# More Chaining and Storing Matrixes 

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Sequential Approach...


64 Elements in sequence: $\mathrm{T}_{\mathrm{s}}=64 *(8+9)=1088$

## Using Pipeline Approach...



Using pipelining it takes 8 units of time to fill pipeline and produce first result, each unit of time after that produces another result $\mathrm{T}_{\mathrm{p}+}=8+63$


The multiplication pipeline takes 9 units of time to fill, and produces another result after each additional unit of time
$\mathrm{T}_{\mathrm{p}^{*}}=9+63$

The combination of the two $T_{p}=T_{p+}+T_{p^{*}}=8+63+9+63=143$

## Pipeline plus Chaining...



Operation using Chaining $T_{c}=17+63=80$

Review of time differences in the three approaches...

Sequential: $\mathrm{T}_{\mathrm{s}}=17 * 64=1088$

Pipelining: $\mathrm{T}_{\mathrm{p}}=8+63+9+63=143$

Chaining: $\quad \mathrm{T}_{\mathrm{c}}=17+63=80$

Storing Matrixes in a SISD Architecture w/ Memory Interleaving...

Matrix

| $\mathrm{A}_{11}$ | $\mathrm{~A}_{12}$ | $\mathrm{~A}_{13}$ | $\mathrm{~A}_{14}$ |
| :--- | :--- | :--- | :--- |
|  | $\mathrm{~A}_{21}$ | $\mathrm{~A}_{22}$ | $\mathrm{~A}_{23}$ |
|  | $\mathrm{~A}_{24}$ |  |  |
|  | $\mathrm{~A}_{32}$ | $\mathrm{~A}_{33}$ | $\mathrm{~A}_{34}$ |
|  | $\mathrm{~A}_{41}$ | $\mathrm{~A}_{42}$ | $\mathrm{~A}_{43}$ |
| $\mathrm{~A}_{44}$ |  |  |  |

4 Memory Modules

| $\mathrm{M}_{1}$ | $\mathrm{M}_{2}$ | $\mathrm{M}_{3}$ | $\mathrm{M}_{4}$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{~A}_{11}$ | $\mathrm{~A}_{21}$ | $\mathrm{~A}_{31}$ | $\mathrm{~A}_{41}$ | One column of the matrix can be accessed at one time.

$\begin{array}{llll}\mathrm{A}_{12} & \mathrm{~A}_{22} & \mathrm{~A}_{32} & \mathrm{~A}_{42}\end{array}$
$\begin{array}{llll}\mathrm{A}_{13} & \mathrm{~A}_{23} & \mathrm{~A}_{33} & \mathrm{~A}_{43}\end{array}$
$\begin{array}{llll}\mathrm{A}_{14} & \mathrm{~A}_{24} & \mathrm{~A}_{34} & \mathrm{~A}_{44}\end{array}$

## Storing the Matrix by Column...

Matrix

| $\mathrm{A}_{11}$ |  |  |  |
| :--- | :--- | :--- | :--- |
| $\mathrm{~A}_{12}$ | $\mathrm{~A}_{13}$ |  | $\mathrm{~A}_{14}$ |
| $\mathrm{~A}_{21}$ | $\mathrm{~A}_{22}$ | $\mathrm{~A}_{23}$ | $\mathrm{~A}_{24}$ |
| $\mathrm{~A}_{31}$ | $\mathrm{~A}_{32}$ | $\mathrm{~A}_{33}$ | $\mathrm{~A}_{34}$ |
| $\mathrm{~A}_{41}$ | $\mathrm{~A}_{42}$ | $\mathrm{~A}_{43}$ | $\mathrm{~A}_{44}$ |

4 Memory Modules

| $\mathrm{M}_{1}$ | $\mathrm{M}_{2}$ | $\mathrm{M}_{3}$ |
| :--- | :--- | :--- |
| $\mathrm{M}_{4}$ |  |  |
| $\mathrm{~A}_{11}$ | $\mathrm{~A}_{12}$ | $\mathrm{~A}_{13}$ |
| $\mathrm{~A}_{14}$ |  |  |
| $\mathrm{~A}_{21}$ | $\mathrm{~A}_{22}$ | $\mathrm{~A}_{23}$ |
| $\mathrm{~A}_{31}$ | $\mathrm{~A}_{24}$ |  |
| $\mathrm{~A}_{32}$ | $\mathrm{~A}_{33}$ | $\mathrm{~A}_{34}$ |
| $\mathrm{~A}_{41}$ | $\mathrm{~A}_{42}$ | $\mathrm{~A}_{43}$ |
|  | $\mathrm{~A}_{44}$ |  |

One Row can be accessed at a time with this storage
technique.

$$
\begin{array}{llll}
\mathrm{A}_{41} & \mathrm{~A}_{42} & \mathrm{~A}_{43} & \mathrm{~A}_{44}
\end{array}
$$

## Sometimes we need to access both rows and columns fast...

Matrix

| $\mathrm{A}_{11}$ | $\mathrm{~A}_{12}$ |  |  |
| :--- | :--- | :--- | :--- |
|  | $\mathrm{~A}_{13}$ | $\mathrm{~A}_{14}$ |  |
|  | $\mathrm{~A}_{21}$ | $\mathrm{~A}_{22}$ | $\mathrm{~A}_{23}$ |
|  | $\mathrm{~A}_{24}$ |  |  |
|  | $\mathrm{~A}_{32}$ | $\mathrm{~A}_{33}$ | $\mathrm{~A}_{34}$ |
|  | $\mathrm{~A}_{41}$ | $\mathrm{~A}_{42}$ | $\mathrm{~A}_{43}$ |
| $\mathrm{~A}_{44}$ |  |  |  |

4 Memory Modules


By using a skewed matrix representation, we can now access each row at a time, as well as access each column at a time.

Sometimes we need access to the main diagonal as well as rows and columns...

## Matrix

| $\mathrm{A}_{11}$ | $\begin{array}{llll}\mathrm{A}_{12} & \mathrm{~A}_{13} & \mathrm{~A}_{14}\end{array}$ |  |  |
| :---: | :---: | :---: | :---: |
| $\mathrm{A}_{21}$ | $\mathrm{A}_{22}$ | $\mathrm{A}_{23}$ | $\mathrm{A}_{24}$ |
| $\mathrm{A}_{31}$ | $\mathrm{A}_{32}$ | $\mathrm{A}_{33}$ | $\mathrm{A}_{34}$ |
| $\mathrm{A}_{41}$ | $\mathrm{A}_{42}$ | $\mathrm{A}_{43}$ | $\mathrm{A}_{44}$ |

5 Memory Modules


$$
\begin{array}{|lll}
\mathrm{A}_{21} & \mathrm{~A}_{22} & \mathrm{~A}_{23}
\end{array} \mathrm{~A}_{24}
$$

$$
\begin{array}{lllll}
\mathrm{A}_{34} & \boxed{\mathrm{~A}_{31}} & \mathrm{~A}_{32} & \boxed{\mathrm{~A}_{33}} \\
\mathrm{~A}_{43} & \mathrm{~A}_{44} & & \mathrm{~A}_{41} & \mathrm{~A}_{42}
\end{array}
$$

At the cost of adding another memory module and wasted space, we can now access the matrix by row, column, and main diagonal.

