





Projective Flow (weighted)

$$\mathcal{E}_{flow} = \sum \left(\mathbf{u}^{T} \mathbf{f}_{X} + f_{t} \right)^{2}$$

$$= \sum \left(\left(\frac{A\mathbf{x} + \mathbf{b}}{C\mathbf{x}^{T} + 1} - \mathbf{x} \right)^{T} \mathbf{f}_{x} + f_{t} \right)^{2}$$

$$= \sum \left(\left(A\mathbf{x} + \mathbf{b} - (C^{T}\mathbf{x} + 1)\mathbf{x} \right)^{T} \mathbf{f}_{x} + (C^{T}\mathbf{x} + 1)f_{t} \right)^{2}$$

$$\prod \text{minimize}$$

Projective Flow (weighted)
• (b) Homework 3 Derive this equation
Due Sept 28

$$(\sum \phi \phi^T) \mathbf{a} = \sum (\mathbf{x}^T \mathbf{f}_x - f_t) \phi$$

 $a = [a_1, a_2, b_1, a_3, a_4, b_2, c_1, c_2]^T$
 $\phi' = [f_x x, f_x y, f_x, f_y x, f_y y, f_y, xf_t - x^2 f_x - xyf_y, yf_t - xyf_x - y^2 f_y]$

_ 1











Algorithm-1

- Estimate "q" (using approximate model, e.g. bilinear model).
- □ Relate "q" to "p"
 - select four points S1, S2, S3, S4
 - apply approximate model using "q" to compute (x'_k, y'_k)
 - estimate exact "p":



True Projective
a x + a y + b
$\frac{x' = \frac{a_1 x + a_2 y + b_1}{x' = \frac{a_1 x + a_2 y + a_1}{x' = \frac{a_1 x + a_2 y + b_1}{x' = \frac{a_1 x + a_2 y + a_1}{x' = \frac{a_1 x + a_2 x + a_1}{x' = \frac{a_1 x + a_1}{x' = \frac{a_1 x + a_2}{x' = \frac{a_1 x + a_2}{x'$
$c_1 x + c_2 y + 1$
$y' = \frac{a_3x + a_4y + b_1}{a_3x + a_4y + b_1}$
$c_1 x + c_2 y + 1$
$\begin{bmatrix} x'_{k} \\ y'_{k} \end{bmatrix} = \begin{bmatrix} x_{k} & y_{k} & 1 & 0 & 0 & 0 & -x_{k}x'_{k} & -y_{k}x'_{k} \\ 0 & 0 & 0 & x_{k} & y_{k} & 1 & -x_{k}y'_{k} & -y_{k}y'_{k} \end{bmatrix} \mathbf{a}$
$\mathbf{a} = \begin{bmatrix} a_1 & a_2 & b_1 & a_3 & a_4 & b_2 & c_1 & c_1 \end{bmatrix}^T$



Final Algorithm

- □ A Gaussian pyramid of three or four levels is constructed for each frame in the sequence.
- □ The parameters "p" are estimated at the top level of the pyramid, between the two lowest resolution images, "g" and "h", using algorithm-1.

Final Algorithm

- □ The estimated "p" is applied to the next higher resolution image in the pyramid, to make images at that level nearly congruent.
- The process continues down the pyramid until the highest resolution image in the pyramid is reached.

Video Mosaics

- Mosaic aligns different pieces of a scene into a larger piece, and seamlessly blend them.
 - High resolution image from low resolution images
 - Increased filed of view

Steps in Generating A Mosaic

- □ Take pictures
- □ Pick reference image
- Determine transformation between frames
- □ Warp all images to the same reference view

Applications of Mosaics

- Virtual Environments
- □ Computer Games
- □ Movie Special Effects
- Video Compression





















Webpages

- http://n1nlf1.eecg.toronto.edu/tip.ps.gz
 Video Orbits of the projective group, S. Mann and R. Picard.
- http://wearcam.org/pencigraphy (C code for generating mosaics)



Webpages

- □ http://ww-bcs.mit.edu/people/adelson/papers.html
 - The Laplacian Pyramid as a compact code, Burt and Adelson, IEEE Trans on Communication, 1983.
- □ J. Bergen, P. Anandan, K. Hanna, and R. Hingorani, "Hierarchical Model-Based Motion Estimation", ECCV-92, pp 237-22.

Webpages

- http://www.cs.cmu.edu/afs/cs/project/cil/ftp/html/vsource.html (c code for several optical flow algorithms)
- ftp://csd.uwo.ca/pub/vision
 Performance of optical flow techniques
 (paper)

Barron, Fleet and Beauchermin

Webpages

- http://www.wisdom.weizmann.ac.il/~irani/abs tracts/mosaics.html ("Efficient representations of video sequences and their applications", Michal Irani, P. Anandan, Jim Bergen, Rakesh Kumar, and Steve Hsu)
- R. Szeliski. "Video mosaics for virtual environments", IEEE Computer Graphics and Applications, pages, 22-30, March 1996.

M. Irani and P. Anandan, Video Indexing Based on Mosaic Representations. Proceedings of IEEE, May, 1998.

http://www.wisdom.weizmann.ac.il/~irani/abs tracts/videoIndexing.html

Homework Due Feb 11

- (a) Derive linear system equation in Anandan's method Lecture 6, page 4, bottom slide.
- (b) Derive equations for Mann's method (weighted) Lecture
 7, page 5 top slide.
- (c) Derive equations for Mann's method (un-weighted) Lecture 7, page 10 bottom slide.

- Program-1 Due Feb 13

 (a) Implement Anandan's algorithm using affine transformation. To show the results generate a mosaic.

 (b) Implement Szeliski's algorithm using projective transformation. To show the results generate a mosaic.

 (c) Implement Mann's algorithm using projective transformation. To show the results generate a mosaic.

 Implement Mann's algorithm using projective transformation. To show the results generate a mosaic.

 Implement all four steps:

 Pyramid construction

 Motion estimation

 Image warping

 Coarse-to-fine refinement