$ 50$ | $\$ 155.1$ |
| SuperSPARC/60 | $\$ 285.7$ | $\$ 6$ | $\$ 30$ | $\$ 321.7$ |

Testing is calculated using:
Testing Cost $=($ Hourly Cost/Time Unit $) /$ Die Yield
d)

Solving this problem involves doing the same steps as in part a and babove. Instead of using a defect density of $1 \mathrm{~cm}^{2}$, defect densities of .6 and $1.2 \mathrm{~cm}^{2}$ can be used. Then step c is repeated in the same fashion using the new data.

Following these steps yields the following:

| Defect Density <br> $\left(\mathrm{cm}^{2}\right)$ | Packaging | Die Cost | Testing Cost | Total Cost |
| :--- | :--- | :--- | :--- | :--- |
| .6 | 30 | $\$ 157.6$ | $\$ 3.3$ | $\$ 190.9$ |
| 1.2 | 30 | $\$ 386.8$ | $\$ 8.1$ | $\$ 424.9$ |

e)

Solving this problem involves following the steps laid out in parts a - c. Instead of using a defect density of $1 \mathrm{~cm}^{2}$ this problem uses a defect density of $.8 \mathrm{~cm}^{2}$. The steps laid out in parts a - c should be repeated for two $\alpha$ values of 3 and 4.5. Solving the steps laid out above with these new values yield the following:

| $\alpha$ | Packaging | Die Cost | Testing Cost | Total Cost |
| :--- | :--- | :--- | :--- | :--- |
| 3 | $\$ 50$ | $\$ 80$ | $\$ 3.9$ | $\$ 133.9$ |
| 4.5 | $\$ 50$ | $\$ 83.8$ | $\$ 4.2$ | $\$ 138$ |

