

# Dijkstra's Algorithm Definitions

- $s$  = source node
- $N$  = set of nodes so far incorporated by the algorithm
- $c(i, j)$  = link cost from node  $i$  to node  $j$ 
  - $c(i, i) = 0$
  - $c(i, j) = \infty$  if the two nodes are not directly connected
  - $c(i, j) \geq 0$  if the two nodes are directly connected
- $D(v)$  = cost of least-cost path from node  $s$  to node  $v$  currently known (at termination,  $D(v)$  will be the least-cost path from  $s$  to  $v$ )

# Dijkstra's Algorithm

- Step 1 [Initialization]
  - $N = \{s\}$  Set of nodes so far incorporated consists of only source node
  - $D(v) = c(s, v)$  for  $v \neq s$
  - Initial path costs to neighboring nodes are simply link costs
- Step 2 [Get Next Node]
  - Find neighboring node not in  $N$  with least-cost path from  $s$
  - Incorporate node into  $N$
- Step 3 [Update Least-Cost Paths]
  - $D(v) = \min[D(v), D(w) + c(w, v)]$  for all  $w \notin N$
- Return to Step 2. Algorithm terminates when all nodes have been added to  $T$

# Bellman-Ford Algorithm Definitions

- $s =$  source node
- $c(i, j) =$  link cost from node  $i$  to node  $j$ 
  - $c(i, i) = 0$
  - $c(i, j) = \infty$  if the two nodes are not directly connected
  - $c(i, j) \geq 0$  if the two nodes are directly connected
- $h =$  maximum number of links in path at current stage of the algorithm
- $D_h(v) =$  cost of least-cost path from  $s$  to  $v$  under constraint of no more than  $h$  links

# Bellman-Ford Algorithm

- Step 1 [Initialization]

- $D_0(v) = \infty$ , for all  $v \neq s$
- $D_h(s) = 0$ , for all  $h$

- Step 2 [Update]

- For each successive  $h \geq 0$ :

- For each  $v \neq s$ , compute

$$D_{h+1}(v) = \min_w [D_h(w) + c(w, v)]$$

;  $w = v$ 's neighbor